#### EX/SC/CHEM/UG/CORE/TH/07/2024

# **B. Sc. CHEMISTRY EXAMINATION, 2024**

(3rd Semester)

**CHEMISTRY (CORE)** 

PAPER: CORE/CHEM/TH/07

Time: Two Hours Full Marks: 40

(20 marks for each Unit)

Use separate answer scripts for each Unit.

#### UNIT-3071 - P

## Answer any four questions:

5×4

 $1\times5$ 

- 1. Justify or criticize the following statements:
  - (a) Effect of pressure on boiling point and melting point of water is positive.
  - (b) For spontaneous changes, entropy change of the system is always positive.
  - (c) Effect of temperature on the magnitude of dimerization constant is always negative.

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- (d) Efficiency of Carnot Heat Engine and Coefficient of Performance of Carnot Refrigerator is always less than one.
- (e) Internal energy change for isothermal expansion of n mol van der Waals gas is always positive.
- 2. A reversible *Carnot Refrigerator* operating between 0 and 25 °C runs for 2 min using 0·5 hp electric motor. Find (a) the coefficient of performance (Ψ) of the refrigerator, (b) the amount of heat (in J) extracted from water, kept inside at 0 °C and (c) the mass of ice produced.

Given:  $1 \text{ hp} = 746 \text{ W & } Enthalpy \text{ of fusion of ice at } 0 ^{\circ}\text{C} \text{ and } 1 \text{ atm is } 80 \text{ cal g}^{-1}.$  1+2+2

- **3.** (a) Mention factor(s) influences and does not influence the *Carnot efficiency*.
  - (b) Calculate  $\Delta G$  when temperature of  $2 \cdot 0$  mol of  $N_2(g)$  increases from 298 to 348 K at constant pressure of 2 bar. Given:  $S_m(J K^{-1} \text{mol}^{-1}) = A + B \ln(T/K)$  for  $N_2(g)$  where  $A = 25 \cdot 1$  and  $B = 29 \cdot 3$  in SI unit and both are independent of temperature.
- **4.** Derive  $\left(\frac{\partial S}{\partial V}\right)_{T,n} = \left(\frac{\partial P}{\partial T}\right)_{V,n}$  and using this relation, show that for isothermal change of '<u>n</u>' mol ideal gas from  $V_1$  to  $V_2$ , the entropy change,  $\Delta S = nR \ln \left(\frac{V_2}{V_1}\right)$ .

(5)

11. For a particle of mass m moving freely in a cubic box of length l, explain the effect of distortion of the box along x-axis on the degeneracy of the level having energy

$$value = \frac{6h^2}{8ml^2}.$$

**12.** Draw sketches showing the planes having Miller indices (011) and (002).

(OR)

The characteristic  $K_{\alpha}$  lines for Cr, Fe and Ni have wavelengths of 2·29 Å, 1·94 Å and 1·66 Å respectively. Which of these may be used to determine a lattice spacing of 0·97 Å?

**13.** Both NaCl and KCl crystallizes in fcc structure; but NaCl is fcc to X-ray, while KCl is simple cubic to X-ray. Clarify.

 $2\frac{1}{2}$ 

14. What is the law of rational indices?

(OR)

What is the highest order (n) that can be observed in Bragg's reflection from a solid by X-ray of wavelength ' $\lambda$ '? 1½

 $\star\star\star$ 

(3)

- 5. Derive Clausius-Clapeyron equation for **liquid** ⇒ **vapor** equilibrium and *Trouton's Rule* from it, mentioning all assumption(s) and approximation(s). 3+2
- **6.** (a) The molar work function  $(A_m)$  of a gas is expressed as:

 $A_m = -\left(\frac{a}{V_m}\right) - RT \ln(V_m - b) + f(T); \text{ where } a \text{ and } b$  are constants. Obtain the expression of pressure of this gas.

(b) Derive :  $\left[\frac{\partial}{\partial T} \left(\frac{G}{T}\right)\right]_{P,n} = -\frac{H}{T^2}$ ; where each symbol bears usual meaning.

## Answer all questions:

- 7. Arrive at the Stefan-Boltzmann law from the Planck's equation of black-body radiation.
- **8.** Examine whether the following are acceptable wave functions or not:
  - (a)  $\cos^{-1} x [-1 \le x \le 1];$
  - (b)  $1/x [0 \le x \le \infty]$

(OR)

When lithium is irradiated with light, the kinetic energy of the ejected electrons is  $2.935 \times 10^{-19}$  J for  $\lambda = 300$  nm and  $1.280 \times 10^{-19}$  J for  $\lambda = 400$  nm. Calculate the Planck's constant.

(4)

9. Evaluate the commutator  $\left[\frac{d^2}{dx^2} - x, \frac{d}{dx} + x^2\right]$ .

(OR)

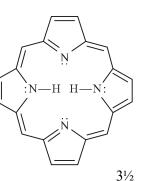
Check whether the set of functions,  $\phi_m = \frac{1}{\sqrt{2\pi}} \exp(im\phi)$  where  $m = 0, \pm 1, \pm 2, ...$  and  $0 \le \phi \le 2\pi$ , will form an orthonormal set or not.

**10.** Consider a particle with quantum number *n*, moving in a one-dimensional box of length *l*. Determine (a) the probability of finding the particle in the left quarter of the box and (b) the value of *n* for which this probability will be maximum.

 $2\frac{1}{2}+1$ 

(OR)

The general structure of a porphyrin molecule is shown on the right side. The molecule is planar and one can approximate that the  $\pi$  electrons are confined inside a square box of perimeter 4000 pm. Calculate the wavelength of radiation absorbed corresponding to the lowest energy absorption of the molecule.



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