

NONLINEAR CONTROL SYSTEM (CON)

Ref. No.: EX/PG/ETCE/T/113C/2024

Time: 3 Hours

Answer Q.1 & any Four from the rest

Full Marks:100

1. Indicate True(T)/ False(F) :

10x2

- i. In State-variable (SV) representation of control system, Choice of state is unique
- ii. A proportional controller improves feedback-system stability
- iii. Controller in a servo-system operates as a gain adjusting element
- iv. Zeigler recommendations are based on root-locus
- v. A third-order closed-loop system is stable if its Phase-Margin (PM) $\gg 180^\circ$
- vi. A limit-cycle phase-Isocline represents a stable system
- vii. Integral controller improves system stability
- viii. A 2nd-Order system is unstable if its S-matrix is nonsingular
- ix. Eigen values of a state-defined system are essentially the poles of system
- x. State-space Re-presentation & choice of states for control system is unique

2. (a) Define Gain-margin (GM) and Phase-margin (PM)

8+12

(b) Sketch the Bode-plot and find GM & PM ; given a transfer function

$$H(s) = 1000 / [(1+0.1s)(1+0.001s)]$$

3. (a) Define State Variable (SV)

8+12

(b) Derive the SV-representation for a system with Transfer Function

$$H(s) = 1 / (s^4 + 3s^3 + 3s^2 + 2s + 1)$$

4. (a) Define the features of PID controller

8+12

(b) A unity feedback system is given by $H(s) = 20 / \{(s+1)(10s+1)(20s+1)\}$

Using a Bode-plot, obtain the parameter settings of a PID controller as per Ziegler

5. (a) What is Describing Function (DF) ?

10+10

(b) A relay with dead-zone element is cascaded to a linear system of transfer function $H(s)$ in closed-loop. Determine the stability conditions of the looped-system using DF. Given $H(s) = 2 / [s(s+2)(s+3)]$.

Assume: $E=1$, $D=2$, $T_m=2$ for nonlinear block.

6. (a) Explain the principles of a Servomechanism

(b) Given transfer function of a servo-system $G(s) = 10A / [s^2 + 35s + 4A]$; If forward gain $A=300$

8+12

Calculate : Damping factor (δ) and Settling time (T_s); Sketch transient response

7. Write Short Notes (Any Two) :

10x2

(a) Controllability / Observability

(b) Phase Variable

(c) Servo-mechanism Characteristics

(d) Lyapunov Stability conditions