

M.E. ELECTRONICS AND TELE-COMMUNICATION ENGINEERING FIRST YEAR
FIRST SEMESTER - 2024

Subject: NEURO-FUZZY AND EVOLUTIONARY COMPUTATION Time: 3 Hours Full Marks: 100

All parts of the same question must be answered at one place only

PART-I

Module-I: Answer ANY TWO (2×20=40)

1. (a) Show that the Einstein product, given by 5

$$ES(\mu_A(x), \mu_B(x)) = \frac{\mu_A(x)\mu_B(x)}{2 - (\mu_A(x) + \mu_B(x) - \mu_A(x)\mu_B(x))},$$

for any two fuzzy sets A and B under a common universe X is a typical T-norm function.

- (b) In public transportation systems there often is a significant need for speed control. For subway systems, for example, the train speed cannot go too far beyond a certain target speed or the trains will have trouble stopping at a desired location in the station. Set up a fuzzy set

$$A = \text{"speed way over target"} = \{0|T_0, 0.6|(T_0+5), 0.9|(T_0+10), 1|(T_0+15)\}$$

on a universe of target speeds, say $T = [T_0, T_0+15]$, where T_0 is a lower bound on speed. Define another fuzzy set

$$B = \text{"apply brakes with high force"} = \{0.3|10, 0.8|20, 0.9|30, 1.0|40\}$$

on a universe of braking pressures, say $S = [10, 40]$.

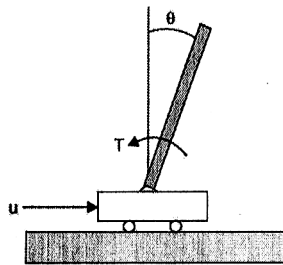
- (i) For the compound proposition, IF speed is "way over target," THEN "apply brakes with high force," find a fuzzy relation using classical implication. 8

- (ii) For a new antecedent, 7

$A' = \text{"speed moderately over target"} = \{0.2|T_0, 0.6|(T_0+5), 1.0|(T_0+10), 0.3|(T_0+15)\}$
find the fuzzy brake pressure using max-min composition.

2. (a) Explain the extension principle of fuzzy sets from n-dimensional product space to a single universe. 5

- (b) The linear differential equation of an inverted pendulum is given next.



$$\frac{1}{3} \frac{4M+m}{4m} \ddot{\theta} - \frac{M+m}{m} g \theta = -\frac{u}{m} \frac{180}{\pi}$$

with $l = \frac{3(M+m)g}{4M+m}$ and $M = \frac{180}{\pi g} - m$

where m is the mass of the pole assumed to be concentrated at the center of the pendulum

M is mass of the cart

$2l$ is the length of the pendulum

θ is the deviation angle from vertical in the clockwise direction

[Turn Over

T is the torque applied to the pole in the counterclockwise direction

U is the control on the cart acting from left to the right producing the counterclockwise torque T

t is time, and

g is the gravitational acceleration constant

- (i) Define membership distributions of the state variables and the control output for $\theta(t) \in [-2 \text{ degree}, 2 \text{ degree}]$, $\dot{\theta}(t) \in [-4 \text{ dps}, 4 \text{ dps}]$ and $u(t) \in [-10, 10]$. 5
 - (ii) Design the production rules for balancing the inverted pendulum in the vertical position. 5
 - (iii) From the designed membership distributions and proposed production rules, determine $u(0)$, $\theta(1)$ and $\dot{\theta}(1)$ for $\theta(0) = 1 \text{ degree}$ and $\dot{\theta}(0) = 0 \text{ dps}$ using Mamdani implication. 5
3. (a) Derive the expressions of the cluster centroids and the memberships of data points in FCM. 10
 - (b) While designing CMOS inverter circuit, it is observed that the W/L ratio of both n-MOS and p-MOS must increase proportionally with an increase in the output load capacitance to maintain the same delay time.
 - (i) Design a suitable production rule to capture the design objective. 1
 - (ii) Find a fuzzy relation for the proposed rule using $\mu_{\text{LARGE}}(\text{capacitance}) = \{0.2|0.5 \text{ pF}, 0.6|2 \text{ pF}, 1|8 \text{ pF}\}$ and $\mu_{\text{HIGH}}(W/L) = \{0.1|4, 0.8|16, 1|64\}$. 4
 - (iii) Find out the fuzzy membership distribution of W/L ratio if the designer is interested with VERY HIGH load capacitance. 5

Module-II: Answer ANY TWO (2×10=20)

4. Illustrate one iteration of particle swarm optimization with a population of 5 particles to optimize the following function with the true optima at (1, 1). 10

$$f(\vec{X}) = (1 - x_1)^2 + 100(x_2 - x_1^2)^2$$
5. (a) How the global best of a swarm and the personal best of a particle help in improving its quality in particle swarm optimization? 4
- (b) Differential evolution employs Darwin principle of the survival of the fittest to improve population over generations. Explain. 3
- (c) What is the significance of the crossover ratio in differential evolution? 3
6. What is multi-objective optimization? 3
 How does the non-dominated sorting helps in multi-criteria decision making? 7
 Explain with an example.

PART-II

Answer any two questions. Each question carries 20 marks.

7. (a) Differentiate among Supervised, Unsupervised and Competitive learnings. 3
- (b) Mathematically discuss the importance of a differentiable function in the context of supervised learning. Give an example of such a function. 3+1

- (c) What is a perceptron? Show how a perceptron can realize an AND function. Does realizing an AND function represent a linearly separable problem? 2+3+1
- (d) State and prove the Perceptron Convergence Theorem. 2+5
8. (a) Distinguish between continuous and discrete Hopfield networks. Encode the four bipolar patterns $X_1 = [1 \ -1]$, $X_2 = [-1 \ 1]$, $X_3 = [-1 \ 1]$ and $X_4 = [-1 \ -1]$ using a discrete Hopfield Network. 2+4
- (b) Mathematically show that - For a discrete Hopfield model having symmetric weights without self-feedback, the dynamics of the network for bipolar output functions using the asynchronous update always leads towards energy minima at equilibrium. 6
- (c) Discuss how Hopfield networks can be used for pattern storage and recall. 3
- (d) Discuss the dynamics of a stochastic network with necessary mathematical details. Explain the objective of a stochastic network in improving the recall in 2(b). 3+2
9. (a) What do you mean by a Winner-Take-All network? Consider a Winner-Take-All network with three nodes A, B, C, and a learning rate of 0.5 for the first two iterations and that of 0.2 for the third iteration. The following three training patterns are shown successively to the above network:
 $i_1 = \{1.1, 1.7, 1.8\}$; $i_2 = \{0, 0, 0\}$; $i_3 = \{0, 0.5, 1.5\}$
 The initial connection strengths of the network with three input nodes and three output nodes are given by:
- $$\begin{bmatrix} w_A & 0.2 & 0.7 & 0.3 \\ w_B & 0.1 & 0.1 & 0.9 \\ w_C & 1 & 1 & 1 \end{bmatrix}$$
- Further assume that the network has a linear topology of the form: B – A – C. Show the updated weight matrix for three iterations.
- (b) Explain the working principle of a Self-Organizing Feature Map (SOFM). State a similarity and a difference between a Winner-Take-All network and a SOFM. 4+2
- (c) Show how a Back-propagation algorithm works using suitable expressions. You can assume a network in this context with the output layer containing appropriate synaptic non-linearity. Justify the name “Back-Propagation”. 5+1