MASTER OF CONSTRUCTION ENGINEERING EXAMINATION, 2024 (1st Semester)

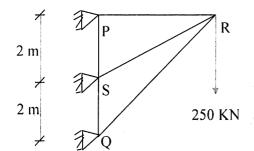
ADVANCED STRUCTURAL ANALYSIS

Answer any **four questions**. All question carry equal marks. Explain your answer, with neat sketches if necessary. Assume any other relevant data not provided.

- a) Deduce the Stiffness Matrix of N numbers of Springs connected in a series by Matrix method of analysis.
 - b) The spring constants are K, 2K, 3K, 4K, 5K, 6K, 7K, 8K, 9K of nine (9) numbers of springs connected in a series, which is subjected to a force of 100 KN.

 Formulate the matrix equation of static equilibrium if K = 10 KN/m.
 - c) Derive Transformation Matrix of Truss Element from Local Coordinate to Global Coordinate system.

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- 2. a) Evaluate the horizontal and vertical components of deflection of the free end R of the bracket truss as shown in Fig.1 by Matrix Method of analysis.



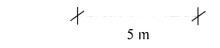
 $E = 2.1 \times 10^5 MPa$ for all Members.

c/s Area of PR = 20.38 cm^2 (**1** ISA 150X115X8)

c/s Area of SR, QR = $2X15.39 \text{ cm}^2$ (2 ISA 100X100X8)

c/s Area of PS, $SQ = 15.39 \text{ cm}^2 (ISA 100X100X8)$

Fig. 1: Truss Problem



- b) Calculate also the Member Forces of PR, SR & QR of the same truss.
- 3. a) Deduce Shape Function for Beam Element in Finite Element Method.
 - b) Derive the **stiffness matrix of Beam Element** in local coordinate system adopting finite element method.

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- 4.a) Deduce the Strain-Displacement and Stress-Strain relationship for a Triangular Element in Plain Stress FEM Problem.
 - b) Derive the Stiffness matrix for the Triangular element in plain stress problem. 10
- 5. a) Deduce the expression of consistent load vector by virtual work method. 10
 - b) Calculate the Slope and Deflection at Point Q of the Fixed Beam from FEM formulation. The depth of beams PQ and QR RS are 300 mm and 500 mm. The width of all these beams are 250 mm. $E = 2.5 \times 10^4 \text{ MPa}$.

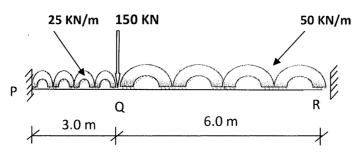


Fig. 2: Fixed Beam

- 6.a) Derive the Shape functions of Truss element and Shape functions for a Rectangular element in plain stress problem and discuss the relationship between these two set of Shape functions.
 - b) Deduce the expression of Slope, Curvature, Bending Moment, Shear Force and Loading intensity from deformations at a regular grid of 'a' in Finite Difference Method (FDM) formulation.