

M. C. E. EXAMINATION, 2024

1st semester

THEORY OF ELASTICITY AND ELASTIC STABILITY

Time 3 hours

Full marks 100

Answer each part in separate answer scripts

Part- I (Full marks = 60)

Answer either Question 1 or 2. Questions 3 and 4 are mandatory.

1. Deduce the generalized tensorial transformation law for vectors. Hence show how does a dyad (say stress or strain) transform? Also, prove that the determinant of a transformation matrix a_{jq} is unity. 6+6+6 = 18
2. It is given that at a certain point in a solid metal cube, the stress-components relative to axes x_i are $\sigma_{11}=80$ MPa, $\sigma_{22}=60$ MPa, $\sigma_{33}=20$ MPa, $\sigma_{12}=20$ MPa, $\sigma_{23}=10$ MPa, and $\sigma_{31}=40$ MPa.
 - (a) Determine the stress vector on a plane normal to the vector $\vec{R} = 3\hat{i} + 3\hat{j} + 3\hat{k}$.
 - (b) Determine the principal stresses and principal direction of the major principal stress. 6+12=18
3. Find the expressions for (a) traction $T_i^{(n)}$ and (b) normal stresses σ_n with respect to stress components σ_{ij} . 8+8 =16
4. Provide a graphical interpretation of the strain terms ϵ_{11} , ϵ_{22} and ϵ_{12} . Derive the stress-strain law of an orthotropic material from that of an anisotropic material. 6+12+8 =26

[Turn over

M.E. CIVIL ENGINEERING FIRST YEAR FIRST SEM. EXAM. -2024**Subject: THEORY OF ELASTICITY AND ELASTIC STABILITY****Time: 3 Hrs****Full Marks 100****PART-II (MARKS-40)**

Use a separate Answer-Script for each part

No. of questions	<u>Answer all questions</u>	Marks 6+18+16=40
1.	What do you mean by stable, unstable and neutral equilibrium. Discuss with neat sketch.	6
2.	Determine the elastic buckling load of a column having one fixed support and other end free. Also determine the buckling load of a column having both end fixed support.	18
3.	Deduce the fourth order equation of plate bending with neat sketch.	16