

1. Consider the following SIMSCAPE figure for a simple spring-mass damper system shown in Fig. 1 below:

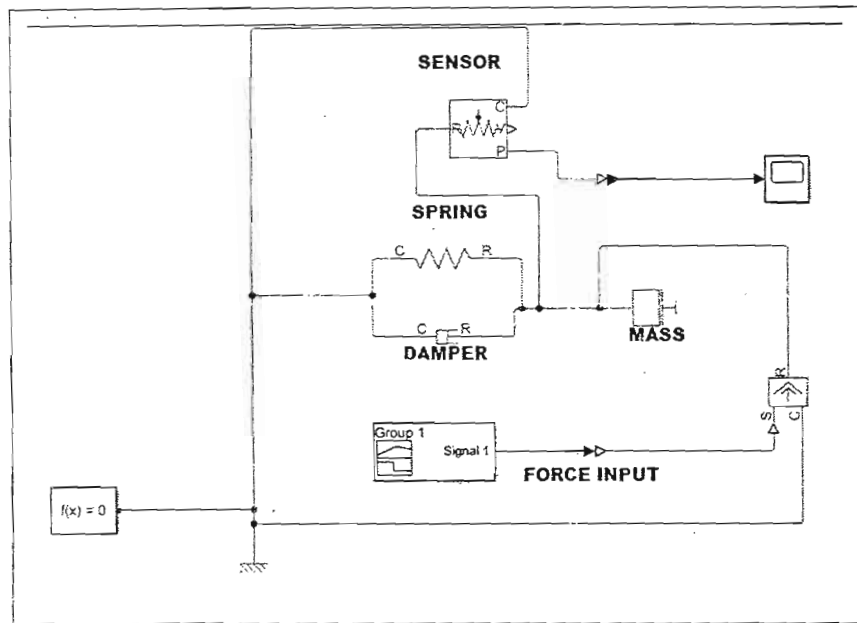


Fig. 1

Assuming that the mass is  $M$ , damping constant is  $D$ , the spring constant is  $K$  and the force input is  $F(t) = \delta(t)$  (all in SI units), deduce the following from Fig.1

- (i) The initial displacement and velocity of the mass
  - (ii) The A and B matrices for a state-variable representation of the physical model.
  - (iii) The C matrix (hint: look at the sensor node)
  - (iv) The steady state displacement and velocity of the mass for the applied force
- CO1(10)+ CO2(10)
2. Reduce the block diagram shown in Fig. 2 to obtain the transfer function between the input and the output

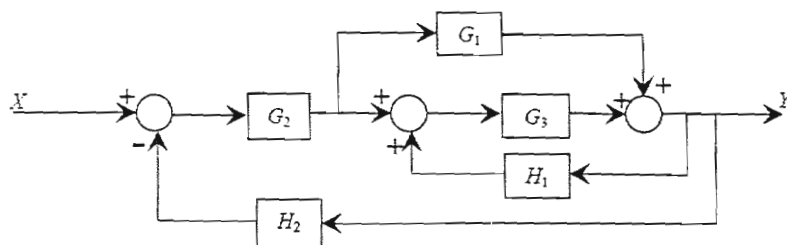


Fig. 2 (Refer Q2.)

Check the result using a Signal Flow Graph and Mason's Gain formula CO1 (10)+ CO2(10)

3. Deduce the Laplace Transform of a Pulse-Train of Time period 5 seconds , Duty Cycle 0.4 and height 2V.

Deduce and sketch the approximate waveform you would see in a simulation if this waveform is applied to a system with Transfer Function  $G(s) = \frac{0.5e^{-0.1s}}{s+1}$ .

CO1 (10)+ CO2(10)

**Group B (Answer Any Two)**

4. Represent the Pole-Zero map of the system  $G(s) = \frac{4(s-0.5)}{s^2+2.4s+4}$  in the complex plain. Calculate the corresponding damping, natural frequency of the system. How does the output change because of the addition of a RH zero at  $s = 0.5$  to the basic second order system i.e.  $G(s) = \frac{4}{s^2+2.4s+4}$ ?

If the system is controlled by a controller K , with a unity feedback, calculate the maximum value of K for which the closed loop system is stable using RH Criterion?

CO3(4+6) + CO4(10)

5. Use Nyquist criterion to estimate the stability of a unity feedback closed loop system corresponding to the open-loop system defined by  $G(s) = \frac{10(s-2)}{(s+1)(s+1)(s+3)}$  and interpret the stability of the closed loop system. Hand-sketch the corresponding Nyquist Plot

CO3(10) + CO4(10)

6. Draw the asymptotic Bode plot for the system in Problem 5. Identify the corner frequency, the asymptotes and sketch a rough Bode Plot. Calculate the Gain Margin and Phase Margin Using the Bode Plot, calculate how much delay the system can tolerate.

CO3(10)+CO4(5)+CO4(5)

**Group C**

7. A valve in a Thermal Power Plant has a transfer function  $G_v(s) = \frac{2}{0.5s+1}$  and it is controlled by a controller with transfer function  $H(s) = (1 + \frac{0.2}{s})$  in the forward path.

- (i) Represent the system with a schematic for unity feedback
- (ii) Draw the PZ map for  $G_v(s)H(s)$
- (iii) Using Root-Locus, calculate a value of K (if any), for which the system is unstable.

CO5(4+4+12)