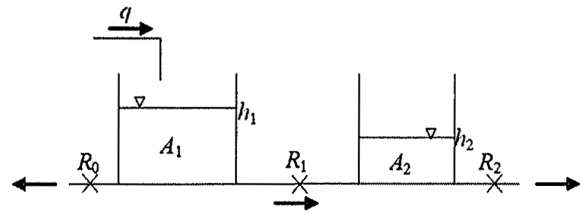


**B.E. MECHANICAL ENGINEERING FOURTH YEAR SECOND SEMESTER - 2024**Subject: **INTRODUCTION TO MODERN CONTROL THEORY(HONS.)****Time: Three hours****Full Marks: 100**Answer any **FIVE** questions. Different parts of the same question should be answered together.

Assume any relevant data if necessary.

[1] For the process, shown in Fig.P1, consisting of 2 interconnected tanks –  $R_0$ ,  $R_1$  and  $R_2$  are the linearized pipe resistances,  $h_1$  and  $h_2$  are the water levels in the 2 tanks and  $A_1$  and  $A_2$  are the tank cross-sectional areas. The input to the system is the flow rate  $q$  into tank 1 and output of the system is the height of water in tank 2 i.e.  $h_2$ . For  $A_1 = 1$ ,  $A_2 = 0.5$ ,  $R_0 = 0.25$ ,  $R_1 = 0.5$ ,  $R_2 = 2$ , [20]

- Write down the governing differential equations.
- Construct the block diagram.
- Obtain the state space model, clearly specifying **A**, **B** and **C**.
- Check the stability of the system.
- Obtain the transfer function matrix.
- Obtain the system response for  $q = 1$ .

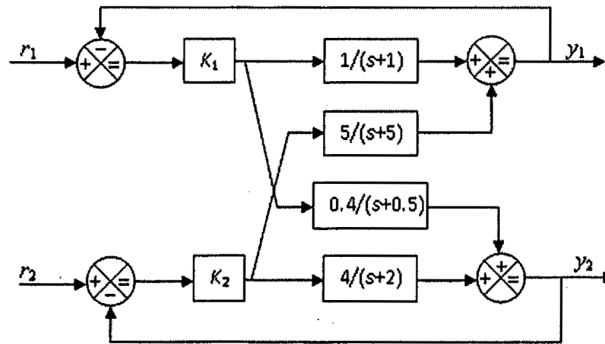
**Fig.P1**

[2] (a) For a state-space system given by  $\dot{\mathbf{X}} = \begin{bmatrix} -6 & 2 \\ 4 & -5 \end{bmatrix} \mathbf{X} + \begin{bmatrix} 1 \\ 0 \end{bmatrix} \mathbf{U}$ ;  $\mathbf{Y} = \begin{bmatrix} 0 & 1 \end{bmatrix} \mathbf{X}$ , design the state feedback controller and observer so that the controller eigenvalues are placed at  $-4$  and  $-9$  whereas the observer eigenvalues are placed at  $-12$  and  $-15$ .

(b) What is meant by *observability* and *stabilizability*?

[14+6=20]

[3] A control system with 2 inputs  $r_1$  and  $r_2$  and 2 outputs  $y_1$  and  $y_2$  is shown in Fig.P3 below. Construct a state space model for the system. [20]

**Fig.P3**

[4] (a) Model a 4-way 3-position proportional valve with a 3-layer feed forward neural network. The inputs are the valve pressure drop and the command voltage while the output is the valve flow rate. Sketch the network with a single hidden layer comprising of 3 hidden neurons having tan sigmoid activation functions. The output layer has linear activation functions. Obtain the learning equations for  $w_{23}$  (weight between 2<sup>nd</sup> input and 3<sup>rd</sup> hidden neuron) and  $v_{11}$  (weight between 1<sup>st</sup> hidden and output neuron) using the backpropagation training algorithm for a given set of 100 training data.

(b) What is the role of *momentum factor* in the learning process?

[15+5=20]

[5] (a) For an under-damped second order system, obtain the phase-plane equation and the isocline equation. Sketch the isoclines.

(b) Explain the terms globally asymptotically stable, locally asymptotically stable, and stable for a dynamic system with  $\mathbf{X}$  as the state vector

(c) State *Lyapunov's* Stability Theorem.

(d) A spring-mass-damper system for which the damping force is proportional to the third power of the velocity is described by the differential equation

$$\ddot{y} + 0.5\dot{y}^3 + y = 0$$

Comment on the stability of the system.

[8+3+3+6=20]

[ Turn over

[6] (a) Consider:  $\dot{x}_1 = 2x_2$   
 $\dot{x}_2 = -4x_1 - 9x_2 + 5u$

If the system lumped uncertainty can be expressed as  $|e(\mathbf{X}, \mathbf{U}, \mathbf{V}, t)| \leq 3$  and a sliding surface is defined as,  $\sigma = 4x_1 + x_2$ , then obtain the sliding mode control  $u$  in terms of  $x_1$  and  $x_2$ .

(b) Consider a state model  $\dot{\mathbf{X}} = \mathbf{A}\mathbf{X} + \mathbf{B}\mathbf{U} + \Delta\mathbf{A}\mathbf{X} + \Delta\mathbf{B}\mathbf{U} + \mathbf{G}\mathbf{V}$  where  $\Delta\mathbf{A}$  and  $\Delta\mathbf{B}$  are the uncertainties associated with the state matrix  $\mathbf{A}$  and the input matrix  $\mathbf{B}$ ;  $\mathbf{V}$  are the external disturbances. With suitable assumptions, identify the *lumped uncertainty*  $e(\mathbf{X}, \mathbf{U}, \mathbf{V}, t)$ . [14+6=20]

[7] (a) A dynamic system can be modelled as a spring-mass-dashpot system with force as input and displacement as output. What can be 2 possible inputs and the output of a fuzzy logic controller for this dynamic system? Design the membership functions for these input-output(s) assuming suitable ranges. State some realistic rules for the controller. The force ranges between  $\pm 1000\text{N}$ , the displacement ranges between  $\pm 0.1\text{m}$  and the rate of force ranges between  $\pm 20\text{N/s}$ . Show the membership functions in a graph paper corresponding to the rules.

(b) What is the advantage of fuzzy controllers over crisp controllers. [16+4=20]

[8] Write short notes on any FOUR (4) of the following:

- (i) Companion form of the state matrix;
- (ii) Sliding mode and reaching mode;
- (iii) Feedforward neural network;
- (iv) Features in system responses indicating presence of nonlinearity;
- (v) Linearization techniques.

[4×5=20]