

B.E.Tel.E. 2nd YEAR SUPPLEMENTARY EXAMINATION, 2024
(1st Semester)

ELECTRO MAGNETIC THEORY

Time: Three hours

Full Marks 100

No. of
questions

Marks

Answer any *five* questions.

Consider $\epsilon_0=8.854 \times 10^{-12} \text{F/m}$ and $\mu_0=4\pi \times 10^{-7} \text{H/m}$

Values of other universal physical constants may be assumed, if necessary.

All symbols carry their usual meanings.

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|-------|--|--------|
| 1.(a) | Prove that $\nabla \times (a\vec{B}) = \nabla a \times \vec{B} + a\nabla \times \vec{B}$ | 10 |
| (b) | Convert $3\hat{x} + 4\hat{y} + 5\hat{z}$ to spherical co-ordinates. | 10 |
| 2.(a) | Define electrostatic potential and equipotential surfaces. What is the nature of equipotential surfaces due to a point charge? | 6 |
| (b) | What is the difference between conservative and dissipative fields? Site one example of each. | 4 |
| (c) | Derive the fields due to an infinitesimal static electric dipole. | 10 |
| 3.(a) | State and prove Gauss' Law of electrostatics. | 8 |
| (b) | Derive an appropriate expression for density of stored energy in electric field. | 12 |
| 4.(a) | Define an irrotational field. Is a magnetic field rotational or irrotational? | 4 |
| (b) | Justify why a magnetic potential is vector rather than a scalar. | 2 |
| (c) | Consider $\phi=\pi/4$ plane defined in cylindrical coordinates. Find the amount of magnetic flux crossing the portion between $0.01 < \rho < 0.05 \text{m}$ and $0 < z < 2 \text{m}$ due to a current filament of 2.5A along the z-axis in +z direction. | 14 |
| 5.(a) | For a time harmonic field propagating through a good dielectric, determine the attenuation constant and phase velocity. | 8 |
| (b) | Repeat the same for a good conductor. | 8 |
| (c) | How do you demarcate between a good dielectric and a good conductor? | 4 |
| 6.(a) | What are parallel and perpendicular polarizations? | 4 |
| (b) | For both of them, find an appropriate expression for the reflection coefficient at a dielectric-dielectric interface. | 8+8 |
| 7.(a) | Prove Snell's law for electromagnetic fields. | 8 |
| (b) | A current sheet $K = 9\hat{y} \text{ a/m}$ is located at $z=0$. Region 1 at $z<0$ has $\mu_{r1}=4$ and region 2 at $z>0$ has $\mu_{r2}=3$. Given that $H_2=14.5\hat{x}+8\hat{z} \text{ A/m}$, find H_1 . | 12 |
| 8. | Write notes on any <i>two</i> of the followings. | |
| (a) | Total internal reflection | |
| (b) | Inductance and capacitance | |
| (c) | Method of images and fundamental problem of electrostatics | 10 X 2 |