

B.E.ELECTRICAL ENGINEERING SECOND YEAR FIRST SEMESTER
EXAMINATION, 2024

SIGNALS AND SYSTEMS

Full Marks 100

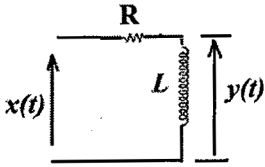
Time: Three hours

(50 marks for each part)

Use a separate Answer-Script for each part

Question No.	PART I	Marks
	<p align="center">Answer Question No. 5 and any TWO from rest. <u>Give proper units wherever necessary.</u></p>	
1. (a)	<p>Evaluate the following integrals.</p> <p>(i) $\int_{-\infty}^{+\infty} \delta(bt-a) \cos^2(t-c) dt$, from the definition of $\delta(t)$, where $b > 0$.</p> <p>(ii) $\int_{-\infty}^{+\infty} \frac{1}{3} \text{Sinc}^2(3t) dt$</p>	7
(b)	<p>The impulse response of a linear time-invariant (LTI) system is</p> <p>$h(t) = e^{-t} [u(t-3) - u(t-5)]$. <i>Without actually determining the expression for the frequency response, obtain the value of the DC gain of the system.</i></p>	5
(c)	<p>Determine the ‘Duty Cycle’ and ‘AC Coupled Crest factor’ of the pulse train $x(t)$ depicted in Fig.[A].</p> <div style="text-align: center;"> <p>Fig. [A] [CO2-K2]</p> </div>	4
2. (a)	<p>The response of an LTI system to a unit parabola input is</p> <p>$\phi(t) = \frac{3}{2} t^2 u(t) - e^{-2t} u(t)$.</p> <p>Perform time-domain analysis to obtain the expression for the</p>	7

Question No.	PART I	Marks
	<p>response of the system to an input $f(t) = \text{tri}(t-1)$, where $\text{tri}(t)$ is shown in Fig. [B].</p> <div data-bbox="587 517 949 786" data-label="Figure"> </div> <p style="text-align: center;">Fig. [B]</p> <p>(b) The input $x(t)$ to an LTI system has an autocorrelation function $R_x(\tau) = 2\delta(\tau)$. The impulse response function of the system is $g(t) = 3e^{-5t}u(t)$. Determine the expression for the autocorrelation function of the output.</p> <p>(c) Determine the energy of the signal</p> $x(t) = \sin(\omega_o t) \text{ for } -\frac{2\pi}{\omega_o} \leq t \leq \frac{2\pi}{\omega_o}$ <p>and $x(t) = 0$ otherwise, where t is in seconds and $x(t)$ is in A.</p> <p style="text-align: right;">[CO3-K3]</p> <p>3. (a) With the help of neat labeled sketches, determine and sketch the odd component of the signal $y(t)$ shown in Fig. [C]. Also sketch the derivative of $y(t)$.</p> <div data-bbox="646 1512 944 1769" data-label="Figure"> </div> <p style="text-align: center;">Fig. [C]</p> <p>(b) Obtain the one-sided line amplitude spectrum, phase spectrum and the power density spectrum (up to 3rd harmonic) for the periodic signal $x(t)$ shown in Fig. [A]. Is the integral of $x(t)$ periodic? Explain.</p> <p style="text-align: right;">[CO4-K2]</p>	<p>5</p> <p>4</p> <p>7</p> <p>7+2</p>

Question No.	PART I	Marks
4.	<p>In the circuit shown in Fig. [D], if $R=10\ \Omega$ and $L=1\ \text{H}$, determine the expression for the steady state output $y(t)$ and for an input $x(t) = 2\cos(2t) + 3\cos(4t)$, where t is in seconds. Also determine the expressions for the step response of the circuit and the response corresponding to an input $x(t) = e^{-3t}u(t)$. [CO5-K3]</p>  <p style="text-align: center;">Fig. [D]</p>	6+4+6
5.	<p>Write short notes on <i>any two</i> of the following. [CO1-K1]</p> <p>(a) Frequency response of second-order system.</p> <p>(b) Energy spectral density and power spectral density.</p> <p>(c) Periodicity of linear combination of periodic signals.</p>	9+9
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B. E. ELECTRICAL ENGINEERING 2ND YEAR 1ST SEMESTER EXAMINATION, 2024**Subject: SIGNALS & SYSTEMS****Time: Three Hours****Full Marks: 100****Part II (50 marks)**

Question No.	Question 1 is compulsory Answer <i>Any Two</i> questions from the rest (2×20)	Marks
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Q1 Answer *any Two* of the following:

- (a) Determine if the system given by

$$\frac{dy(t)}{dt} + \sin(t)y(t) = 4x(t) \quad 5$$

is time-invariant, linear, causal, and/or memoryless?

- (b) An LTI system has an impulse response
- $h(t) = e^{-at}u(t)$
- . When it is excited by an input signal
- $x(t)$
- its output is
- $y(t) = [e^{-bt} - e^{-ct}]u(t)$
- . Determine
- $x(t)$
- .
- 5

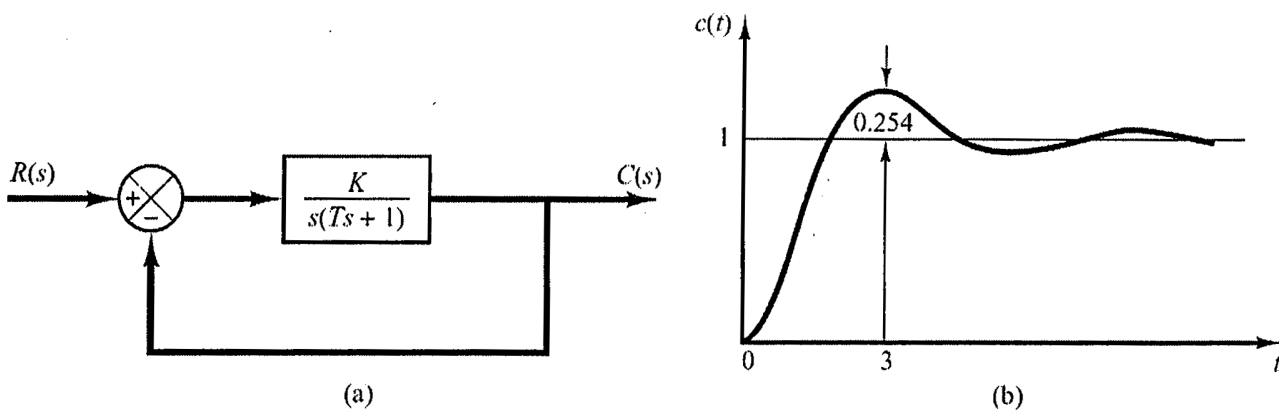
- (c) Find state equations for the following system

$$\frac{d^2y(t)}{dt^2} + 2\frac{dy(t)}{dt} + 4y(t) = 2u(t) \quad 5$$

where, $y(t)$ and $u(t)$ are output and input, respectively.

- (d) Find an analog simulation that converts feet into inches utilizing the full amplifier range of 0 to +10 volts and is capable of converting up to 5feet.
- 5

- Q2 (a) When the system shown in Figure Q2(a) is subjected to a unit-step input, the system output responds as shown in Figure Q2(b). Determine the values of K and T from the response curve. 6

**Figure Q2**

- (b) Define State and Output equations for an LTI system. 2+2
For n -th order SISO, LTI system indicate the dimensions of the matrices and vectors involved in State and Output equations. 4

- (c) Consider an LTI system given by the differential equation:

$$2\frac{d^3y(t)}{dt^3} + 4\frac{d^2y(t)}{dt^2} + 6\frac{dy(t)}{dt} + 8y(t) = 10u(t) \quad 6$$

Obtain the state-space model of the system in the phase variable canonical form.

- Q3 (a) (i) Define damping ratio (ξ) and undamped natural frequency (ω_n) for a second order system? 2+2
- (ii) Show that the locus of the poles of a 2nd order system for ξ varying from 0 to 1, with ω_n held constant, will be a circle of radius ω_n with its center at origin. 4
- (b) Obtain the transfer function of the circuit, shown in Figure Q3(b), in terms of R_1 , R_2 , C , and L .
Determine the poles of the circuit for $R_1=R_2=2000\ \Omega$, $C = 100\text{mF}$, $L = 10\text{mH}$.

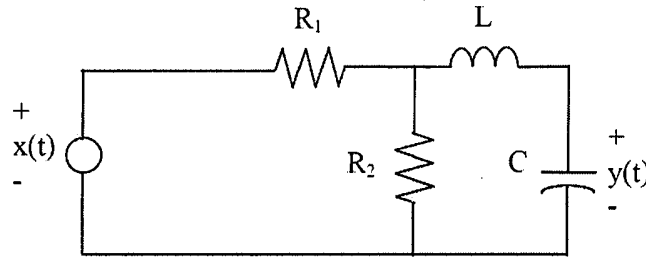


Figure Q3(b)

8+4

- Q4 (a) (i) State and prove the Final Value Theorem for Laplace Transform. 4
- (ii) Find the initial value of $\frac{df(t)}{dt}$ for $F(s) = \mathcal{L}[f(t)] = \frac{2s+1}{s^2+s+1}$ 4
- (b) Use one-sided Laplace Transform to find the output $y(t)$ of a system given by

$$\frac{dy(t)}{dt} + 4y(t) = 3x(t)$$
6
 with, $x(t) = \sin(2t)$, and $y(0^+) = 1$
- (c) Simplify the block diagram shown in Figure Q4(c) to find the transfer function.

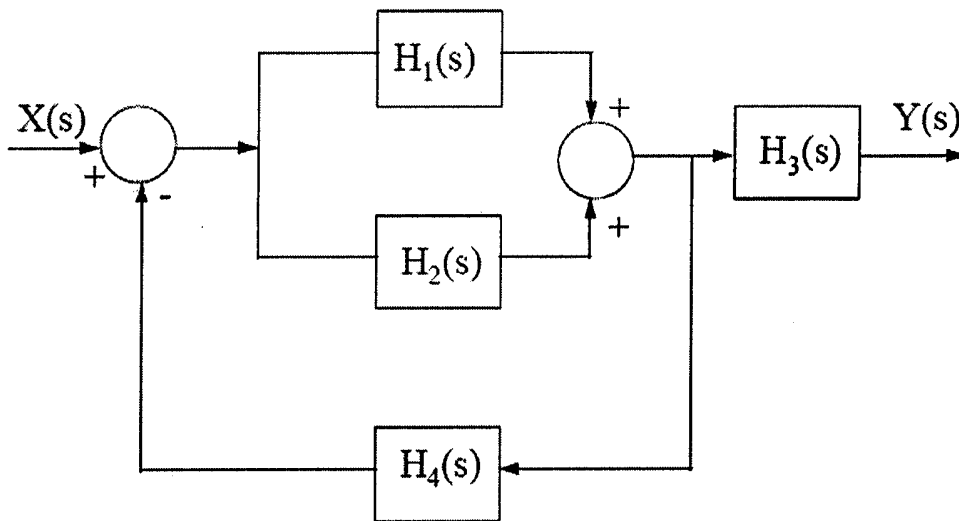


Figure Q4(c)

6

[Turn over

Q5 (a) (i) Draw analog simulation diagram for the following system.

$$\ddot{x} + 8\dot{x} + 25x = 500, \quad x(0) = 40, \dot{x}(0) = 150,$$

$$\text{with, } |x|_{\max} = 50, |\dot{x}|_{\max} = 250.$$

4+8

(ii) Obtain magnitude-scaled analog simulation of the system to utilize the full amplifier range of 0 to +10 volts without any overloading.

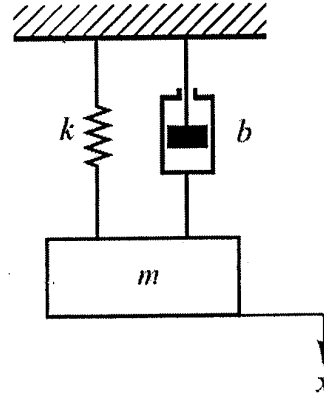
(b) (i) In the system shown in Figure Q5(b), the numerical values of m , b , and k are given as

$$m=1 \text{ kg, } b=2 \text{ N-sec/m, and } k=100 \text{ N/m.}$$

The mass is displaced 0.05 m and released without initial velocity.

Find the frequency observed in the vibration.

(ii) Obtain the analogous electrical network based on *force-voltage* analogy.



4+4

Figure Q5(b)