

***Diesel engine waste heat recovery using a CO<sub>2</sub>-  
Propane mixture based trans-critical power  
cycle: Optimization using Energy, Exergy and  
Economic Analyses***

A thesis submitted in partial fulfillment of the requirements for  
the degree of Master in Mechanical Engineering

By

**Akash Saha**

**Roll No: 002011202002**

**Examination Roll No: M4MEC22002**

**Registration No: 131758 of 2015-16**

Under the supervision of

Prof. Sudipta De

**Mechanical Engineering Department**

**Jadavpur University**

# Faculty of Engineering & Technology

Jadavpur University

Kolkata-700 032

I hereby recommend that the thesis, entitled as — **"Diesel engine waste heat recovery using a CO<sub>2</sub>-Propane mixture based trans-critical power cycle: Optimization using Energy, Exergy and Economic Analyses"**, prepared by Mr. Akash Saha (Registration No-131758 of 2015-2016) under my guidance, be accepted in partial fulfillment of the requirement for the degree of Master of Engineering (Mechanical Engineering – Heat Power) from the Department of Mechanical Engineering of Jadavpur University.

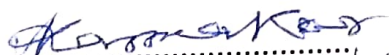


Adviser, 16/6/2022

Prof. Sudipta De,  
Department of Mechanical Engineering  
Jadavpur University.

Professor

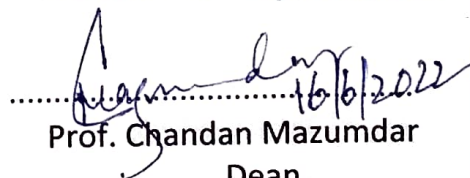
Countersigned by: Dept. of Mechanical Engineering  
Jadavpur University, Kolkata-32



Prof. Amit Karmakar 16/6/2022

Head,  
Department of Mechanical Engineering  
Jadavpur University

Professor & Head  
Dept. of Mechanical Engineering  
Jadavpur University, Kolkata-32



Prof. Chandan Mazumdar

Dean,

FET

Jadavpur University



DEAN

Faculty of Engineering & Technology  
JADAVPUR UNIVERSITY  
KOLKATA-700 032

## *Faculty of Engineering & Technology*

*Jadavpur University*

*Kolkata-700 032*

---

### *Certificate of Approval*

*The foregoing thesis, entitled as “Diesel engine waste heat recovery using a CO<sub>2</sub>-Propane mixture based trans-critical power cycle: Optimization using Energy, Exergy and Economic Analyses” is hereby approved by the committee of final examination for evaluation of thesis as a creditable study of an engineering subject carried out and presented by Mr. Akash Saha (Registration No-131758 of 2015-2016) in a manner satisfactory to warrant its acceptance as a prerequisite to the degree of Master of Engineering (Mechanical Engineering – Heat Power). It is understood that by this approval, the undersigned do not necessarily endorse or approve any statement made, opinion expressed or conclusion drawn therein, but approve the thesis only for the purpose for which it is submitted.*

*Committee of final examination for evaluation of thesis:*

---

*Dr. Sudipta De, Professor and Supervisor,  
Mechanical Engg Department, Jadavpur  
University.*

---

*External Examiner,*



## **Acknowledgement**

I am extremely grateful to my guide Prof. Sudipta De and my collaborator for this project Prof. Subho Mondal, for their help and guidance to complete my Master's thesis. Prof. Subho Mondal has helped me formulate the problem statement, while I took the computational responsibility to run Python code to solve cycles, parametrically optimize the design and cost of the cycle and heat exchangers involved. Prof. Sudipta De helped us coordinate the work and provided valuable insights from his rich academic experience to complete the work in a time-bound manner. I am deeply indebted to the Mechanical Engineering faculty of Jadavpur University, who taught me several important concepts related to Heat Transfer (Prof. Balaram Kundu, Prof. Koushik Ghosh), Heat Exchangers (Prof. Dipten Misra), Computational Heat Transfer (Prof. Achintya Mukhopadhyay, Prof. Himadri Chattopadhyay) and Energy Conservation and Waste Heat Recovery (Prof. Sudipta De), in order to sharpen my research capabilities and complete my Master's project.

**Akash Saha**

Akash Saha  
16/6/2022

## **Contents**

<b><u>Sl. No.</u></b>	<b><u>Subject</u></b>	<b><u>Page No.</u></b>
1.	<i>Abstract</i>	6-6
2.	<i>Nomenclature</i>	7-9
3.	<i>Introduction</i>	10-12
4.	<i>Selection of working fluid</i>	13-15
5.	<i>System description</i>	16-16
6.	<i>Modeling and methodology</i>	17-23
7.	<i>Results and discussions</i>	24-32
8.	<i>Conclusions</i>	33-34
9.	<i>References</i>	35-38

## **1. Abstract**

Though CO<sub>2</sub> power cycles are preferred for diesel engine waste-heat recovery, cost of equipments and complexity of equipments for a CO<sub>2</sub> power cycle is an issue of concern. For mitigating this issue, in my ME thesis work, CO<sub>2</sub>/ Propane mixtures with various CO<sub>2</sub> mass fraction ratios are used as working fluid for a regenerative trans-critical power cycle diesel power plant waste heat recovery. We have also used an optimization algorithm to ensure the best performance – both power and cost wise. To avoid accidental flame propagation, the minimum permissible CO<sub>2</sub> mass fraction is restricted to 0.3. At a lower turbine inlet pressure, we can have a higher output power by reducing CO<sub>2</sub> mass fraction, and lesser levelized electricity cost (LEC). By using the presented waste heat recovery scheme, we can also enhance the output power of the diesel power plant by 8%. The LEC of the presented optimized cycle is about 6.36% lower compared to that of the optimized supercritical CO<sub>2</sub> power cycle recovering the same waste heat. Turbine inlet pressure corresponding to the minimum LEC of the optimized mixture-based cycle is close to 33% lower than that of the optimized supercritical CO<sub>2</sub> power cycle. Finally, while recovering diesel power plant waste-heat, the optimized mixture-based cycle can ensure a safe, environment friendly and economically feasible operation at a significantly lower operating pressure.

### **Key words:**

Diesel power plant waste heat; CO<sub>2</sub>/Propane mixture; Transcritical power cycle; Output power; Levelized electricity cost.

## 2. Nomenclature

<i>Symbol</i>	
$\dot{m}$	Mass flow rate (kg/s)
$C_p$	Specific heat capacity (kJ/kgK)
$t$	Temperature (°C)
$T$	Temperature (K)
$h$	Specific enthalpy (kJ/kg)
$s$	Specific entropy (kJ / kg K)
$u$	Fluid velocity (m /s)
$\dot{W}$	Power (kW)
$\dot{E}_{in}, \dot{E}_D, \dot{E}_L$	Exergy inflow, destruction and loss (kW)
$LMTD$	Log mean temperature difference (K)
$q$	Heat transfer at each HX section (kW)
$N$	Number of HX sections
$Q$	Heat transfer (kW)
$A$	Area of heat exchange (m <sup>2</sup> )
$F$	Correction factor of HX
$U$	Overall heat transfer coefficient (W/m <sup>2</sup> K)
$\alpha$	Heat transfer coefficient (W/m <sup>2</sup> K)
$Re$	Reynolds number
$Pr$	Prandtl number
$Nu$	Nusselt number
$C_p^0$	Purchase cost
$K_1, K_2, K_3$	Purchase cost coefficients
$B_1, B_2$	Bare module coefficients
$F_m, F_p, F_{BM}$	Material, Pressure, Bare module factors
$CRF$	Capital Recovery Factor

$C_{OM}$	Cost of Operations and Management (\$)
$AOH$	Annualized Operating Hours (h)
$LEC$	Levelized Energy Cost (\$/kWh)
$i$	Interest rate
$LT$	Lifetime (years)
$P$	Pressure (MPa)
$S_T, S_L$	Transverse and longitudinal pitch (m)
$mf$	Mass fraction
<b>Greek symbol</b>	
$\eta$	Efficiency (Dimensionless)
<b>Subscript</b>	
$CO_2$	Carbon dioxide
$cond$	Condenser
$WF$	Working fluid
$gi, g, fg$	Flue gas inlet or flue gas
$J_{cw}$	Jacket coolant water
$cw$	Coolant water
$w$	Water
$in$	Inlet
$coolant$	coolant
$i$	Section number i
$si$	Shell side at section i
$ti$	Tube side at section i
$II$	2 <sup>nd</sup> law
$I$	1 <sup>st</sup> law
$1-1e$	Flue gas states
$2-2c$	Jacket coolant water states



3-7,7c,8	Working fluid cycle states
0	Ambient state
<b>Abbreviation</b>	
FGHRU	Flue gas heat recovery unit
ORC	Organic Rankine Cycle
HRU	Heat recovery unit
ODP	Ozone depletion potential
GWP	Global Warming Potential
LMTD	Log Mean Temperature Difference
CEPCI	Chemical Engineering Plant Cost Index
CWHRU	Coolant water heat recovery unit
LEC	Levelized Energy Cost
CRF	Capital Recovery Factor
AOH	Annual Operating Hours
TIP	Turbine inlet pressure
TIT	Turbine inlet temperature

### **3. Introduction**

A huge amount, around  $2/3^{\text{rd}}$  of heat input to a diesel engine in the form of calorific value of fuel is usually rejected to the immediate surroundings as the waste heat. Hence, systematic waste heat recovery can enhance the energy utilization efficiency of a diesel engine. Turbocompounding, CO<sub>2</sub> based power cycle, organic Rankine cycle (ORC) are some commonly employed methods for diesel engine waste heat recovery [1].

Turbocompounding is preferred for a moving vehicle operating at a higher load over a substantially higher time period. The yielded efficiency of a marine diesel engine with turbocompounding is above 50% [2]. However, turbocompounding produces a back pressure due to which the exhaust stroke encounters significant adverse pressure gradient, hampering the process therein [3].

Recently, ORC has been proposed by many researchers. Yu et al. [4] proposed to use R245fa as the working fluid of an ORC cycle driven by the waste heat of a diesel engine coupled with a generator. Shu et al. [5] reported that an ORC driven by diesel engine waste heat using Cyclohexane as the working fluid can reduce brake specific fuel consumption by 10%. Yang et al. [6] proposed an ORC layout which recovers waste heat simultaneously from the exhaust gas, jacket cooling water, scavenging air cooling water and lubricating oil of a large marine diesel engine. Boodaghi et al. [7] reported that a dual loop ORC delivers 310 kW power at an engine speed of 1800 RPM when it is coupled with a heavy-duty diesel engine. R134a and R245fa had been working fluids for the low temperature and high temperature loops respectively. Lion et al. [8] revealed that the annual fuel cost of the marine diesel engine with a waste heat recovery

system using ORC was around 5% lower when compared to that of the marine diesel engine without using waste heat recovery.

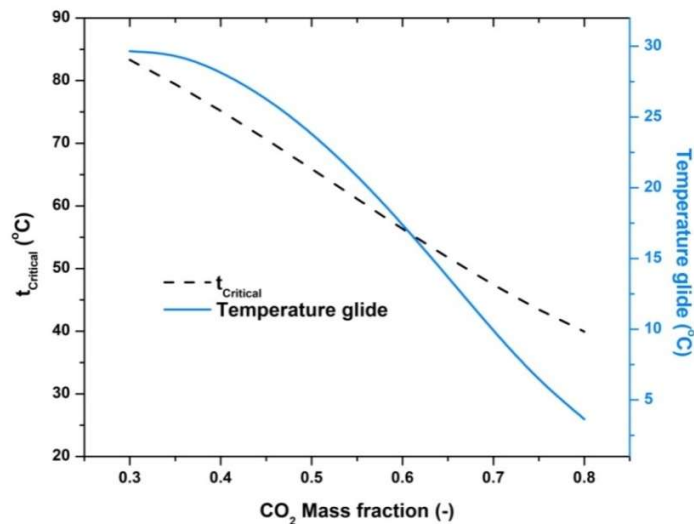
Recently, CO<sub>2</sub> has been considered as the working fluid in many waste heat recovery schemes for power cycles as it is environment friendly and non-flammable [9-11]. CO<sub>2</sub> is also preferred for engine waste heat recovery as it is stable at higher temperature and the design of CO<sub>2</sub> turbomachinery is very compact [12]. Song et al. [13] proposed a supercritical CO<sub>2</sub> power cycle driven by diesel engine waste heat with two pre-heaters. By incorporating the 2<sup>nd</sup> pre-heater output power was enhanced by 6.7%. Pan et al. [14] showed that recompression CO<sub>2</sub> power cycle, driven by diesel engine waste heat, with dual turbine would substantially reduce auxiliary fuel consumption. Mondal et al. [15] maximized the heat recovery from a marine diesel engine using a CO<sub>2</sub> organic cascade cycle. Sakalis [16] showed that the efficiency improvement of a standalone marine diesel engine would be 6.6% to 7.25%, due to waste heat recovery through supercritical CO<sub>2</sub> power cycles. Zhang et al. [17] revealed that the maximum thermal efficiency that could be achieved by an optimized recompression CO<sub>2</sub> power cycle driven by engine waste heat would be about 35.86%.

The drawback of CO<sub>2</sub> power cycles is very high turbine inlet pressure, in spite of studies conducted to show its efficacy. A mixture of CO<sub>2</sub> and organic fluid as the working fluid of power cycles had been recommended by many researchers, to reduce this limitation [18]. Liu et al. [19] showed experimentally that a power cycle with (0.6/0.4) CO<sub>2</sub>/ R134a mixture exhibited better performance in engine waste heat recovery compared to the pure CO<sub>2</sub> power cycle. Shu et al. [20] reported that the optimum operating pressure of a power cycle driven by engine waste heat could be decreased by 1.4 MPa, using (0.3/0.7) CO<sub>2</sub>/R32 mixture as the working fluid compared to that of the pure CO<sub>2</sub> power cycle.

It appears that waste heat recovery from engines is an emerging subject in the field of energy study. In the present study, a regenerative trans-critical power cycle with CO<sub>2</sub>/ Propane mixture as the working fluid is employed for a stationary diesel power plant waste heat recovery. Quality and quantity of exhaust gas waste heat differs substantially from that of the engine coolant waste heat. The fraction of waste heat from the two sources can be optimized under temperature and compositional constraints to deliver the maximum output power. Thus, we find out the turbine inlet temperature using an optimization algorithm corresponding to this operating condition. The optimization algorithm also helps to determine the operating condition to minimize the levelized cost of electricity. The use of CO<sub>2</sub>/ propane mixture ensures operation in an environment-friendly manner and also provides a safeguard for the flame propagation by accident.

#### 4. Selection of working fluid

Selection of a suitable working fluid is a critical factor in design of a waste heat recovery system. Good thermodynamic performance with a minimal adverse environmental impact is an important selection criterion for a suitable working fluid. Flammability and commercial availability are also factors which determine the selection of a working fluid. As already discussed, many researchers propose CO<sub>2</sub> as a working fluid for waste heat recovery from engine as it is commercially available and stable at a higher temperature. CO<sub>2</sub> is non-flammable, has zero ozone depletion potential (ODP). Global warming potential of CO<sub>2</sub> is 1. Temperature profile of supercritical CO<sub>2</sub> streams has been observed to match well with that of many heat carrying streams. In spite of so many advantages, a very high operating pressure of the CO<sub>2</sub> power cycle is an issue in proper equipment design [21]. Thus, we have tried to reduce the operating pressure of the supercritical CO<sub>2</sub> power cycle in the present study using different compositions of CO<sub>2</sub>/propane mixture as working fluids of cycle driven by waste heat.

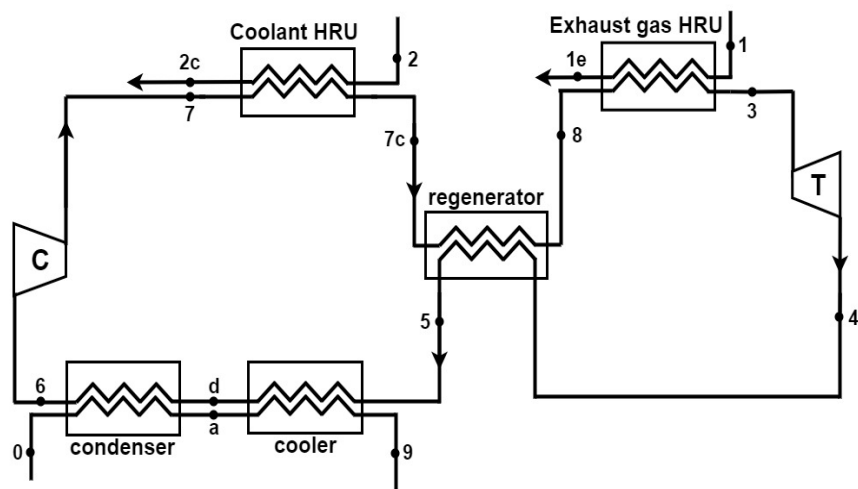


**Fig. 1: Effect of different CO<sub>2</sub> mass fraction in (CO<sub>2</sub>/ Propane) mixture of critical temperature and temperature glide at condenser operating condition**

It is worthwhile to mention that ODP and GWP of propane are 0 and 3 respectively. Thus, the mixture working fluid ensures an environment friendly operation for all compositions. An inert working fluid can be mixed with a hydrocarbon to reduce the chances of accidental fire due to burning of the hydrocarbon [22-24]. CO<sub>2</sub> acts as the diluent to suppress the Propane from accidental flame propagation. To ensure safety against the high flammability of propane, the mass fraction of CO<sub>2</sub> should not be allowed to fall below 0.3 [24].

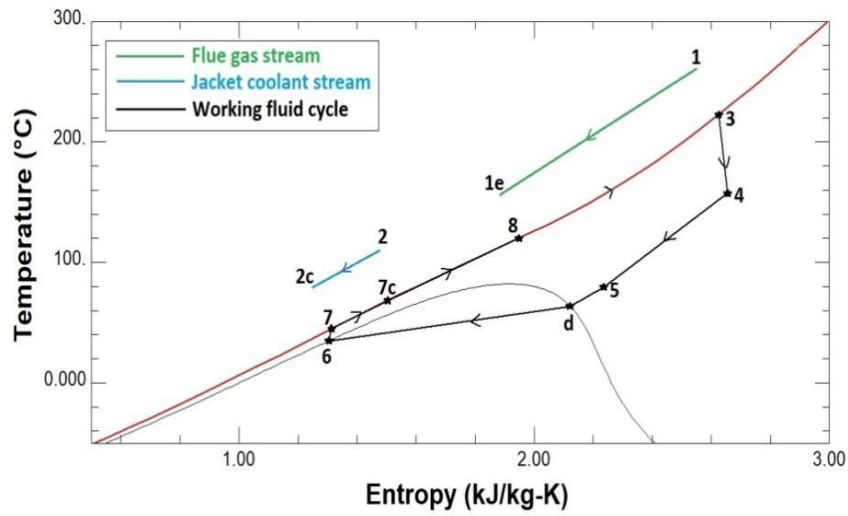
In case of a mixture working fluid, it is not desirable to have a very high glide temperature as it would lead to a composition shift [25]. From Fig. 1, it appears that the temperature glides of the considered CO<sub>2</sub>/ propane mixture for all the considered mass fraction ratios remain well below 50°C.

It also appears from Fig. 1 that mixing propane with CO<sub>2</sub> results in an increase in the critical temperature compared to that of pure CO<sub>2</sub>, thus eliminating a low temperature heat sink (at temperatures less than 30°C) and permitting the operation of the cycle driven by exhaust gas heat in trans-critical mode even for a 25°C ambient temperature. Trans-critical mode of operation appreciably reduces the power consumption of the compressor when compared to that of a supercritical cycle.





**Fig. 2(a): Layout of the waste heat driven cycle**



**Fig. 2 (b): T-s diagram of the waste heat driven cycle**

**Table 1: Diesel power plant waste heat data [26]**

Input parameters	Value
Engine shaft power (MW)	9
Electric power (MW)	8.73
Specific fuel consumption (g /kWh)	183
Exhaust gas temperature (°C)	345
Mass flow rate of exhaust gas (kg/s)	16.7
Temperature of jacket cooling water	78.4
Cooling water available (kg/s)	27.02

## **5. System description**

Fig. 2 (a) shows the layout of the power cycle recovering waste heat from a diesel power plant. Fig. 2 (b) is the temperature entropy diagram associated with the layout. From Table 1, we observe that exhaust gas and engine coolant are the main carriers of the exhaust waste heat of the diesel power plant under consideration. The power cycle presented, hence, consists of two heat recovery units (HRUs) recovering waste heat of both the exhaust gas and engine coolant. The working fluid is heated from the compressor exit state (i.e., 7) to the regenerator inlet state (i.e., 7c) in the engine coolant HRU. After undergoing a heating process in the regenerator (process 7c-8), the hot working fluid enters into the exhaust gas HRU. In the exhaust gas HRU, the working fluid is heated up to the turbine inlet state. The mixture working fluid exiting the exhaust gas HRU is expanded through the radial flow turbine (process 3-4) to produce the output power. A portion of turbine power is expended to run the compressor.

## **6. Modeling and methodology**

The intention of this study is to systematically implement waste heat recovery in a diesel power plant using a CO<sub>2</sub>/ propane mixture based transcritical power cycle. Thus, to analyze the performance of the implemented waste heat recovery scheme, a mathematical is developed based on the following simplified assumptions:

- i. Steady flow operating conditions are applicable
- ii. Isentropic efficiencies of the compressor and the turbine are both assumed to be 85%.
- iii. The ambient condition is specified to be 100kPa and 25°C.
- iv. The chemical exergy has been ignored as the composition is constant throughout the cycle.
- v. All the heat exchangers are assumed to be of shell and tube type.
- vi. In both the HRU, the working fluid is assumed to flows through tubes
- vii. Working fluid mass flux is assumed to be 350kg/m<sup>2</sup>s
- viii. Flue gas velocity over the tube bank is not allowed to go above 10m/s.
- ix. Maximum velocity of engine coolant in the HRU is assumed to be 0.75m/s
- x. In the regenerator, high pressure working fluid is taken on the tube side, while the low pressure working fluid is taken on the shell side.
- xi. The thermo-physical properties of flue gas are assumed to be the same as that of air.
- xii. The cooling water is available at 25°C. Thus, the minimum cycle temperature is assumed to be 35°C.

- xiii. Flue gas contains SO<sub>2</sub>. Thus, the acid dew point temperature of the flue gas is assumed to be 120°C (so the flue gas is cooled to just 130 °C for additional safety).
- xiv. Due to a lower turbine power output (< 1.5 MW turbine power), radial flow turbines are used.
- xv. The whole heat exchanger system is designed taking a pinch point temperature difference of 10°C.

### 6.1. Thermodynamic performance estimation

Cycle power output and 2<sup>nd</sup> law efficiency are the parameters to depict the thermodynamic performance of the waste heat recovery scheme. For any specified composition of the working fluid, the working fluid mass flow rate is estimated from the energy balance of the exhaust gas HRU as presented below:

$$\dot{m}_{WF} = \frac{\dot{m}_{gi} C_{pg} (T_1 - T_{1e})}{h_3 - h_8} \quad (1)$$

The mass flow rate of the engine coolant (i.e., Jacket cooling water) through the engine coolant HRU is estimated as

$$\dot{m}_{Jcw} = \frac{\dot{m}(h_{7c} - h_7)}{C_{pJcw}(T_2 - T_{2c})} \quad (2)$$

Turbine power output, compressor power input, net cycle power output and 1<sup>st</sup> law efficiency are estimated by Eqs. (3) to (6).

$$\dot{W}_t = \dot{m}_{WF}(h_3 - h_4) \quad (3)$$

$$\dot{W}_c = \dot{m}_{WF}(h_7 - h_6) \quad (4)$$

$$\dot{W}_{net} = \dot{W}_t - \dot{W}_c \quad (5)$$

$$\eta_I = \frac{\dot{W}_{net}}{\dot{m}_{cw}C_{pw}(T_2 - T_{2c}) + \dot{m}_{gi}C_{pg}(T_1 - T_{1e})} \quad (6)$$

Equations for exergy destructions (or irreversibilities) of different components are summarized in Table 2:

**Table 2: component exergy destruction equations**

Component	Exergy destruction (kW)
Turbine	$\dot{m}_{WF}T_o(s_4 - s_3)$
Compressor	$\dot{m}_{WF}T_o(s_7 - s_6)$
Condenser	$\dot{m}_{WF}T_o(s_6 - s_d) + \dot{m}_{cond}T_o(s_a - s_o)$
Cooler	$\dot{m}_{WF}T_o(s_d - s_5) + \dot{m}_{cond}T_o(s_9 - s_a)$
Regenerator	$\dot{m}_{WF}T_o\{(s_8 - s_{7c}) + (s_5 - s_4)\}$
Flue gas HRU	$\dot{m}_{gi}C_{pg}T_o \ln\left(\frac{T_{1e}}{T_1}\right) + \dot{m}_{WF}T_o(s_3 - s_8)$
Coolant HRU	$\dot{m}_{Jcw}C_{pJcw}T_o \ln\left(\frac{T_{2c}}{T_2}\right) + \dot{m}_{WF}T_o(s_{7c} - s_7)$

Now, 2<sup>nd</sup> law efficiency is expressed as

$$\eta_{II} = \frac{\dot{W}_{net}}{\dot{E}_{infg} + \dot{E}_{inJcw}} = \frac{\dot{E}_{infg} + \dot{E}_{incw} - \Sigma \dot{E}_D - \dot{E}_{Lfg} - \dot{E}_{LJcw} - \dot{E}_{Lcoolant}}{\dot{E}_{infg} + \dot{E}_{inJcw}} \quad (7)$$

Exergy inputs with flue gas and engine coolant are estimated by Eq. (8) and (9) respectively:

$$\dot{E}_{infg} = \dot{m}_{gi}C_{pg}(T_1 - T_o) - \dot{m}_{gi}C_{pg}T_o \ln\left(\frac{T_1}{T_o}\right) \quad (8)$$

$$\dot{E}_{in\ Jcw} = \dot{m}_{Jcwav} C_{pw} (T_2 - T_o) - \dot{m}_{Jcwav} C_{pJcw} T_o \ln \left( \frac{T_2}{T_o} \right) \quad (9)$$

Exergy losses with different outgoing streams are presented as follows:

$$\dot{E}_{Lfg} = \dot{m}_{gi} C_{pg} (T_{1e} - T_o) - \dot{m}_{gi} C_{pg} T_o \ln \left( \frac{T_{1e}}{T_o} \right) \quad (10)$$

$$\dot{E}_{L\ Jcw} = \dot{m}_{Jcw} C_{pw} (T_{2c} - T_o) - \dot{m}_{Jcw} C_{pJcw} T_o \ln \left( \frac{T_{2c}}{T_o} \right) + (\dot{m}_{Jcwav} - \dot{m}_{Jcw}) \dot{e}_{inJcw} \quad (11)$$

$$\dot{E}_{Lcoolant} = \dot{m}_{cond} \{ (h_9 - h_0) - T_o (s_9 - s_0) \} \quad (12)$$

## 6.2. Economic assessment

The intention of the economic assessment is to estimate the levelized electricity cost for the proposed waste heat recovery scheme. The economic assessment begins with the bare module cost estimation of equipment constituting the waste heat recovery system.

The bare module cost of any heat exchanger is a function of its heat transfer area and associated operating pressure. As shown in Fig. 3 the heat exchanger has been discretised into N subsections assuming an equal enthalpy drop is occurring across the each subsection. Finally, the temperatures of the tube side fluid are evaluated accordingly at each of the subsections.

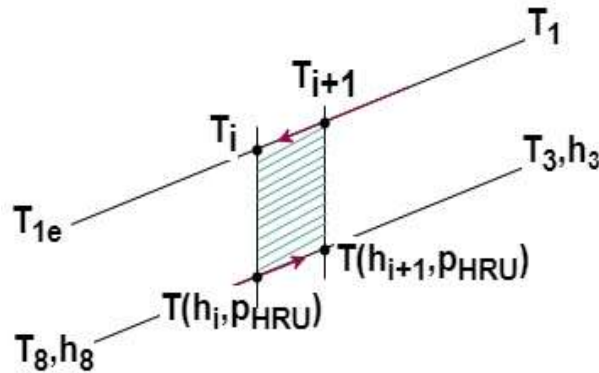


Fig. 3: Discretization of the flue gas HRU



The LMTD at each section has been calculated as

$$LMTD_i = \frac{(T_i - T(h_i)) - (T_{i+1} - T(h_{i+1}))}{\ln\left(\frac{T_i - T(h_i)}{T_{i+1} - T(h_{i+1})}\right)} \quad (13)$$

The heat recovery at each and every subsection is estimated as

$$q = \frac{Q_{FGHRU}}{N} \quad (14)$$

The area required at each and every subsection has been calculated as:

$$A_i = \frac{q}{FU_i LMTD_i} \quad (15)$$

In above equation  $F$  is the correction factor and  $U_i$  is the overall heat transfer coefficient. The overall heat transfer coefficient is expressed as

$$\frac{1}{U_i} = \frac{1}{\alpha_{si}} + \frac{1}{\alpha_{ti}} \quad (16)$$

Shell side heat transfer coefficient is estimated by using following correlation of fluid flowing over the tube bank [27]:

$$Nu_{si} = 0.35 \left(\frac{S_T}{S_L}\right)^{0.2} Re_{si}^{0.6} Pr_{si}^{0.36} \quad (17)$$

For supercritical CO<sub>2</sub> flowing inside the tube, Protopopov correlation (without wall correction factor) is applied to estimate the associated Nusselt number [28]. Heat transfer area of a heat exchanger is estimated by adding areas of all discretized elements.

Once the areas of all heat exchangers, turbine and compressor capacities are estimated, the purchase cost of any equipment is estimated by using following equation [29]

$$\log_{10} C_p^0 = K_1 + K_2 \log_{10} Z + K_3 [\log_{10} Z]^2 \quad (18)$$

Hence, the bare module cost of individual equipment is expressed as

$$C_{bm} = C_p^0 (B_1 + B_2 F_m F_p) = C_p^0 F_{BM} \quad (19)$$

$F_{BM}$  is the bare module factor.  $F_m$  &  $F_p$  are material correction and pressure correction factors respectively.

The pressure correction factor for heat exchangers is estimated by the following equation:

$$\log_{10} F_p = C_1 + C_2 \log_{10}(P) + C_3 \{\log_{10}(P)\}^2 \quad (20)$$

In Eq. (20),  $P$  is the operating pressure in bar gauge. The total equipment cost is converted in to the cost of current date by applying Eq. (21).

$$C_{Tot} = \left( \sum C_{BM,eq} \right) \times \left( \frac{CEPCI_{current\ year}}{CEPCI_{2001}} \right) \quad (21)$$

The values of different coefficients of bare module cost estimation are summarized in Table 3.

**Table 3: Coefficient for total cost estimation [29]**

Equipments	Performance parameters (Z)	K <sub>1</sub>	K <sub>2</sub>	K <sub>3</sub>	B <sub>1</sub>	B <sub>2</sub>	F <sub>M</sub>	C <sub>1</sub>	C <sub>2</sub>	C <sub>3</sub>
FGHRU	A <sub>FGHRU</sub> (m <sup>2</sup> )	4.8306	-0.8509	0.3187	1.63	1.66	1.3178	-0.00164	-0.00627	0.0123
Jacket CWHRU	A <sub>CWHRU</sub> (m <sup>2</sup> )	4.3247	-0.3030	0.1634	1.63	1.66	1.3178	-0.00164	-0.00627	0.0123
Regenerator	A <sub>reg</sub> (m <sup>2</sup> )	4.8306	-0.8509	0.3187	1.63	1.66	1.3178	-0.03881	-0.11272	0.08183
Condenser	A <sub>cond</sub> (m <sup>2</sup> )	4.3247	-0.3030	0.1634	1.63	1.66	1.3178	-0.00164	-0.00627	0.0123
Turbine	W <sub>t</sub> (kW)	2.2476	1.4965	-0.1618	—	—	3.4825	—	—	—
Compressor	W <sub>c</sub> (kW)	2.2897	1.3604	-0.1027	—	—	2.433	—	—	—

Finally, the levelized electricity cost is estimated as follows

$$LEC = \frac{CRF \times C_{Tot} + C_{OM}}{W_{net} \times AOH} \quad (22)$$

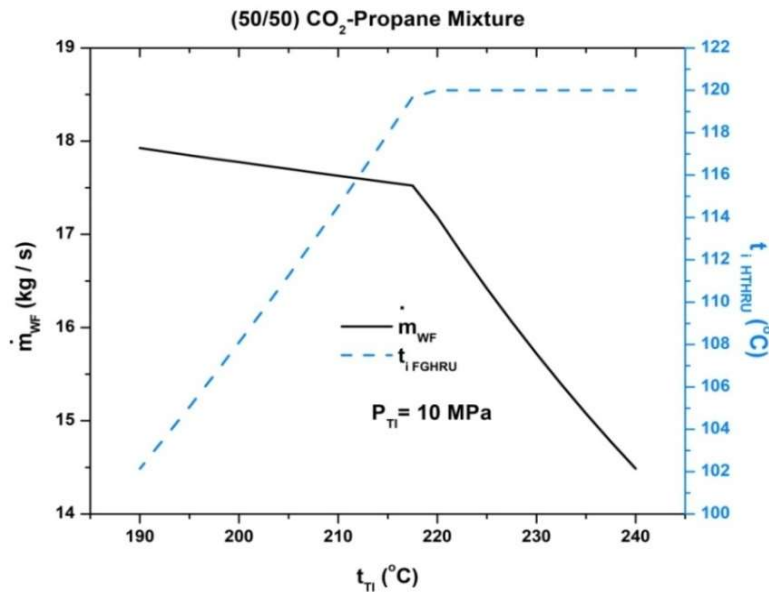
In Eq. (22), annual operating hour (AOH) is assumed to be 8000 hours. Annual operation and maintenance cost is 5% of the total capital investment. The capital recovery factor is estimated from the following equation:

$$CRF = \frac{i (1 + i)^{LT}}{(1 + i)^{LT} - 1} \quad (23)$$

While estimating the CRF, life of the plant and interest rate are assumed 25 years and 5% respectively.

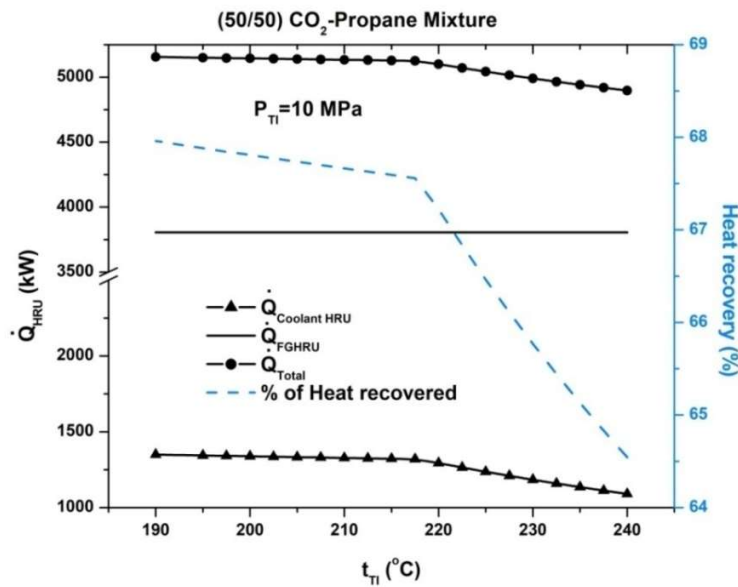
## 7. Results and discussion

In the present study, CO<sub>2</sub>/Propane mixtures with different CO<sub>2</sub> mass ratios are employed as the working fluid of a trans-critical power cycle recovering the diesel power plant waste heat. Initially in this section, effects of different input parameters on cycle performance are discussed for a specified mixture composition. Effects of varying mixture composition on cycle performance are also discussed in the subsequent stage of the study. Finally, the optimum levelized electricity cost (LEC) and associated operating parameters are presented and compared with those of the optimized supercritical CO<sub>2</sub> power cycle recovering the waste heat of a similar source. It is important to note that the proposed power cycle consists of two heat recovery units and a regenerator. The quantity of recoverable high grade waste heat differs appreciably compared to that of the recoverable low grade waste heat. While optimizing, maximum usable high grade waste heat is recovered due to its greater exergy content.



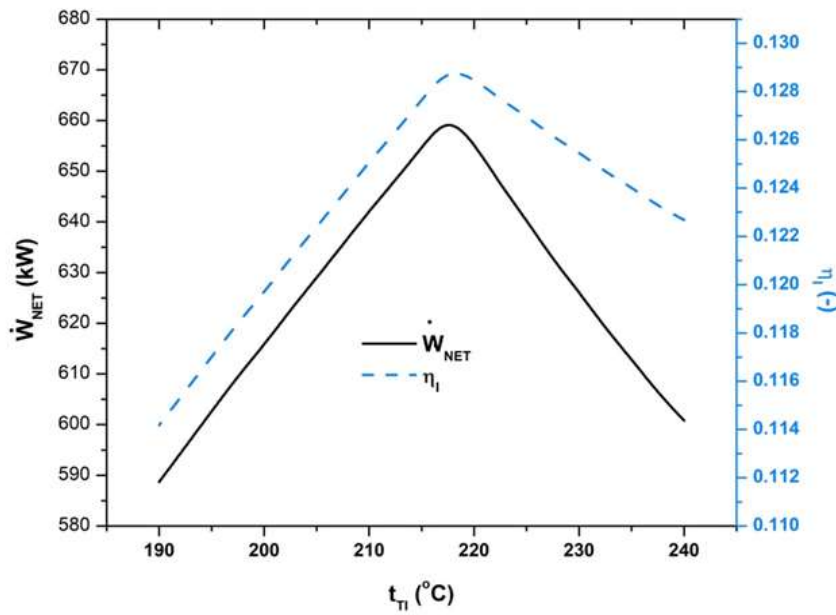
**Fig. 4: Effects of turbine inlet temperature on working fluid mass flow rate and working fluid inlet temperature to FGHRU**

Effects of varying turbine inlet temperature on working fluid mass flow rate and inlet temperature of working fluid to the FGHRU are presented in Fig. 4. Working fluid mass flow rate initially slowly decreases with an increasing turbine inlet temperature. However, the mass flow rate of working fluid starts to decrease much rapidly as turbine inlet temperature is raised above a certain value. With an increasing turbine inlet temperature, specific enthalpy change of the working fluid in the FGHRU increases. However, with initial increments of the turbine inlet temperature, this increment is not very rapid as working fluid inlet temperature to the FGHRU increases due to the increasing heat duty of the regenerator. However, as a reasonable pinch point temperature difference (i.e., 10°C or above) is to be maintained in the FGHRU, the temperature of the high pressure working fluid exiting the regenerator is not allowed to go above 120°C, as shown in Fig. 4. As temperature of the high pressure working fluid stream reaches to 120°C, mass flow rate of the working fluid through the FGHRU starts to decrease rapidly with a further increment in turbine inlet temperature (mainly, due to the rapid increment in specific enthalpy change of the working fluid).



**Fig. 5: Effects of varying turbine inlet temperature of waste heat recovery**

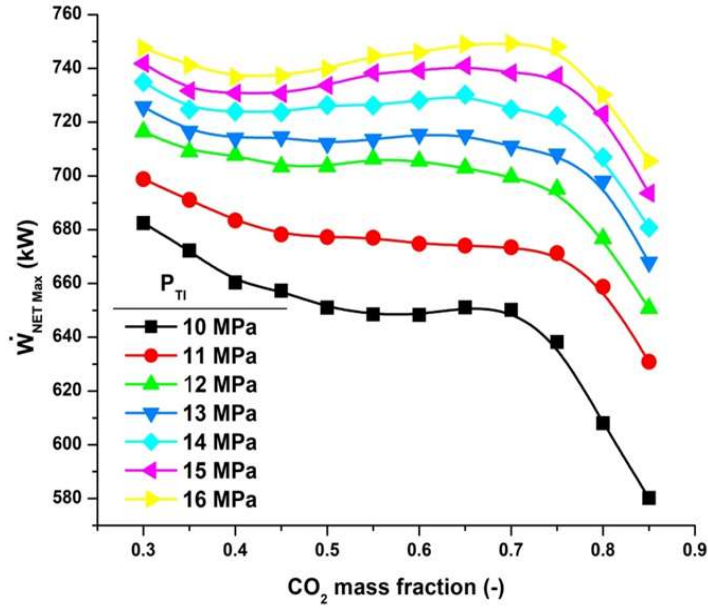
Effects of varying turbine inlet temperature on heat recoveries in different HRUs are presented in Fig. 5. Always the entire recoverable heat of the exhaust gas is recovered due its higher exergy content. Thus, the heat duty of the FGHRU is independent of turbine inlet temperature. Heat recovery in the coolant HRU as well as % of heat recovery rapidly decreases above a certain turbine inlet pressure due to the rapid reduction of the working fluid mass flow rate.



**Fig. 6: Effects of varying turbine inlet temperature in net work output and 1<sup>st</sup> law efficiency**

It is observed in Fig. 6 that for any specified turbine inlet pressure; there exists an optimum turbine inlet temperature corresponding to the maximum cycle power output (or maximum 1<sup>st</sup> law efficiency). As regenerator exit temperature of the higher pressure working fluid stream is not allowed to go above 120°C, the turbine inlet temperature corresponding to this particular operating condition results in the highest 1<sup>st</sup> law efficiency and power output.



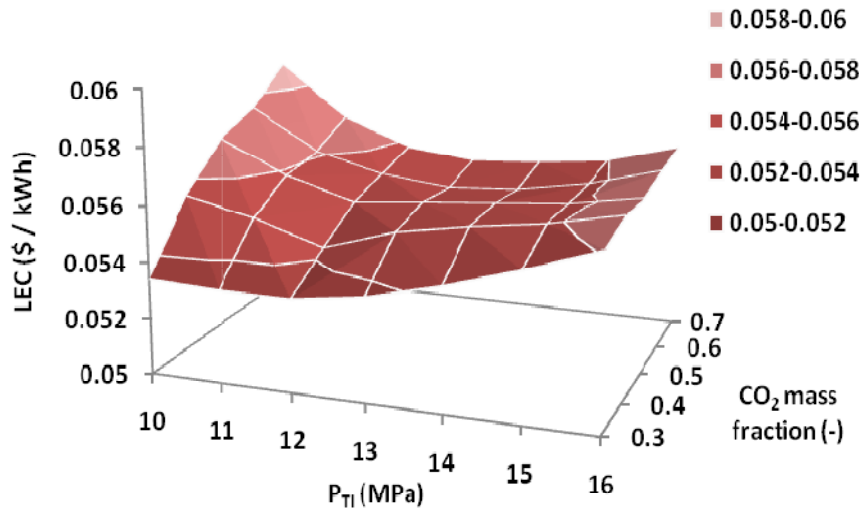


**Fig. 7: Effects of varying CO<sub>2</sub> mass fraction on maximum cycle power output at different turbine inlet pressure**

Effects of varying CO<sub>2</sub> mass fraction in CO<sub>2</sub>/ propane mixture on maximum achievable power outputs corresponding to different turbine inlet pressure are presented in Fig. 7. It is observed that for any specified working fluid composition, cycle power output increases with an increasing turbine inlet pressure. However, above a certain turbine inlet pressure this increment is not very significant. It appears from Fig. 7 that, for a lower turbine inlet pressure (13 MPa or less); reducing the CO<sub>2</sub> mass fraction of the mixture working fluid significantly enhances cycle power output. For a turbine inlet pressure above 13 MPa, net cycle power output remains more or less constant for CO<sub>2</sub> mass fraction varying between 0.3 and 0.75. For all considered turbine inlet pressures, raising the CO<sub>2</sub> mass fraction above 0.75 results rapid decrement in cycle power output.

Effects of varying the CO<sub>2</sub> mass fraction in the working fluid and the turbine inlet pressure on levelized electricity cost (LEC) is presented in Fig. 8. It appears from Fig. 8 that LEC is a

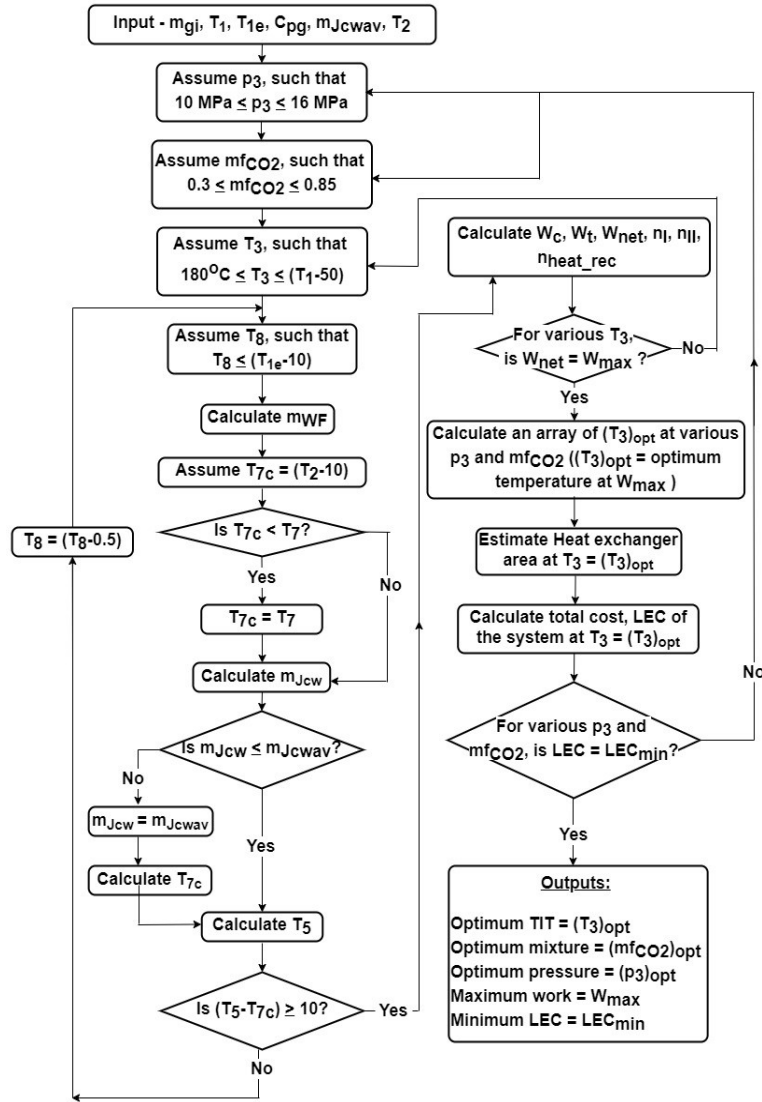
minimum if the cycle is operated with the 0.3 mass fraction of CO<sub>2</sub> in the working fluid. It is also observed that for a higher turbine inlet pressure, LEC is a weak function of the working fluid composition. It is observed in Fig. 8 that for all specified working fluid compositions, varying turbine inlet pressure significantly affects the LEC. For each specified composition of the working fluid, there exists an optimum turbine inlet pressure corresponding to a minimum LEC of the presented waste heat recovery scheme.



**Fig. 8: Effects of varying CO<sub>2</sub> mass fraction and turbine inlet pressure on levelized electricity cost**

As the intention of the present study is to explore the optimum operating condition for the CO<sub>2</sub>/propane mixture based transcritical power cycle recovering the waste heat of a diesel power plant, an optimization algorithm is proposed as presented in Fig. 9. While recovering the maximum usable high grade waste heat, the presented optimization algorithm of Fig. 4 initially estimates the optimum turbine inlet temperature corresponding to the maximum power output at any specified turbine inlet pressure. The optimization algorithm also iterates the turbine inlet pressures and mixture composition to find out their optimum value corresponding to the minimum levelized electricity cost (LEC). Pinch point temperature differences of all heat

exchangers, maximum usable low grade waste heat in the coolant HRU, acid condensation temperature of the flue gas and minimum allowable mass fraction of CO<sub>2</sub> (depending on safety issue) are applied constraints of the optimization algorithm.



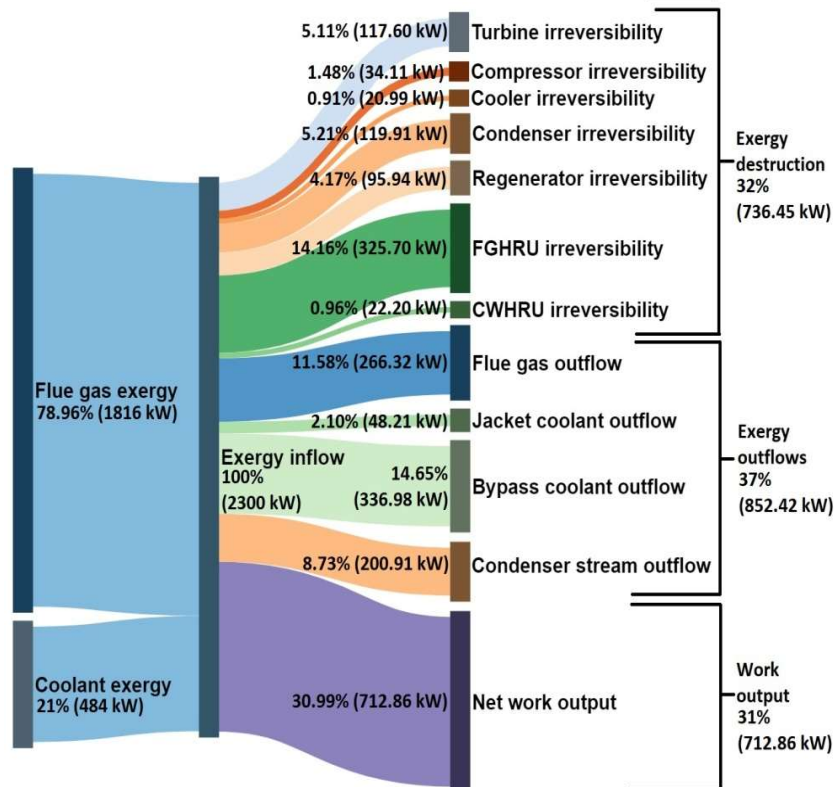
**Fig. 9: Optimization algorithm**

Minimum levelized electricity cost (LEC) and associated other parameters obtained by applying the optimization algorithm are summarized in Table 4.

**Table 4: Parameters corresponding to minimum LEC**

Type of cycle	$t_{TI}$ (°C)	$P_{TI}$ (MPa)	$P_{Te}$ (MPa)	CO <sub>2</sub> mass fraction	$W_{NET}$ (kW)	$\eta_{II}$ (%)	$LEC_{Min}$ (\$/kWh)
Trans-critical cycle with CO <sub>2</sub> - propane mixture	222.5	12.00	3.5606	0.3	712.90	36.32	0.053

A Grassmann diagram corresponding to the operating condition of Table 4 is presented in Fig. 10 to depict exergy destructions of different components and exergy losses associated with different fluid streams exiting the waste heat recovery system. It is observed that the largest exergy destruction occurs in the FGHRU. The maximum exergy loss occurs with the flue gas stream exiting the HRU. However, this exergy loss with the flue gas stream is unavoidable due to the constraint of acid condensation.



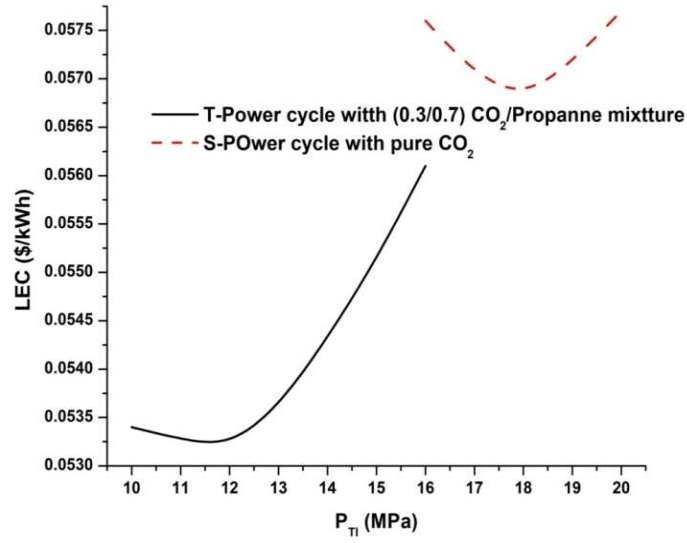
**Fig. 10: Grassmann diagram**

For a better understanding state point properties corresponding to the optimized operating condition are summarized in Table 5.

**Table 1: State points of the optimized cycle**

<b>Working fluid</b>				
<i>State points</i>	<i>t (°C)</i>	<i>P (MPa)</i>	<i>h (kJ/kg)</i>	<i>s (kJ/kgK)</i>
3	222.50	12.000	834.19	2.6248
4	157.38	3.5606	759.611	2.6556
5	79.54	3.5606	595.991	2.2358
d	63.72	3.5606	556.52	2.1212
6	35.00	3.5606	291.73	1.3046
7	44.95	12.000	310.64	1.3135
7c	68.40	12.000	373.35	1.5037
8	120.00	12.000	536.97	1.9486
<b>Flue gas stream</b>				
<i>State points</i>	<i>t (°C)</i>	<i>P (MPa)</i>	<i>h (kJ/kg)</i>	<i>s (kJ/kgK)</i>
1	345.00	0.1	_____	_____
1e	130.00	0.1	=====	=====
<b>Jacket coolant water stream</b>				
<i>State points</i>	<i>t (°C)</i>	<i>P (MPa)</i>	<i>h (kJ/kg)</i>	<i>s (kJ/kgK)</i>
2	78.40	0.1	_____	_____
2c	54.95	0.1	=====	=====
<b>Condenser and cooler water streams</b>				
<i>State points</i>	<i>t (°C)</i>	<i>P (MPa)</i>	<i>h (kJ/kg)</i>	<i>s (kJ/kgK)</i>
0	25.00	0.1	_____	_____
a	53.71	0.1	_____	_____
9	57.99	0.1	=====	=====

In Fig. 11, minimum levelized electricity costs for different turbine inlet pressures of the mixture based cycle are compared with those of the supercritical CO<sub>2</sub> power cycle.



**Fig.11: Comparison of minimum achievable LEC at different TIP of the transcritical power cycle with mixture working fluid with the LEC at different TIP of the supercritical  $CO_2$  power cycle.**

It appears from Fig. 11 that the minimum achievable LEC of the transcritical cycle with the mixture working fluid is 6.36% lower compared to that of the supercritical power cycle using pure  $CO_2$  as the working fluid. It is also apparent that the turbine inlet pressure corresponding to the minimum LEC of the waste heat driven cycle using  $CO_2$ / Propane mixture as the working fluid is close to 33% lower compared to that of the waste heat driven supercritical power cycle using pure  $CO_2$  as the working fluid.



## 8. Conclusions

Intention of the present study is to employ a transcritical regenerative power cycle to recover waste heat of a diesel power plant. CO<sub>2</sub>/propane mixture with different CO<sub>2</sub> mass ratio is used as the working fluid of the power cycle to ensure safe and environment friendly operation simultaneously. An optimization algorithm is also employed to ensure the best operating performance of the presented power cycle. The principal findings of the study are summarized as follows:

- It is observed that, at a lower turbine inlet pressure of working fluid, cycle power output significantly increases with reducing CO<sub>2</sub> mass fraction in the mixture working fluid. Corresponding reduction in levelized electricity cost (LEC) is also found to be significant. For a higher turbine inlet pressure, effects of varying mixture composition are having less significant effects on cycle power output and LECs.
- For any specified mixture composition net cycle power output increases with an increasing turbine inlet pressure. However, this increment is not very appreciable above a certain turbine inlet pressure (i.e., 14 MPa).
- For any specified mixture composition, LEC becomes minimum corresponding to a specific turbine inlet pressure. The minimum LEC of the cycle is found to be at 12 MPa turbine inlet pressure, for 0.3 mass fraction of CO<sub>2</sub>.
- The minimum achievable LEC for the presented transcritical cycle operating with mixture working fluid is close to 6.36% lower compared to that of an optimized supercritical CO<sub>2</sub> power cycle recovering waste heat from a similar source.

Corresponding turbine inlet pressure for the transcritical mixture based cycle is close to 33% lower compared to that of the supercritical CO<sub>2</sub> power cycle.

Finally, diesel power plant and the presented waste heat recovery scheme together can yield 8% higher power output compared to the yielded power output of the diesel power plant without waste heat recovery.

## 9. References

1. Mondal S., De S. (2022) Diesel Engine Waste Heat Recovery Schemes for Improved Fuel Economy and Reduced Emissions: Simulation Results. In: Agarwal A.K., Kumar D., Sharma N., Sonawane U. (eds) Engine Modeling and Simulation. Energy, Environment, and Sustainability. Springer, Singapore. [https://doi.org/10.1007/978-981-16-8618-4\\_13](https://doi.org/10.1007/978-981-16-8618-4_13)
2. Hiereth H, Prenninger P (2007) Charging the internal combustion engine. Springer, New York.
3. Aghaali, H., Ångström, H-E. (2015) A review of turbocompounding as a waste heat recovery system for internal combustion engines. Renewable and Sustainable Energy Reviews 49, 813–824.
4. Yu, G., Shu, G., Tian, H., Wei, H., Liu, L.(2013) Simulation and thermodynamic analysis of a bottoming Organic Rankine Cycle (ORC) of diesel engine (DE). Energy 51, 281-290.
5. Shu, G., Li, X., Tian, H., Liang, X., Wei, H., Wang, Xu. (2014) Alkanes as working fluids for high-temperature exhaust heat recovery of diesel engine using organic Rankine cycle. Applied Energy 119, 204–217.
6. Yang, M. (2016) Optimizations of the waste heat recovery system for a large marine diesel engine based on transcritical Rankine cycle. Energy 113, 1109–1124.
7. Boodaghi, H., Etghani, M. M., Sedighi, K. (2021) Performance analysis of a dual-loop bottoming organic Rankine cycle (ORC) for waste heat recovery of a heavy-duty diesel engine, Part I: Thermodynamic analysis. Energy Conversion and Management 241, 113830.

8. Lion, S., Taccani, R., Vlaskos, I., Scrocco, P., Vouvakos, X., Kaiktsis, L. (2019) Thermodynamic analysis of waste heat recovery using Organic Rankine Cycle (ORC) for a two-stroke low speed marine Diesel engine in IMO Tier II and Tier III operation. *Energy* 183, 48-60.
9. Mondal, S., De, S. (2015) CO<sub>2</sub> based power cycle with multi-stage compression and intercooling for low temperature waste heat recovery. *Energy* 90, 1132-1143.
10. Mondal, S., De, S. (2015) Transcritical CO<sub>2</sub> power cycle—effects of regenerative heating using turbine bleed gas at intermediate pressure. *Energy* 87, 95-103.
11. Zhao, D., Zhao, R., Deng, S., Zhao, L., Chen, M. (2020) Transcritical carbon dioxide power cycle for waste heat recovery: A roadmap analysis from ideal cycle to real cycle with case implementation. *Energy Conversion and Management* 226, 113578.
12. Hosseinpour, J., Howard, J., Chen, J., Engeda, A. (2022) Challenges for Developing and Marketing a Brayton-Cycle Based Power Genset Gas-Turbine Using Supercritical CO<sub>2</sub> and a Compressor Design for Simple Recuperated Cycle. *Journal of Energy Resources Technology* 144, 032101.
13. Song, J., Li, X., Ren, X., Gu, C. (2018) Performance improvement of a preheating supercritical CO<sub>2</sub> (S-CO<sub>2</sub>) cycle based system for engine waste heat recovery. *Energy Conversion and Management* 161, 225-233.
14. Pan, R., Yuan, C., Sun, Y., Yan, X., Lu, M., Bucknall, R. (2020) Thermo-economic analysis and multi-objective optimization of S-CO<sub>2</sub> Brayton cycle waste heat recovery system for an ocean-going 9000 TEU container ship. *Energy Conversion and Management* 221, 113077.

15. Mondal, S., Datta, S., De, S. (2020) Auxiliary power through marine waste heat recovery using a CO<sub>2</sub>-organic cascading cycle. *Clean Technologies and Environmental Policy* 22, 893–906.
16. Sakalis, G. (2021) Investigation of supercritical CO<sub>2</sub> cycles potential for marine Diesel engine waste heat recovery applications. *Applied Thermal Engineering* 195, 117201.
17. Zhang, R., Su, W., Lin, X., Zhou, N., Zhao L. (2020) Thermodynamic analysis and parametric optimization of a novel S-CO<sub>2</sub> power cycle for the waste heat recovery of internal combustion engines . *Energy* 209, 118484.
18. Shu, G., Wang, R., Tian, H., Wang, X., Li, X., Cai, J., Xu, Z. (2020) Dynamic performance of the transcritical power cycle using CO<sub>2</sub>-based binary zeotropic mixtures for truck engine waste heat recovery. *Energy* 209, 116825.
19. Liu, P., Shu, G., Tian, H., Feng, W., Shi, L., Xu, Z. (2019) Preliminary experimental comparison and feasibility analysis of CO<sub>2</sub>/R134a mixture in Organic Rankine Cycle for waste heat recovery from diesel engines. *Energy Conversion and Management* 198, 111776.
20. Shu, G., Yu, Z., Tian, H., Liu, P., Xu, Z. (2018) Potential of the transcritical Rankine cycle using CO<sub>2</sub>-based binary zeotropic mixtures for engine's waste heat recovery. *Energy Conversion and Management* 174, 668-685.
21. Xu, J., Liu, C., Sun, C., Xie, J., Li, M., Yang, Y. (2019) Perspective of SCO<sub>2</sub> power cycles. *Energy* 186, 115831.
22. Mondal, S., De, S. (2019) Waste heat recovery through organic flash cycle (OFC) using R245fa–R600 mixture as the working fluid. *Clean Technologies and Environmental Policy* 21, 1575–1586.

23. Garg, P., Kumar, P., Srinivasan, K., Dutta, P. (2013) Evaluation of isopenatane, R245-fa and their mixture as working fluid for organic Rankine cycles. *Applied Thermal Engineering* 51, 292–300.
24. Garg, P., Kumar, P., Srinivasan, K., Dutta, P. (2013) Evaluation of carbon dioxide blends with isopentane and propane as working fluids for organic Rankine cycles. *Applied Thermal Engineering* 52,439–448.
25. Dai, B., Li, M., Ma, Y. (2014) Thermodynamic analysis of carbon dioxide blends with low GWP (global warming potential) working fluids-based transcritical Rankine cycles for low-grade heat energy recovery. *Energy* 64, 942-952.
26. Morawski, A. P., Araújo, L. R. d., Schiaffino, M. S., Oliveira, R. C. d., Chun, A., Ribeiro, L. C., Santos, J. J. C. S., S., Donatelli, J. L. M., Cunha, C.C.M. (2021) On the suitable superstructure thermoeconomic optimization of a waste heat recovery system for a Brazilian diesel engine power plant. *Energy Conversion and Management* 234, 113947.
27. Cengel, Y. A., Ghajar, A.J. (2011) *Heat and Mass Transfer: Fundamental and application*. 5<sup>th</sup> edition, McGraw-Hill Education.
28. Pioro, I.L., Khartabil, H.F., Duffey, R. B. (2004) Heat transfer to supercritical fluids flowing in channels—empirical correlations (survey). *Nuclear Engineering and Design* 230, 69–91.
29. Turton, R., Bailie, R.C., Whiting, W.B. (2013) *Analysis, synthesis and design of chemical processes*, 4th edn. Prentice Hall PTR, New Jersey.