

**BACHELOR OF ENGINEERING IN CHEMICAL ENGINEERING EXAMINATION, 2019**

( 2nd Year, 2nd Semester )

**CHEMICAL ENGINEERING THERMODYNAMICS**

Time : Three hours

Full Marks : 100

( 50 marks for each Part )

Use a separate Answer-Script for each Part

**PART - I**

The symbols have their usual meaning

Assume any missing data

Answer any two questions

1. (a) Estimate the state of water at 150 °C and 2 bar.  
 (b) Determine the enthalpy of water at 150 °C and 2 bar, given that the enthalpy of liquid water (saturated) at 0 °C is -0.04 kJ/kg. (5 + 20)
- The virial coefficient correlation may be assumed to give good representation of equation of state of the system

$$Z = 1 + \left( \frac{BP_c}{RT_c} \right) \frac{P_r}{T_r} = (B^0 + \omega B^1) \frac{P_r}{T_r}$$

$$B^0 = 0.083 - \frac{0.422}{T_r^{1.6}}$$

$$B^1 = 0.139 - \frac{0.172}{T_r^{4.2}}$$

The critical temperature, pressure and acentric factor of water are 647.1 K, 220.55 bar and 0.345 respectively.

The vapor pressure of and water is given by

$$\log_{10} P(\text{Torr}) = 8.07131 - \frac{1730.63}{t(^{\circ}\text{C}) + 233.46}$$

Other correlations:

Riedel

$$\frac{\lambda(T_n)}{RT_n} = \frac{1.092(\ln P_c - 1.013)}{0.93 - T_n}$$

Watson

$$\frac{\lambda(T_2)}{\lambda(T_1)} = \left( \frac{1 - T_{r_2}}{1 - T_{r_1}} \right)^{0.38}$$

2. (i) The partial molar volume of species 1 in a binary solution at constant  $t$  and  $P$  is given by

$$\bar{V}_1 = V_1 + \alpha x_2^2$$

- (a) What is the corresponding expression of  $\bar{V}_2$ .  
 (b) What the expression of  $V$  consistent with these equations.  
 (c) What are the corresponding equations for  $V^E$ ,  $\bar{V}_1^E$  and  $\bar{V}_2^E$ ? (7+2+10)

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(ii) The excess Gibbs energy of a liquid mixture at T and P is given by

$$\frac{G^E}{RT} = x_1 x_2 (-1.2x_1 - 1.5x_2)$$

Find expressions for  $\ln \gamma_1$  and  $\ln \gamma_2$

(6)

3. The following data are available for the molar volume of liquid mixtures of cyclohexane (1) and carbon tetrachloride at 1 atm and 60 °C

| $x_1$ | $V(\text{cm}^3/\text{gmol})$ | $x_1$ | $V(\text{cm}^3/\text{gmol})$ | $x_1$ | $V(\text{cm}^3/\text{gmol})$ |
|-------|------------------------------|-------|------------------------------|-------|------------------------------|
| 0     | 101.46                       | 0.2   | 104.002                      | 0.9   | 112.481                      |
| 0.02  | 101.717                      | 0.3   | 105.253                      | 0.92  | 112.714                      |
| 0.04  | 101.973                      | 0.4   | 106.49                       | 0.94  | 112.946                      |
| 0.06  | 102.228                      | 0.5   | 107.715                      | 0.96  | 113.178                      |
| 0.08  | 102.483                      | 0.6   | 108.926                      | 0.98  | 113.409                      |
| 0.1   | 102.737                      | 0.7   | 110.125                      | 1.0   | 113.64                       |
| 0.15  | 103.371                      | 0.8   | 111.31                       |       |                              |

(a) Use the above data to determine  $V_1, V_2, \bar{V}_1^\infty$  and  $\bar{V}_2^\infty$

(b) Plot  $\Delta V$  versus  $x_1$  taking Lewis Randall standard state for both components 1 and 2.

Determine  $\Delta \bar{V}_1$  and  $\Delta \bar{V}_2$  at  $x_1 = 0.35$ ?

(25)

## PART II

**Answer any 2 (two) questions**

All symbols have their usual meanings

Assume any missing data

|       |  |
|-------|--|
| Q1(A) | <p>A binary liquid mixture is in equilibrium with its vapor at 300K. The liquid mole fraction of species 1 is 0.4 and the molar excess Gibbs free energy is 200 J/mol. If <math>\gamma_1 = 1.09</math>, calculate the value of <math>\gamma_2</math>. <math>\gamma_i</math> denotes liquid-phase activity coefficient of species <math>i</math> in the binary mixture. [5]</p>   |
| Q1(B) | <p>Starting with the simplest form of virial equation prove that the fugacity of a pure liquid species at a pressure (P) and temperature (T) is given by the following expression</p> $f = p^{sat} \exp \left[ \frac{Bp^{sat} + v^l(P - p^{sat})}{RT} \right]$ <p>where <math>B</math>, <math>p^{sat}</math> and <math>v^l</math> are second virial coefficient, saturation vapour pressure and molar volume of the pure liquid, respectively. List your assumptions [5]</p> |

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| Q1(C)     | <p>A binary liquid mixture containing 40.5 mol% ethanol (1) and the rest methylcyclohexane(2) exerts an equilibrium pressure of 152.4 mm Hg at 35 °C and the vapor phase contains 54.7 mol% ethanol. The Antoine equations for ethanol (1) and methylcyclohexane (2) are given below:</p> $\ln P_1^{sat} = 8.2130 - \left[ \frac{1652.05}{t + 231.480} \right]$ $\ln P_2^{sat} = 6.8230 - \left[ \frac{1270.763}{t + 221.416} \right]$ <p>where <math>P^{sat}</math> and <math>t</math> are in mm Hg and °C, respectively</p> <p>a. Based on the experimental data given in the problem statement, estimate the van Laar parameters (<math>\alpha</math> and <math>\beta</math>) [8]</p> <p>b. Determine the vapour composition in equilibrium with a liquid mixture containing 60 mol% ethanol at 35 °C. [7]</p> <p>The van Laar equations are given below</p> $\ln \gamma_1 = \frac{\alpha}{\left[ 1 + \frac{\alpha}{\beta} \frac{x_1}{x_2} \right]^2} ; \quad \ln \gamma_2 = \frac{\beta}{\left[ 1 + \frac{\beta}{\alpha} \frac{x_2}{x_1} \right]^2}$ $\alpha = \left[ 1 + \frac{x_2 \ln \gamma_2}{x_1 \ln \gamma_1} \right]^2 \ln \gamma_1 ; \quad \beta = \left[ 1 + \frac{x_1 \ln \gamma_1}{x_2 \ln \gamma_2} \right]^2 \ln \gamma_2$ |         |        |   |   |          |         |         |        |           |         |         |        |
|-----------|---|---------|--------|---|---|----------|---------|---------|--------|-----------|---------|---------|--------|
| Q2(A)     | <p>An ideal vapour-liquid mixture of n-hexane (1) and n-heptane (2) is under equilibrium conditions. Calculate the following:</p> <p>(a) vapour composition at 27 °C when the liquid phase contains 20 mol% n-hexane. [4]</p> <p>(b) liquid composition at 27 °C when the vapour phase contains 20 mol% n-hexane. [4]</p> <p>(c) vapour composition at a total pressure of 30 kPa and the liquid phase containing 20 mol% n-hexane (show calculations for only one iteration). [7]</p> <p>The Antoine constants for n-hexane and n-heptane are given below:</p> <table border="1" data-bbox="415 1423 1346 1562"> <thead> <tr> <th></th> <th>A</th> <th>B</th> <th>C</th> </tr> </thead> <tbody> <tr> <td>n-hexane</td> <td>13.8216</td> <td>2697.55</td> <td>224.37</td> </tr> <tr> <td>n-heptane</td> <td>13.8567</td> <td>2911.32</td> <td>216.64</td> </tr> </tbody> </table> $\ln P^{sat} (kPa) = A - \frac{B}{t (^{\circ}C) + C}$   |         | A      | B | C | n-hexane | 13.8216 | 2697.55 | 224.37 | n-heptane | 13.8567 | 2911.32 | 216.64 |
|           | A   | B       | C      |   |   |          |         |         |        |           |         |         |        |
| n-hexane  | 13.8216   | 2697.55 | 224.37 |   |   |          |         |         |        |           |         |         |        |
| n-heptane | 13.8567   | 2911.32 | 216.64 |   |   |          |         |         |        |           |         |         |        |

| Q2(B)        | <p>The activity coefficients of a benzene (1)–cyclohexane (2) mixture at 40 °C, are given by <math>RT \ln \gamma_1 = Ax_2^2</math> and <math>RT \ln \gamma_2 = Ax_1^2</math>. At 40 °C benzene-cyclohexane forms an azeotrope containing 49.4 mol % benzene at a total pressure of 202.5 mm Hg. If the vapour pressures of pure benzene and pure cyclohexane at 40 °C are 182.6 mm and 183.5 mm Hg, respectively, calculate the total pressure for a liquid mixture containing 12.6 mol % benzene at 40 °C. [10]</p>   |                         |                         |                         |              |      |        |            |        |        |
|--------------|--|-------------------------|-------------------------|-------------------------|--------------|------|--------|------------|--------|--------|
| Q3(A)        | <p>Ethanol is manufactured by catalytic vapour phase hydration of ethylene [ <math>C_2H_4 (g) + H_2O (g) \rightleftharpoons C_2H_5OH (g)</math> ]. The reactor operates at 400 K and 2 bar and the feed is a gas mixture of ethylene and steam in the mol ratio 1:3. The equilibrium constant at 400 K is 0.25. Estimate the composition of the equilibrium mixture. Assume ideal gas behavior. [15]</p>   |                         |                         |                         |              |      |        |            |        |        |
| Q3(B)        | <p>Calculate the pressure required for 50% dissociation of nitrogen tetroxide [ <math>N_2O_4 (g) \rightleftharpoons 2 NO_2 (g)</math> ] at 300 K. The standard heat of formation and Gibbs free energy of formation of the reactant and product species (298.15 K and 1 atm) are given below: [10]</p> <table border="1" data-bbox="456 1251 1369 1444"> <thead> <tr> <th></th> <th><math>\Delta h_f^0</math> (kJ/mol)</th> <th><math>\Delta g_f^0</math> (kJ/mol)</th> </tr> </thead> <tbody> <tr> <td><math>N_2O_4 (g)</math></td> <td>9.33</td> <td>97.947</td> </tr> <tr> <td><math>NO_2 (g)</math></td> <td>33.304</td> <td>51.295</td> </tr> </tbody> </table> |                         | $\Delta h_f^0$ (kJ/mol) | $\Delta g_f^0$ (kJ/mol) | $N_2O_4 (g)$ | 9.33 | 97.947 | $NO_2 (g)$ | 33.304 | 51.295 |
|              | $\Delta h_f^0$ (kJ/mol)  | $\Delta g_f^0$ (kJ/mol) |                         |                         |              |      |        |            |        |        |
| $N_2O_4 (g)$ | 9.33   | 97.947                  |                         |                         |              |      |        |            |        |        |
| $NO_2 (g)$   | 33.304   | 51.295                  |                         |                         |              |      |        |            |        |        |