## B. COMPUTER SCIENCE AND ENGINEERING 4th YEAR 1st SEMESTER 2019 OLD Formal Languages and Automata Theory (OLD)

Time: 3 hours Full Marks: 100

Answer any five questions

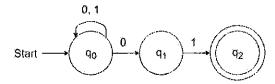
- 1(a) State the Pumping lemma for Regular languages.
- (b) Prove that  $\{0^n 1^n \mid n \ge 1\}$  is not regular.

6+14

- 2(a) Give a Regular Expression (RE) defining all binary strings that do not contain three or more consecutive 1's.
- (b) Prove that for every RE, there is an automaton that accepts the language defined by the RE.

10+10

- 3 (a) Give a DFA for  $\Sigma = \{0,1,2\}$  that accepts any string with 001 as a substring.
  - (b) Give the language accepted by the following NFA.



Construct a DFA equivalent to the NFA, shown above.

6+(4+10)

- 4. Let  $L_1$ ,  $L_2$  be two languages accepted by DFA's. Prove that the following languages are also accepted by DFA's:
- a) L<sub>1</sub>UL<sub>2</sub>
- b)  $L_1 \cap L_2$
- c)  $L_1 L_2$

20

- 5. Develop grammars that accept the following languages. Also give the necessary proof for each grammar.
- a) All strings over a,b that are not palindromes.
- b) All strings over a,b that contain same number of a's and b's.

10+10

6. Prove that for every Non Deterministic Push Down Automata (NPDA) accepting some language L by empty stack, there is an equivalent NPDA accepting the same language L by final states.