

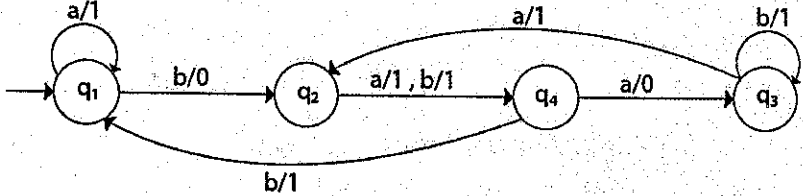
## B.E. INFORMATION TECHNOLOGY THIRD YEAR SECOND SEMESTER – 2019

(3<sup>rd</sup> Year; 2<sup>nd</sup> Semester)

Subject: Formal language &amp; Automata Theory

Time : Three hours

Full Marks: 100

CO1 [20]	<p>A. Find the regular expression of all non-negative integers without leading 0's. [3]</p> <p>B. Find the regular expression of the binary strings whose 1000th symbol from the end is '1'. [3]</p> <p>C. Differentiate recognizer (automata) and Transducers (FSM). [2]</p> <p>D. Attempt any two from the questions. 2x6=12</p> <ol style="list-style-type: none"> <li>Design a DFA M that accepts the language <math>L(M) = \{w \in \{a, b\}^* : w \text{ does not contain three consecutive } b\text{'s}\}</math>.</li> <li>Convert the following Mealy machine into Moore machine</li> </ol>  <ol style="list-style-type: none"> <li>If a DFA M accepts any string at all, it accepts one string whose length is less than the number of states in M. Prove it.</li> </ol>
CO2 [20]	<p>Attempt any two questions. 2x10=20</p> <p>A. Give pushdown automata (PDA) for the following language: <math>L = \{a^n b^m : n &lt; m \leq 2n\}</math></p> <p>B.</p> <ol style="list-style-type: none"> <li>Let 'L' be a GFL and the corresponding grammar 'G' is in CNF. From G, derive the necessary conditions of the pumping lemma for CFL.</li> <li>Prove that <math>L = \{a^p : p \text{ is a prime}\}</math> is not a CFL.</li> </ol> <p>C. Reduce the following grammar into CNF:  <math>S \rightarrow ASA \mid bA</math>  <math>A \rightarrow B \mid S</math>  <math>B \rightarrow c</math></p>
CO3 [20]	<p>Attempt any two questions. 2x10=20</p> <p>A. Design a Turing Machine which computes 2's complement of the given binary string.</p> <p>B. Design a Turing Machine over <math>\Sigma = \{a, b, c\}</math>, which accepts the language <math>\{wcw : w \in \{a, b\}^*\}</math>.</p> <p>C. Define TM with following variants:</p> <ol style="list-style-type: none"> <li>Storage in finite control</li> <li>Multiple track in the tape</li> <li>Multiple tape in TM</li> </ol>

CO4 [20]	<p>Attempt any four questions. <span style="float: right;">4x5=20</span></p> <p>A. Let <math>G=(V, \Sigma, P, S)</math>, where <math>V=\{a, b, S\}</math>, <math>\Sigma=\{a, b\}</math>, and <math>P=\{S \rightarrow aSb \mid aSa \mid bSa \mid bSb \mid \epsilon\}</math>. Show that <math>L(G)</math> is regular.</p> <p>B. Show that the grammar <math>G=(V, \Sigma, P, S)</math>, where <math>V=\{a, b, S, A\}</math>, <math>\Sigma=\{a, b\}</math>, and <math>P</math>:</p> $S \rightarrow AA$ $A \rightarrow AAA \mid a \mid bA \mid Ab$ $A \rightarrow bA$ <p>is an ambiguous grammar.</p> <p>C. Find the type of the following grammar and justify your answer.</p> $S \rightarrow ACaB$ $Bc \rightarrow acB$ $CB \rightarrow DB$ $aD \rightarrow Db$ <p>D. Let two languages <math>L_1</math> and <math>L_2</math> are of type-<math>i</math> (<math>i \in \{0, 1, 2, 3\}</math>). Prove that <math>L_1</math> and <math>L_2</math> are closed under concatenation.</p> <p>E. Define monotonic grammar with an example. Define yield of a parse tree with an example.</p>
CO5 [20]	<p>A. Show that diagonalization (or non-self-accepting) language is not recursively enumerable. <span style="float: right;">5</span></p> <p>B. Prove that universal language (<math>L_u</math>) is undecidable. <span style="float: right;">5</span></p> <p>Attempt any one form rest. <span style="float: right;">10</span></p> <p>C. State the complete sub graph problem (CSP) and then prove that CSP is NP complete.</p> <p>D. State the set cover problem and then prove that it is NP complete.</p>

CO1: Explain and construct Finite automata, Regular Languages and their properties. (K3)

CO2: Describe and construct Context Free Languages, Push Down Automata and their properties. (K3)

CO3: Explain and outline Turing Machine, its variants. (K4)

CO4: Classify and analyze different types of grammar and language. (K4)

CO5: Illustrate different decidable languages, unsolvable problems and complexity. (K3)