

9. A block of weight 50 N is placed on an inclined surface ($\mu = 0.3$). The block is released at the position as shown in Fig. 6 at a rest condition. What is the maximum compression of the spring? Take spring constant as 120 N/m.

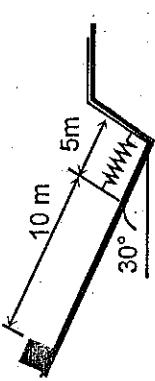


Fig. 6

10. The two flywheels are mounted on a common shaft which is supported by a journal bearing between them as shown in Fig. 7. Each flywheel has a mass of 40 kg, and the diameter of the shaft is 40 mm. If a 3-N·m couple M on the shaft is required to maintain rotation of the fly wheels and shaft at a constant low speed, compute:
 (i) the coefficient of friction in the bearing and
 (ii) the radius of the friction circle.

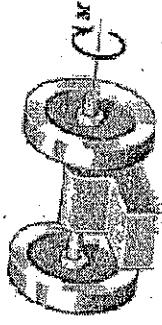


Fig. 7

Time : Three Hours. Full Marks : 100

Answer Part – A(compulsory) (10+30=40), any Two from Part – B (2x10=20), and any four from Part – C (4x10=40).
[40+20+40=100]

Answer as per instruction/choose the most appropriate option as the case may be:

1. (a) The unit of work or energy in S.I units is :
 (i) Newton, (ii) Pascal, (iii) Watt, (iv) Joule.
 - (b) Given $\varphi_1 = 5\hat{i} + 4\hat{k}$ and $\varphi_2 = 3\hat{i} + 6\hat{k}$. Find the magnitude of the scalar product of these two vectors.
 - (c) What is angle of friction?
 - (d) If a momentum of a body is doubled, its K.E will:
 (i) Increase by two times, (ii) increase by four times, (iii) Remains same, (iv) Get halved, (v) Reduce to four times.
 - (e) Two non-collinear parallel equal forces in opposite direction
 (i) balance each other, (ii) constitute a moment, (iii) constitute a couple, (iv) constitute a moment of couple, (v) constitute a resultant couple.
 - (f) State the condition of equilibrium for co-planar non-concurrent forces.
 - (g) A projectile is fired at an angle θ to the vertical. Its horizontal range will be minimum when θ is :
 (i) 0°, (ii) 30°, (iii) 45°, (iv) 60°, (v) 90°.
 - (h) Two equal forces of magnitude P are acting at an angle θ . Find out the resultant force.
- (i) Work done by all the forces is equal to change in:**
 (i) Potential Energy, (ii) Kinetic Energy, (iii) Power, (iv) Total mechanical energy, (v) None of these.
- (j) M.I. of a circular cylinder of radius R and mass M about its axis is:**
 (i) $(\pi/5)MR^2$, (ii) $(2/5)MR^2$, (iii) $(\pi/5)MR^3$, (iv) $(1/2)MR^2$

2. (a) The moment of a force about the origin is $x\hat{i} + y\hat{j} + z\hat{k}$ N.m. Find the moment about x-axis.

(b) Two springs of stiffness k_1 and k_2 are joined in series. Find stiffness of the system.

- (c) In a flat belt drive, tension in the slack side and initial tension are 80 N and 100 N respectively. Find the tension in the tight side.

- (d) A ladder AB of length L is supported by a horizontal floor at A and by a vertical wall at B and makes an angle with the horizontal as shown in Fig. 1.

Draw free body diagram of the ladder.

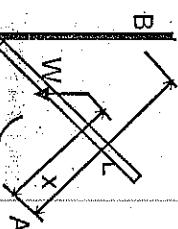


Fig. 1

- (e) State and prove Lami's theorem.

- (f) What is the momentum of a body of 2 kg at its highest point, when thrown with a velocity of 15 m/s at an angle of 70° with the horizontal?

- (g) Draw the graph of stress-strain for cast iron specimen indicating all types of stresses.

- (h) A man can throw a ball upto a maximum distance of 20 m on a horizontal plane. Find out the maximum height he can throw the ball?

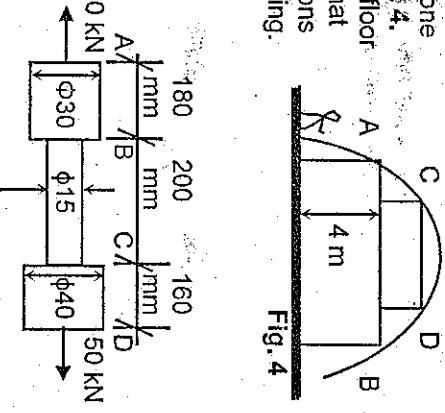
- (i) A particle moves from $t=0$ to $t \geq 3.5$ sec along a straight line such that its velocity is given by $v = (3t^2 - 6t)$ m/sec. Find the average velocity of the particle.

- (j) The position vector of a point at time 't' is $\vec{r} = a \cos \omega t \hat{i} + b \sin \omega t \hat{j}$

Find out the equation of its path.

Part – E (Any Two) (2x10=20)

8. A bar consists of three parts as shown, in the Fig. 5. Find the stresses in those parts and the total extension of the bar for an axial load of 50 kN. Take $E = 2 \times 10^5$ N/mm².



3. A force $\vec{F} = 6\hat{i} - 3\hat{j} - 2\hat{k}$ N acts at a point P(2, 3, 4). The coordinates being given in meters. Determine moment of this force about the point of origin.

4. Determine the range of values

which the mass m may have so that the 100 kg block shown in Fig. 2 will neither start moving up the plane nor slip down the plane. The coefficient of static friction for the contact surfaces is 0.3..

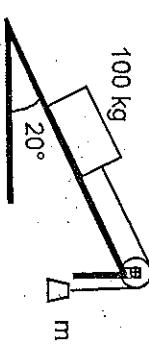


Fig. 2

5. A beam is subjected to forces as shown in Fig. 3. Find the magnitude, direction and the position of the resultant force.

Given: $\tan \theta = 1$, $\tan \alpha = \frac{3}{4}$

Fig. 3

Part – C (Any Four) (4x10=40)

6. A train enters bend of radius 500 m with a speed of 30 kmph and leaves the bend with a speed of 40 kmph during which it covers a distance of 200 m. Determine the total acceleration when it leaves the bend.

7. A boy standing on the ground throws a stone which crosses a building as shown in Fig. 4.

- It is found that the time taken to pass the floor AB in both directions is 2 sec, whereas that taken to cross the floor CD in both directions is 1 sec. Determine the height of the building.

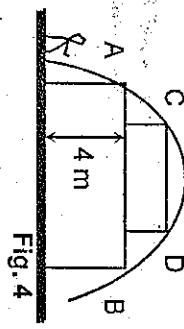


Fig. 4