

Assume the following properties of air and water unless otherwise specified:

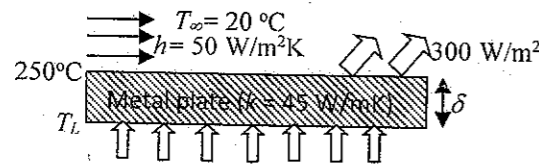
AIR:  $\rho = 1.16 \text{ kg m}^{-3}$ ,  $\nu = 1.86 \times 10^{-5} \text{ m}^2 \text{ s}^{-1}$ ,  $C_p = 1.014 \text{ kJ kg}^{-1} \text{ K}^{-1}$ ,  $Pr = 0.7$

WATER:  $\rho = 1000 \text{ kg m}^{-3}$ ,  $\nu = 1.0 \times 10^{-6} \text{ m}^2 \text{ s}^{-1}$ ,  $C_p = 4.186 \text{ kJ kg}^{-1} \text{ K}^{-1}$ ,  $Pr = 7.0$

**Part I (10 marks)**

1. Air at 20°C with a convection heat transfer coefficient of 25 W/m<sup>2</sup>K blows over a horizontal metal plate of  $k = 45 \text{ W/mK}$  to maintain the plate temperature at 250°C, while the plate continuously loses a radiative heat flux of 300 W/m<sup>2</sup> from the upper face. The plate has a thickness  $\delta = 2 \text{ cm}$  and area  $A = 0.4 \text{ m}^2$ . Calculate the steady operating temperature  $T_L$  of the lower surface and the heat flux from below.

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OR

A 3-m internal diameter spherical tank made of 2-cm-thick stainless steel ( $k = 15 \text{ W/m K}$ ) is used to store iced water at  $T_1 = 0^\circ\text{C}$ . The tank is housed in a room whose temperature is  $T_2 = 22^\circ\text{C}$ . Heat transfer between the outer surface of the tank and the surroundings is by natural convection only. The convection heat transfer coefficients at the inner and the outer surfaces of the tank are  $h_1 = 80 \text{ W/m}^2\text{K}$  and  $h_2 = 10 \text{ W/m}^2 \text{ K}$ , respectively. Determine the rate of heat transfer to the iced water in the tank. Also find the inner and outer surface temperatures of the tank.

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**Part II (Answer Q 2 and 3, total 30 marks)**

2. A 20 mm thick, infinitely spread, flat metal ( $k = 200 \text{ W m}^{-1} \text{ K}^{-1}$ ) plate carries electrical current so that it generates  $80 \text{ MWm}^{-3}$  of Joule heating (see Fig 2A). The left and right faces of the plates are maintained at 160 °C and 120 °C, respectively. (a) Starting from the energy equation, derive the expression for temperature distribution within the plate. Also evaluate (b) location and the value of maximum temperature within the plate and (c) the heat flux at the left and right faces of the plate.

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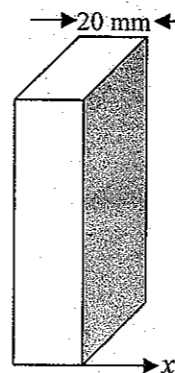


Fig 2A

OR

Glass wool insulation of thickness  $\delta$  is wrapped over the main steam pipeline of a power plant. The metal pipe has an outer radius  $R$  maintained at temperature  $T_R$ . The insulation fits tightly on the metal pipe and has an outer radius  $r$ , while its thermal conductivity is  $k$ . The outer surface of the insulation is exposed to an ambient of  $T_\infty$ . (a) Starting from the energy equation in cylindrical coordinates, deduce the expression of thermal resistance offered by a cylindrical insulation layer. (b) Do you think the thermal resistance increase with the insulation thickness  $\delta = (R - r)$  monotonically? (c) Deduce an expression of  $\delta$  for which the heat loss from the pipe will be maximum. What is it called?

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3. Define bulk mean temperature for a forced convection through a circular pipe. The velocity and temperature profiles inside a circular pipe, of radius  $R=10$  cm, vary as  $u=1$  m/s and  $T(r)=[400 - 1000(R-r)^2]$  K. Calculate the centerline and bulk mean temperature inside the pipe. Also calculate the Nusselt number for the flow. **10**

OR

State the summation and reciprocity rules of view factor. A hollow cylinder of height  $L$  and diameter  $D$  has three inner surfaces  $A_1$ ,  $A_2$  and  $A_3$ , respectively denoting the bottom, side (curved) and the upper surface, respectively. The view factor  $F_{12} = 2x[(1+x^2)^{1/2}-x]$ , where  $x=L/D$ . Find the value of  $F_{21}$  and  $F_{22}$  in terms of  $x$ . Refer to Fig 3B. **10**

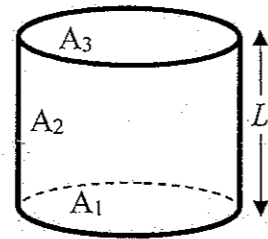


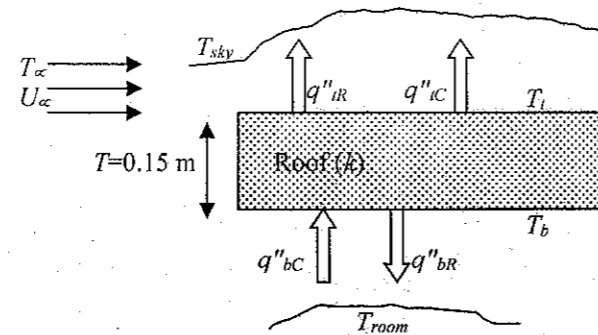
Fig 3B

Part III (Answer Q 4 and 5; 20×2 = 40 Marks)

4. In a boiler furnace, the hot flue gas, flowing out of the furnace region at a mean velocity of 10 m/s, temperature is measured by an R-type thermocouple inserted in the furnace space. What is the actual gas temperature if the thermocouple reads 1000 K? The bead of the thermocouple has a diameter of 800 micron, and the bead surface emissivity is 0.9. Consider the furnace walls to be blackbody at 700 K. Consider the expression for Nusselt number for forced flow over a sphere as  $Nu_D = 2 + (0.4Re_D^{0.5} + 0.06Re_D^{2/3})Pr^{0.4}$ . Also use the same fluid properties specified at the beginning of the question paper for the furnace gas. **20**

OR

The roof of a house consists of a 1.5 m × 1.5 m and 10 cm thick flat concrete slab ( $k=2.5$  W/mK). The convection heat transfer on the inner surface of the room is 4.5 W/m<sup>2</sup>. The ambient air is reported to be at 7°C, while the night sky temperature is at 100K. Interior of the house and the internal surfaces of the walls are maintained at a constant temperature of 27°C. The emissivity of both surfaces of the concrete roof is 0.9.



Considering both radiation and forced convection heat transfer, determine the rate of heat transfer through the roof, when the ambient air is blowing at 3.6 km/h blowing over the roof. For laminar flow,  $Nu_x=0.296 Re_x^{0.8} Pr^{1/3}$ . **20**

5. A heated metallic sphere of 8 cm diameter hung in a quiescent air of 27° C maintains surface temperature of 327° C. Assume the walls of room where the bulb is housed are also at 27°C and the surface of the sphere has a spectral hemispherical emissivity as  $\epsilon_\lambda = 0.3$  for  $\lambda \leq 4 \mu\text{m}$  and  $\epsilon_\lambda = 0.9$  for  $\lambda > 4 \mu\text{m}$ . Assume the correlation  $Nu_D = 2 + (0.589 Ra_D^{0.25}) / [1 + (0.469/Pr)^{9/16}]^{4/9}$  to hold for free convection over a sphere. Calculate the heat loss from the sphere, and the fraction lost by radiation. Use the blackbody radiation chart provided at the end of the question paper. **20**

Time: Three Hours

(Full Marks 100)

OR

A long cylindrical metal rod ( $k = 150 \text{ W/m K}$  and  $\alpha = 5 \times 10^{-5} \text{ m}^2/\text{s}$ ) is 10 cm in diameter and is initially at a uniform temperature of  $10^\circ\text{C}$ . It is exposed to hot gases at  $200^\circ\text{C}$  in a furnace when the gases blow over the cylinder at  $10 \text{ m/s}$  velocity. Assume the same air properties prescribed in the beginning of the question paper to represent the furnace gas, and the following expression of Nusselt number for cross-flow over a cylinder. How long it will be before the metal is heated to  $150^\circ\text{C}$ ?

$Nu = A Re^m Pr^{1/3}$ ; where  $A=0.95$  and  $m = 0.35$  for  $0 < Re < 50$ ;  $A=0.68$  and  $m = 0.46$  for  $50 < Re < 5000$ ;  $A=0.2$  and  $m = 0.62$  for  $5000 < Re < 50000$ .

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**Part IV (20 Marks)**

6. A hot surface at  $100^\circ\text{C}$  is to be cooled by attaching an array of 10 cm-long, 2mm-diameter metal pin fins ( $k = 200 \text{ W/m K}$ ) to it, with a center-to-center distance of 1 cm. The temperature of the surrounding medium is  $30^\circ\text{C}$ , and the heat transfer coefficient on the surfaces is  $200 \text{ W/m}^2\text{K}$ . Determine the rate of heat transfer from the surface for a  $1\text{-m} \times 1\text{-m}$  section of the plate. Also determine the overall effectiveness of the finned surface.

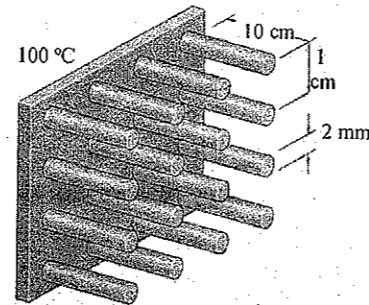


Fig 6A

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OR

Water ( $c_{pw} = 4.19 \text{ kJ/kg K}$ ) flowing at a rate of  $0.667 \text{ kg/s}$  enters a countercurrent, double-pipe heat exchanger at  $308\text{K}$  and is heated by an oil stream entering at  $383\text{K}$  at a rate of  $2.85 \text{ kg/s}$  ( $c_{po} = 1.89 \text{ kJ/kg K}$ ). The heat transfer coefficients on the outer and inner sides of the inner pipe are  $600 \text{ W/(m}^2\text{K)}$  and  $400 \text{ W/m}^2\text{K}$ , respectively, while the resistance due to fouling on the pipe is  $0.004 \text{ K.m}^2/\text{W}$ . Heat transfer area in the exchanger is  $15.0 \text{ m}^2$ . Calculate the heat-transfer rate and the exit water temperature. The effectiveness for a counterflow heat exchanger is

$$\epsilon = \frac{1 - \exp[-NTU(1 - C_r)]}{1 - C_r \exp[-NTU(1 - C_r)]} \quad (\text{for } C_r < 1); \quad \epsilon = \frac{NTU}{1 + NTU} \quad (\text{for } C_r = 1) \quad 20$$

**ADDITIONAL INFORMATION**

**Blackbody Radiation Function  $f_\lambda$**

| $\lambda T (\mu\text{m.K})$ | $f_\lambda$ | $\lambda T (\mu\text{m.K})$ | $f_\lambda$ |
|-----------------------------|-------------|-----------------------------|-------------|
| 200                         | 0           | 1600                        | 0.019718    |
| 400                         | 0           | 1800                        | 0.039341    |
| 600                         | 0           | 2000                        | 0.066728    |
| 800                         | 0.000016    | 2200                        | 0.100888    |
| 1000                        | 0.000321    | 2400                        | 0.140256    |
| 1200                        | 0.002134    | 2600                        | 0.18312     |
| 1400                        | 0.00779     | 2800                        | 0.227897    |