## BACHELOR OF ENGINEERING IN CHEMICAL ENGINEERING EXAMINATION, 2018

(1st Year, 2nd Semester)

## STRENGTH OF MATERIALS

Time: Three hours Full Marks: 100

## Answer any five questions

- 1. Answer the following questions-
  - a. Clearly state the assumptions made in deriving the following relations (symbols have their usual meanings)-

$$\tau_0 = \frac{Tr_0}{J}$$
 and  $\phi = \frac{TL}{GJ}$ . [5]

- b. The electric motor exerts a 500 N-m torque on the aluminum shaft ABCD when it is rotating at a constant speed. Clearly draw the FBD of each section. Knowing that G=27GPa and that the torques exerted on pulleys B and C are as shown, determine the angle of twist between (i) B and C, (ii) B and D.
  [5+5+5=15]
- 2. Answer the following questions
  - a. Derive the expression for critical load for a fixed-fixed column. [10]
  - b. Define slenderness ratio. Based on slenderness ratio how due classify columns into short, medium and long columns? What is the significance of this classification in relation to failure mode?
- Draw the shear force and bending moment diagrams for the beam configuration.
   Determine the location of point of contraflexure, if any.
- 4. A bar (E = 210 GPa) of length 1.2 m tapers uniformly from a diameter of 30 mm to 18 mm. Calculate its increase in length when subjected to a tensile force of 45 kN.

A rod of length 500 mm and diameter 25 mm is stretched by a tensile force of 10 kN at 20°C. What will be the ratio of the maximum normal and maximum shear stresses set up in the bar at 0°C, if  $\alpha = 1.2 \times 10^{-6}$ °C and E = 200 GPa?

Deduce, stating assumptions, an expression for the elongation of a close-coiled helical spring subjected to axial tensile force.

[Turn over

Consider the plane stress system shown in Fig. 5, where  $\sigma_x = 500$  MPa,  $\sigma_y = -300$  MPa and  $\tau_{xy} = 200$  MPa. Draw Mohr's circle, and mark the values of the principal stresses on the diagram. Also mention the planes on which they act.

6. Derive an expression of normal bending stress, mentioning assumptions.

A cantilever beam carries a uniformly distributed load of 10 kN/m over its entire span of 9 m. Find its maximum deflection if the flexural rigidity is  $1.5 \times 10^6$  kNm<sup>2</sup>. [to + to = 20]

7. Write short notes on any two of the following-

[10+10]

- a. By drawing the FBD of a general differential element of a beam and using equations of equilibrium show that  $\frac{dM(x)}{dx} = V(x)$  and  $\frac{dV(x)}{dx} = -w(x)$ , where symbols have their usual meaning.
- b. Mention a failure theory applicable for brittle materials. Using that theory and with the help of Mohr's circle explain the nature of the fractured surface of a piece of chalk under torsional loading.
- c. Explain the utility of Williot diagram with an example.
- d. Show that the maximum shearing stress in a bent beam with rectangular cross-section is 50% more than the average stress.

