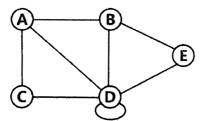
Bachelor Of Engineering In Information Technology 2nd Year 2nd Semester, Semester Examination, 2023 Subject Name –Graph Theory & Combinatorics (IT/PC/B/T/224)

Full Marks=100

CO1 Q1. (i) Find the adjacency matrix of the graph given below. Find out the number of paths of length 2 [10] from one vertex to others.



(ii) Find out the maximum and minimum number of edges in a 3-component graph having 10 vertices.

[5+5=10]

CO2 | Q2. (i) Does a Hamiltonian path or circuit exist on the graph below (Figure: 1)? Justify it.

[20] (ii) Prove with a suitable example "Every tree has either one or two centers".

(iii) Using Prim's algorithm find the minimal spanning tree of the graph given below (Figure: 2).

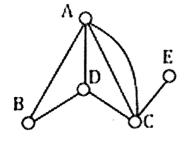


Figure: 1

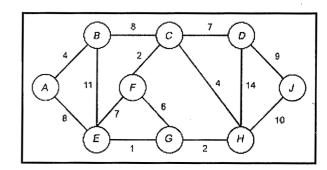


Figure: 2

[6+6+8=20]

- CO3 Q3. (i) Does a cut point and cut edges exist of the graph given below (Figure: 3)? If yes then mention [20] them.
 - (ii) Find the union of the two graphs G_1 and G_2 given below (Figure: 4).
 - (iii) Justify this using a suitable example "The vertex connectivity of any graph G can never exceed the edge connectivity of G".

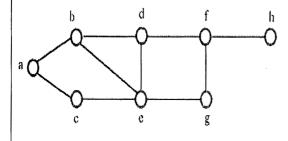
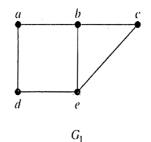
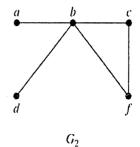


Figure: 3



-1

Figure: 4

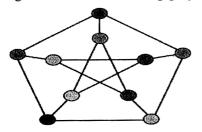


[7+7+6=20]

- CO4 Q4. (i) "A graph is 2-colorable if it is bipartite and every cycle has an even length." Justify this with a suitable example.
 - (ii) If a graph has 100 vertices and 300 edges, can it be planer?
 - (iii) Find the chromatic number of the graph given below (Figure: 5). (Mention all steps properly)

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(iv) Find out how many vertices can be matched using maximum matching in the bipartite graph algorithm of the following graph given below (Figure: 6)? Can we call it perfect matching? Justify this.



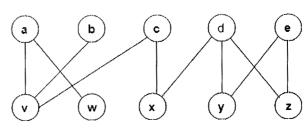


Figure: 5

Figure: 6

[6+3+4+(4+3)=20]

Q5. (i) How many cards must be selected from a standard deck of 52 cards to guarantee that at least three

hearts are selected??

- (ii) How many ways are there for **eight men** and **five women** to stand in a line so that **no two women** stand next to each other?
- (iii) Suppose a club has 25 members. How many ways are there to choose a **president**, **vice-president**, **secretary**, and **treasurer** of the club, where no person can hold more than one office?

[6+7+7=20]

CO6 O6.(i) Find the generating functions of the following sequences given below in closed form.

[10]

$$0, 1, -\frac{1}{2}, \frac{1}{3}, -\frac{1}{4}, \dots$$

(ii) Using generating functions, find an in terms of n for the case given below:

$$a_0 = 1$$
, $a_1 = 2$ and $a_{n+2} = 5a_{n+1} - 4a_n$ for $n \ge 0$

[5+5=10]

CO1: Explain and discuss the concept of different types of Graphs with fundamental properties and express different types of matrix representation. (K2)

CO2: Illustrate different types of trees such as (i) rooted tree (ii) spanning tree etc, and explain their properties. (K3)

CO3: Apply operations like Union, Deletion, and decomposition of graphs and illustrate Cut vertex and Cut edge and their properties. (K3)

CO4: Illustrate planar graph and their properties and Graph Coloring and Matching. (K3)

CO5: Apply and evaluate basic counting rules, pigeon-hole principle and principle of inclusion-exclusion. (K3)

CO6: Apply and Solve problems using Generating Function and Recurrence Relations. (K3)