

B.E.Tel.E. 2nd YEAR EXAMINATION, 2023  
(1<sup>st</sup> Semester)

**ELECTRO MAGNETIC THEORY**

Time: Three hours

Full Marks 100

No. of  
questions

Marks

Answer any *five* questions.

Consider  $\epsilon_0=8.854 \times 10^{-12}$  F/m and  $\mu_0=4\pi \times 10^{-7}$  H/m

Values of other universal physical constants may be assumed, if necessary.

- |       |  |    |
|-------|--|----|
| 1.(a) | Discuss the physical significance of “Divergence” operation.   | 8  |
| (b)   | Hence find an appropriate expression of the divergence of a vector in cylindrical coordinates.   | 12 |
| 2.(a) | Two point charges of equal mass $m$ and charge $Q$ are suspended from a common point by two threads of negligible mass and length $l$ . Find the inclination angle $\alpha$ with respect to the vertical made by each thread at equilibrium. Assume $\alpha$ to be very small.     | 8  |
| (b)   | Determine the electrostatic pressure on a conducting surface carrying a surface charge density $\rho_s$ suspended in a medium of permittivity $\epsilon$ .   | 12 |
| 3.(a) | A point charge $Q$ is located at the origin of spherical coordinate system. Calculate the electric flux crossing the portion of a spherical shell described by $\alpha \leq \theta \leq \beta$ .   | 10 |
| (b)   | Comment on the result obtained for $\alpha=0$ and $\beta=\pi/2$ .  | 2  |
| (c)   | A total charge of 40 nC is uniformly distributed on a circular disk. Determine the potential at a point $2m$ distant from the disk along its axis.   | 8  |
| 4.(a) | Consider a single turn rectangular coil in the $z=0$ plane carrying a current $I$ having dimensions $w$ and $l$ along $x$ and $y$ axes respectively. If a uniform magnetic field $B$ exists in the $+x$ direction, how much is the torque rotating the coil?                       | 10 |
| (b)   | Using the definition $\mathbf{B}=\nabla \times \mathbf{A}$ , derive an expression for magnetic vector potential from Biot Savart Law.  | 10 |
| 5.(a) | Assume that a material behaves as a good conductor if the displacement current through it is at least 10 times the conduction current. For sea water, $\epsilon_r=81$ and $\sigma=20$ S/m. What is the maximum frequency up to which sea water may be treated as a good conductor? | 4  |
| (b)   | For such good conductors, how do you evaluate the skin depth and the phase velocity?   | 8  |
| (c)   | Discuss the concept of surface impedance and its significance therein.   | 8  |
| 6.(a) | State and prove Poynting theorem.  | 6  |
| (b)   | Using it, determine the reflection coefficient at a dielectric-dielectric interface in terms of the material properties for both the cases of horizontal and vertical polarizations.   | 8  |
| (c)   | Hence discuss the phenomenon of total internal reflection.   | 4  |
| 7.(a) | For a current sheet $\mathbf{K}=9.0\mathbf{a}_y$ , A/m is located at $z=0$ , the interface between region 1 ( $z<0$ ) with $\mu_r=4$ and region 2 ( $z>0$ ) with $\mu_r=3$ . Given that $\mathbf{H}_2=14.5\mathbf{a}_x+8.0\mathbf{a}_z$ Am, find $\mathbf{H}_1$ .                  | 10 |
| (b)   | Prove that for uniform plane waves, the mode of propagation is always TEM.   | 10 |
| 8.(a) | What do you understand by retarded potential approach?   | 4  |
| (b)   | Elaborate its usage in determining the radiated fields from a time varying current source.   | 16 |