

BACHELOR OF ENGINEERING (ELECTRICAL ENGINEERING)
SECOND YEAR
FIRST SEMESTER
SUPPLEMENTARY EXAM 2023
FIELD THEORY

Time:3 hours

Full Marks:100

(50 marks for each part)

Use separate Answer-script for each part

PART-I

Answer any three questions. Two marks for neatness. All symbols have their usual significance

1. a) Derive the expression for curl of a vector field C , written as $\nabla \times C$ where ∇ is the vector differential operator in Cartesian coordinates. What is the physical significance of the $\nabla \times C$, curl of a vector field.

b) Establish the Stoke's theorem.

10+6=16

2. a) What is significance of $\nabla \cdot J = -\partial \rho / \partial t$, where ρ is volume charge density.

b) Establish $\nabla \cdot B = 0$.

c) Find the curl H at the origin, where $H = (2y)i - (x^2 + z^2)j + (3y)k$ A/m also what may be J here?

6+6+4=16

3. a) Establish $\nabla \times E = -\partial B / \partial t$ and show the pictorial view of this relation.

b) Establish $\nabla \times H = J + \partial D / \partial t$ and show the pictorial view of this relation.

What is displacement current?

8+8=16

4. a) Derive electromagnetic wave equations. Using E.M. wave equation in free space, obtain an analytical solution of the wave equation of Electric Field(E) considering it as a plane wave and also draw the wave propagation.

b) What do you mean by electromagnetic fields? Why do E.M. fields travel?

10+6=16

5. Write short notes on any two:

8+8=16

a) Boundary relation for magnetic field when it passes through two different magnetic media having permeabilities μ_1 and μ_2 .

b) "Poynting Theorem".

c) $\nabla \times H = J$ and its physical significance.