## Ref. No. : Ex/CE/PC/H/T/424/2023(S)

## Name of the Examinations: B.E. CIVIL ENGINEERING FOURTH YEAR SECOND SEMESTER SUPPLEMENTARY EXAM - 2023

## Subject : THEORY OF STRUCTURES Time : $\mathbf{3}$ hours Full Marks : 100 IV(HONS.)

Use separate answer script for each Part
PART I (50 Marks)

1. Define (i) Reynold's Number (ii) Weber Number
2. A ship 300 m long moves in sea water, whose density is $1030 \mathrm{~kg} / \mathrm{m}^{3}$. A $1: 100$ model of this ship is to be tested in a wind tunnel. The velocity of air in the wind tunnel around the model is $30 \mathrm{~m} / \mathrm{s}$ and the resistance of the model is 60 N . Determine the velocity of ship in sea water and also the resistance of ship in sea water. The density of air is given as $1.24 \mathrm{~kg} / \mathrm{m}^{3}$. Take the kinematic viscosity of sea water and air as 0.012 stokes and 0.018 stokes respectively. (15)
3. Develop the governing Matrix Finite Element equation (in local coordinate) using weak variational principle for the differential equation given below -

$$
-\frac{d^{2} u}{d x^{2}}-u+x^{3}=0 \text { for } 0<x<2
$$

with $u(0)=0$ and $u(2)=0$. Develop the necessary matrix equation for equally spaced two numbers of 2 -noded linear element and solve for ' $u$ ' at intermediate points.
4. (a) Write the properties of Lagrange interpolation function used in finite element model.
(b) Develop Lagrange Interpolation Functions for 4-node one dimensional element.

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Subject TmeORY OR STRUCTURES IV (MONS.) Tme: 3 hours Full Marks 100
PART-M (MARKSS-50)
Use a separate Answer-Script for each part

| No. of questions | Answer all questions | $\begin{gathered} \text { Marks } \\ 18+18+14=50 \end{gathered}$ |
| :---: | :---: | :---: |
| 1. | A simply supported rectangular plate subjected to sinusoidal loading distributed over the plate surface is given by the expression. $q=$ $\dot{q}_{0} \sin \frac{\pi x}{a} \sin \frac{\pi y}{b}$. ' $q_{0}$ ' is the intensity of loading at center of the plate. ' $a$ ' and ' $b$ ' are the length of and breath of the plate. Deduce the expressions for deflection ( $w$ ) and moments $\mathrm{M}_{\mathrm{x}}, \mathrm{M}_{\mathrm{y}}, \mathrm{M}_{x y}$. | $\begin{gathered} \mathrm{COH} \\ 18 \end{gathered}$ |
| $2 .$ | Show that the maximum deflection at the center of a simply supported rectangular plate subjected to a single concentrated load ' Q ' at center point is $w_{\max }=\frac{4 Q}{n^{4} a b D} \sum_{m=1}^{\infty} \sum_{n=1}^{\infty} \frac{1}{\left(\frac{m^{2}}{a^{2}}+\frac{n^{2}}{b^{2}}\right)^{2}}$ <br> Use Navier Solution. ' $a$ ' is the length of plate and " $b$ ' is the width of plate. D is the flexural rigidity. ' $m$ ' and ' $n$ ' are no. of terms. | $\begin{gathered} \mathrm{CO} \\ 18 \end{gathered}$ |
| 3. | Find the membrane forces in a cylindrical shell roof subjected to gravity load (self-weight) only. | $\begin{gathered} \mathrm{CO} 2 \\ 14 \end{gathered}$ |

