

B.E. CHEMICAL ENGINEERING SECOND YEAR FIRST SEMESTER EXAMINATION - 2023

SUBJECT: STRENGTH OF MATERIALS

Time: 3 Hours

Full Marks: 100 (10 × 10)

Any missing data may be assumed with suitable justification

The symbols/notations carry its usual meanings

For question Q9, the figure should be drawn in graph paper

ANSWER ANY TEN QUESTIONS

(All Questions Carry Equal marks)

Q1. A uniform and homogenous bar (Fig.Q1) is subjected to axial loading where $P_1 = 30$ kN, $P_2 = 20$ kN and $P_3 = 15$ kN. Find the distance x (in metres) where P_1 should be applied so that the net change in length of the bar is zero.

Q2. At room temperature (20° C), a 0.5-mm gap exists between the ends of the rods shown in Fig Q2. At a later time when the temperature has reached 140° C, determine (i) the normal stress in the aluminum rod, (ii) the change in length of the aluminum rod.

Q3. The aluminum rod BC ($G=26$ GPa) is bonded to the brass rod AB ($G=39$ GPa) (Fig. Q3). Knowing that each rod is solid and has a diameter of 12 mm, determine the angle of twist (i) at B, (ii) at C.

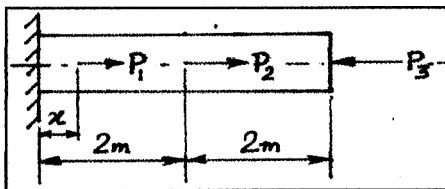


Fig. Q1

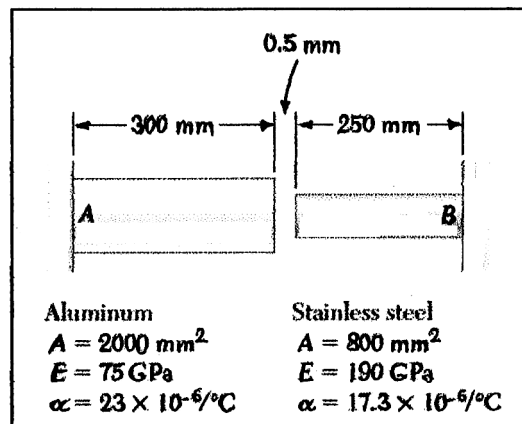


Fig. Q2

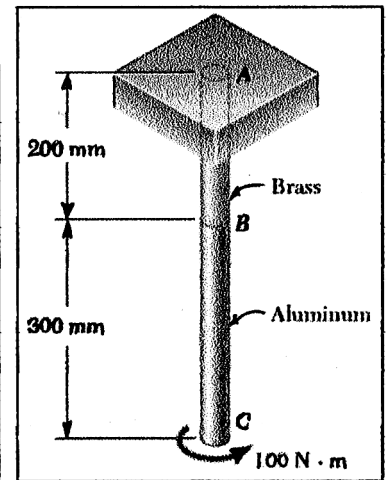


Fig. Q3

Q4. [6+4]

- (a) Deduce the expression of axial deflection for a close-coiled helical spring under the action of an axial load.
- (b) A close-coiled helical spring having 24 turns is made of 8 mm diameter wire. The mean diameter of the spring is 80 mm and it carries a load of 250 N. Determine the maximum shear stress developed, the deflection and the stiffness of the spring. Take $G = 84$ GPa.

[Turn over

Q5. For the beam loaded as shown in Fig. Q5, draw the complete shear force and bending moment diagrams by writing appropriate equations.

Q6. The beam shown in Fig. Q6 is made of a nylon for which the allowable stress is 24 MPa in tension and 30 MPa in compression. Determine the largest couple **M** that can be applied to the beam.

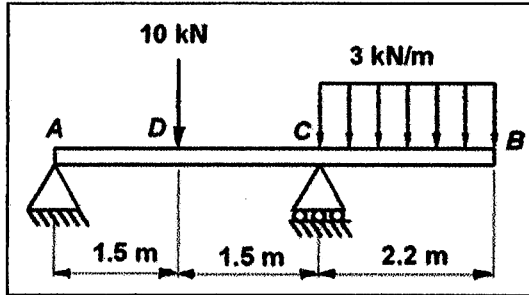


Fig. Q5

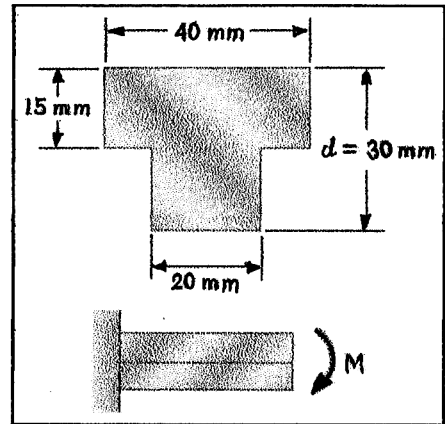


Fig. Q6

Q7. Stating the assumptions, derive the following relation for pure bending of a beam: $\frac{M}{I} = \frac{\sigma_x}{y} = \frac{E}{\rho}$

Q8. A cantilever beam carries a uniformly distributed load of intensity 10 kN/m over its entire span of 9 m. Deducing the necessary relation, find its maximum deflection if the flexural rigidity (EI) is 1.5×10^6 kN-m².

Q9. Draw the Mohr's circle on a graph paper for a state of plane stress defined by the following: $\sigma_x = 120$ MPa, $\sigma_y = 60$ MPa and $\tau_{xy} = -45$ MPa. Find the principal stresses and principal planes using Mohr's circle.

Q10. Drawing suitable neat sketches, derive the membrane stress equation for an axisymmetric thin-walled pressure vessel subjected to internal pressure.

Q11. Derive Euler's critical load for the fundamental mode of a fixed-pinned column of length L . Take $EI = \text{constant}$.

Q12. Answer any two:

[5 × 2 = 10]

(i) Write a short note on 'Bearing Stress'.

(ii) Establish the relation between bending moment and shear force in beams.

(iii) Prove that the maximum shear stress developed in a rectangular section beam is 1.5 times the average shear stress.