

## M. C. E. EXAMINATION, 2017

1<sup>st</sup> semester

## THEORY OF ELASTICITY AND ELASTIC STABILITY

Time 3 hours

Full marks 100

Use separate answer scripts for each part

## Part- I

Answer any Three questions. Each question carries 20 marks.

1. The stress-components relative to axes  $x_i$  are  $\sigma_{11} = 90$  MPa,  $\sigma_{22} = 60$  MPa,  $\sigma_{33} = 20$  MPa,  $\sigma_{12} = 20$  MPa,  $\sigma_{23} = 10$  MPa, and  $\sigma_{31} = 40$  MPa.

- (a) Determine the normal and shear components of stresses on a plane perpendicular to vector (1,3,1). Avoid using formula.  
 (b) Determine the principal stresses.

8+6+6=20

2. Deduce the tensor formula for transforming strain. What is a Jacobian matrix with relation to the expression of strain? What is the significance of the determinant of the Jacobian matrix?

10+8+2=20

3. Deduce the following relationships where the variables hold their usual meaning

$$(a) T_i^{(n)} = \sigma_{ij} n_j$$

$$(b) \sigma'_{ij} = a_{ip} a_{jq} \sigma_{pq}$$

10+10=20

4. Write notes on constitutive relationships of each kind of linear elastic materials.

20

M. Civil Engineering, 1<sup>st</sup> Semester , 2017

SUBJECT – Theory of Elasticity and Elastic Stability

Full Marks 100

Time: Three hours

(40 marks for this part)

Use a separate Answer-Script for each part

PART II

Answer ALL Questions

1. Use the energy approach to calculate the buckling load of a fixed-fixed column 6m long and with  $EI = 2000t\text{-m}^2$ . Obtain the buckling load also by finite difference dividing the total column height into four equal portions. Compare the results. 20
2. Calculate the buckling load of the truss shown below.  $AE = 8 \times 10^8\text{N}$ . 20

