

Answer Question number 1, and any **FOUR** from the rest

Assume the following properties of air and water unless otherwise specified:

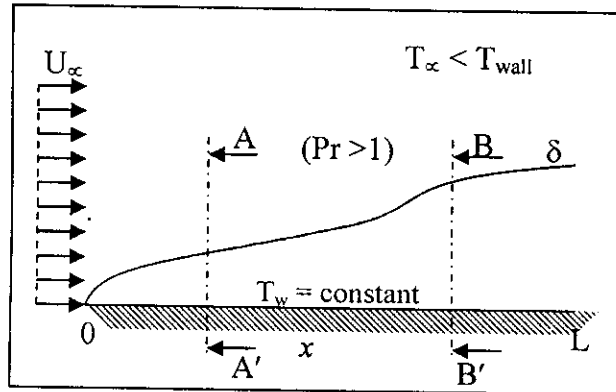
AIR: $\rho = 1.16 \text{ kg m}^{-3}$, $\nu = 1.86 \times 10^{-5} \text{ m}^2 \text{ s}^{-1}$, $C_p = 1.014 \text{ kJ kg}^{-1} \text{ K}^{-1}$, $Pr = 0.7$

WATER: $\rho = 1000 \text{ kg m}^{-3}$, $\nu = 1.0 \times 10^{-6} \text{ m}^2 \text{ s}^{-1}$, $C_p = 4.186 \text{ kJ kg}^{-1} \text{ K}^{-1}$, $Pr = 7.0$

A few useful heat transfer correlations are provided in Table 1 (last page)

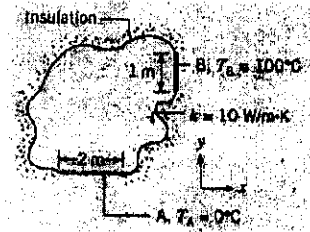
1. **Answer Any Four**

- i. What do you mean by *Thermally Fully Developed* (TFD) flow in a pipe? For turbulent flow, what is the L/D ratio beyond which the TFD persists in case of turbulent flow? 5
- ii. From the following sketch, draw a neat sketch of the thermal boundary layer and the $h(x)$ and $\bar{h}(x)$ profiles. Also draw the temperature and velocity profile across the section AA' and BB'. 5



- iii. A copper sphere of diameter D is hung in a quiescent air in zero gravity condition. Estimate the Nusselts number without the help of Table 1. Neglect radiation. 5

- iv. In the two-dimensional body illustrated in the figure, the temperature gradient at A is found to be $\partial T / \partial y = +30 \text{ K/m}$. What are the $\partial T / \partial x$ and $\partial T / \partial y$ at surface B? 5



- v. What do you mean by critical radius of insulation? Deduce the expression for critical radius of insulation for a cylindrical geometry 5
- vi. Velocity and temperature profiles for laminar flow in a tube of radius $R = 10 \text{ mm}$ has the forms: $u(r) = 0.5 \text{ m/s}$ and $T(r) = 350 + 80(r/R)^2 - 24(r/R)^4 \text{ K}$, respectively. Determine the corresponding value of the bulk mean temperature and Nu . 5

- 2. In a boiler furnace, the hot flue gas (consider thermophysical properties are same as those of air), flowing out of the furnace region at a mean velocity of 10 m/s , temperature is measured by an R-type thermocouple inserted in the furnace space. What is the actual gas temperature if the thermocouple reads 1000 K ? The bead of the thermocouple has a diameter of 800 micron , and the bead surface emissivity is 0.9 . Consider the furnace walls to be blackbody at 700 K . 20

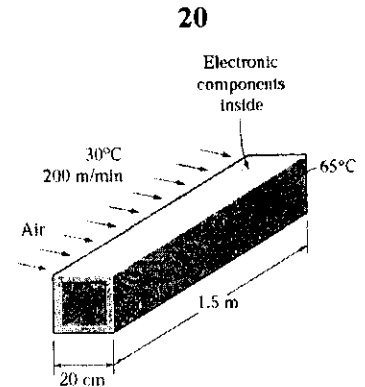
Time: Three Hours

(Full Marks 100)

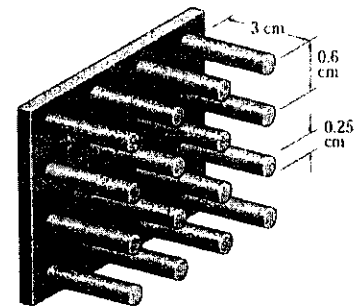
3. A hollow cylinder with inner radius of a and outer radius of b is heated at the inner surface at a rate of q_0 W/m² and it dissipates heat by convection from the outer surface into a fluid at temperature T_∞ with a heat transfer coefficient h . There is no energy generation, and the thermal conductivity of the solid is assumed to be constant. Develop an expression for the determination of the temperatures T_1 and T_2 of the inner and outer surfaces of the cylinder. Also, calculate the temperatures T_1 and T_2 for $a = 3$ cm, $b = 5$ cm, $h = 400$ W/m²K, $T_\infty = 100$ °C, $k = 15$ W/mK, and $q_0 = 10^5$ W/m².

4. The components of an electronic system are located in a 1.5-m-long horizontal duct whose cross section is 20 cm × 20 cm. The components in the duct are cooled by air at 30°C flowing over the duct with a velocity of 200 m/min. If the surface temperature of the duct is not to exceed 65°C, determine the total power rating of the electronic devices that can be mounted into the duct. For cross flow over a cylinder or rectangular parallelepiped, the Nu correlation is:

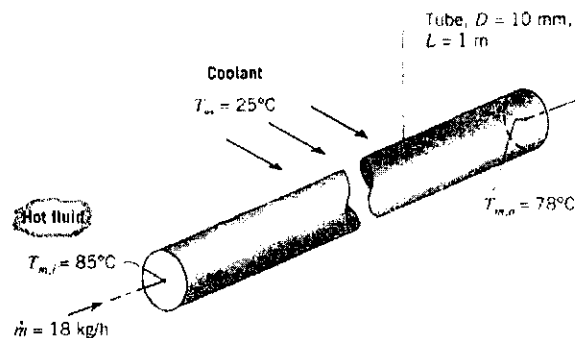
$$\overline{Nu}_D = 0.3 + \frac{0.62 Re_D^{1/2} Pr^{1/3}}{\left[1 + (0.4/Pr)^{1/4}\right]^{1/4}} \left[1 + \left(\frac{Re_D}{282000}\right)^{5/8}\right]^{4/5} \quad 20$$



5. A hot surface at 100 °C is to be cooled by attaching an array of 17 cm-long, 0.25-cm-diameter aluminum pin fins ($k = 237$ W/m K) to it, with a center-to-center distance of 0.6 cm. The temperature of the surrounding medium is 30 °C, and the heat transfer coefficient on the surfaces is 35 W/m² K. Determine the rate of heat transfer from the surface for a 1-m × 1-m section of the plate. Also determine the overall effectiveness of the finned surface.



6. A hot fluid passes through a thin-walled tube of 10 mm diameter and 1 m length, and a coolant at $T_\infty = 25$ °C is in cross flow over the tube (see Fig. below). When the flow rate through the tube is 18 kg/h and the inlet and outlet bulk mean temperatures are $T_{m,i} = 85$ °C and $T_{m,o} = 78$ °C, respectively. Assuming hydrodynamic and thermally fully developed flow within the tube, determine the heat transfer coefficient outside the tube. The thermophysical properties of the hot fluid are $\rho = 1079$ kg/m³, $c_p = 2637$ J/kgK, $\mu = 0.0034$ N.s/m², and $k = 0.261$ W/mK.



Time: Three Hours

(Full Marks 100)

7. Water ($c_{pw}=4.18$ kJ/(kg.K) flowing at a rate of 0.667 kg/s enters a countercurrent, double-pipe heat exchanger at 308K and is heated by an oil stream entering at 383K at a rate of 2.85 kg/s ($c_{po}=1.89$ kJ/kg.K). The overall heat transfer coefficient of the heat exchanger is 300 W/(m².K) and the heat transfer area in the exchanger is 15 m². Calculate the heat-transfer rate and the exit fluid temperatures. **20**
8. An electrically heated vertical plate 0.3 m high and 1 m wide is maintained at a uniform temperature of 124 °C in quiescent atmospheric air of 30 °C in a blackbody enclosure that is also maintained at 30 °C. The plate has an emissivity of 0.9. Calculate the rate of heat loss from the plate due to radiation and free convection, if the plate loses heat from both sides. **20**

Table 1: Heat transfer correlations

Nu Correlations	(Geometry)	Condition	
		Flow, Temp.	Property
$Nu_x = 0.332 Re_x^{1/2} Pr^{1/3}$	(Flat Plate)	Laminar, forced convection, T_w	$0.6 \leq Pr \leq 50$
$Nu_x = 0.75 Re_x^{1/2} Pr^{1/2}$	(Flat Plate)	Laminar, forced convection q''	$Pr \ll 1$
$Nu_x = 0.0296 Re_x^{0.8} Pr^{1/3}$	(Flat Plate)	Turbulent, forced convection $5.0 \times 10^5 \leq Re \leq 10^8$, T_w	$0.6 \leq Pr \leq 60$
$\overline{Nu_D} = 0.3 + \frac{0.62 Re_D^{1/2} Pr^{1/3}}{[1 + (0.4/Pr)^{1/4}]^{1/4}} \left[1 + \left(\frac{Re_D}{282000} \right)^{5/8} \right]^{4/5}$	(Cross flow over Cylinder)	All $Re_D, Pr > 0.2$	
$\overline{Nu_D} = 2 + (0.4 Re_D^{0.5} + 0.06 Re_D^{2/3}) Pr^{0.4} (\mu/\mu_s)^{0.25}$	(Cross flow over Sphere)	$3.5 < Re_D < 7.6 \times 10^4$	$0.71 < Pr < 380$, $1 < \mu/\mu_s < 3.2^*$
$Nu_L = \left\{ 0.825 + \frac{0.387 Ra_L^{1/4}}{[1 + (0.492/Pr)^{9/16}]^{8/27}} \right\}^2$	(flat plate)	Free convection for all Ra_L	
$\overline{Nu_D} = 2 + 0.6 Re_D^{1/2} Pr^{1/3} D$		Falling droplet	

* Fluid properties are evaluated at T_∞

$$\epsilon_{PARALLEL} = \frac{1 - \exp[-NTU(1+C_r)]}{1+C_r}$$

$$\epsilon_{COUNTER} = \frac{1 - \exp[-NTU(1+C_r)]}{1 - C_r \exp[-NTU(1-C_r)]} \quad (C_r < 1)$$

$$= \frac{NTU}{1+NTU} \quad C_r = 1$$