

ENGINEERING MECHANICS

FULL MARKS 100

DURATION 3 HRS.

Answer any five questions with no more than three from each group. Marks are equally distributed (if not mentioned otherwise) among the parts (if any) of a given question. Assume reasonable values for any missing data.

Group A

1. Answer the following questions-

- a. For the given force moment system acting on the plate, determine the position at which the line of action intersects with the y axis.
- b. The cable exerts a tension of $T = 2\text{ kN}$ on the fixed bracket A . Determine-
 - i. The vector expression for the tension T .
 - ii. The moment developed at the support O due to the tension.

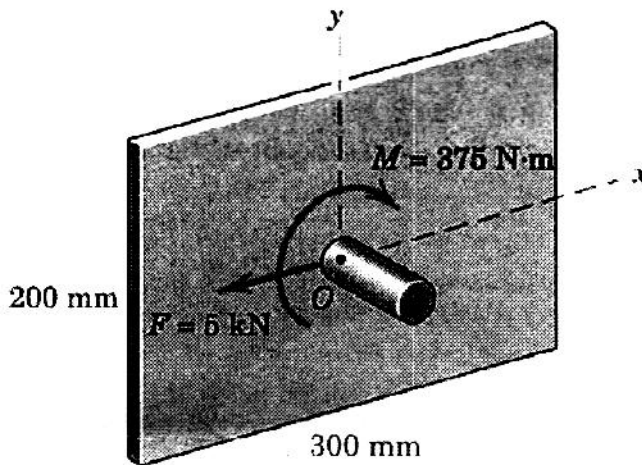


Figure (1a)

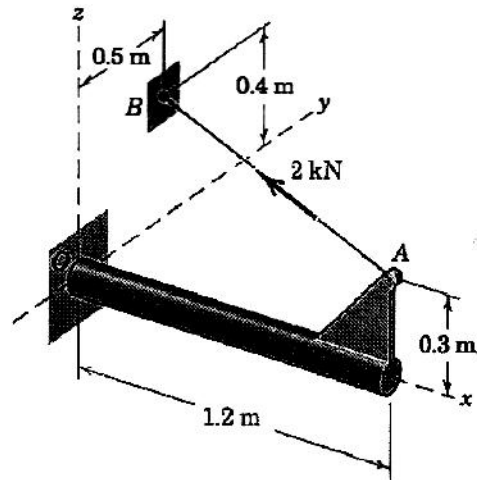


Figure (1b)

[Turn over

2. Each of the three uniform 1200-mm bars has a mass of 20 kg. The bars are welded together into the configuration shown and suspended by three vertical wires. Bars AB and BC lie in the horizontal $x - y$ plane, and the third bar lies in a plane parallel to the $x - z$ plane. Compute the tension in each wire.

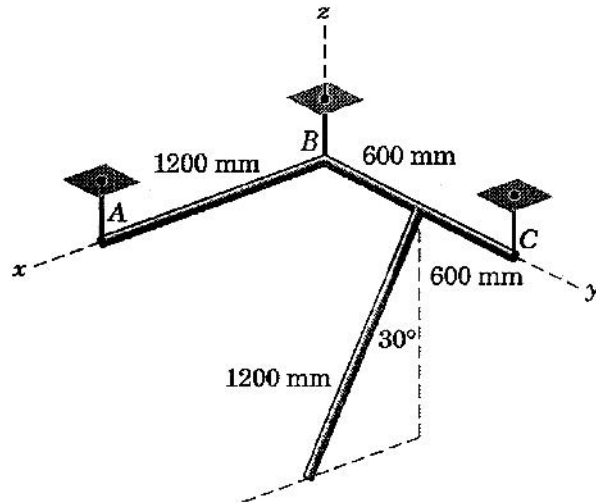


Figure (2)

3. Answer the following questions-
- The top of the folding workbench has a mass of 50 kg with mass center at G . Calculate the $x -$ and y -components of the force supported by the pin at E .
 - For the shaded area-
 - Determine the *volume of revolution* about x axis using the concept of a compound geometry.
 - Apply Pappus theorem on the above result to determine the centroid of the shaded area.

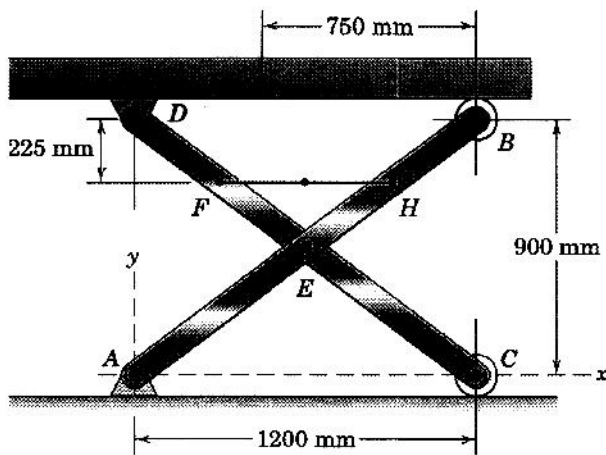


Figure (3a)

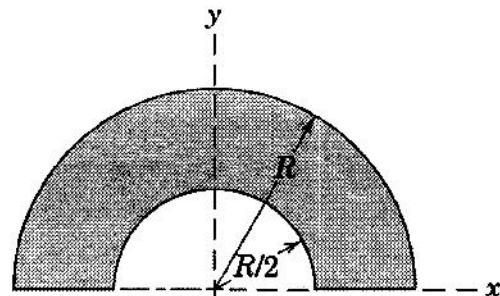


Figure (3b)

4. Answer the following questions-

- a. Determine the range of weights W of the uniform slender bar for which the system will be in equilibrium. Neglect friction at all bearings. Given, $L = 1\text{m}$.
- b. The moments of inertia of the area A about the parallel p - and p' -axes differ by $15 \times 10^6 \text{mm}^4$. Compute the area A , which has its centroid at C .

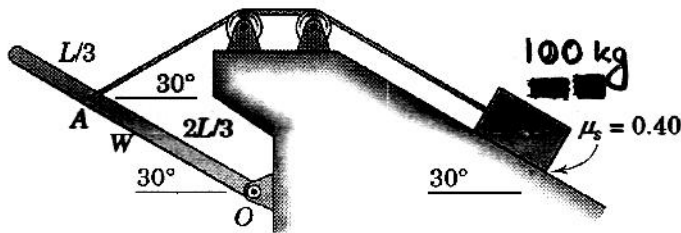


Figure (4a)

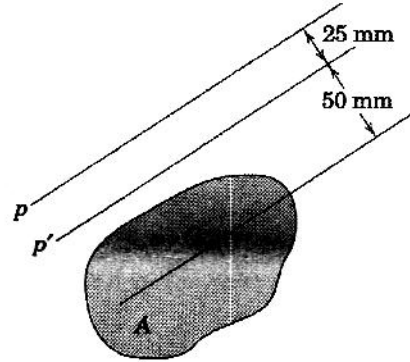


Figure (4b)

Group B

5. Answer the following questions-

- a. The acceleration of a point A is defined by the relation $a = 600x(1 + kx^2)$, where a and x are expressed in m/s^2 and m , respectively, and k is a constant. Knowing that the velocity of A is 7.5 m/s when $x = 0$ and 15 m/s when $x = 0.45 \text{ m}$, determine the value of k . [8]
- b. The pilot of an airplane pulls into a steep 45° climb at 300 km/h and releases a package at position A as shown in Fig. 5b. Calculate the horizontal distance s and the corresponding time t from the point of release to the point at which the package strikes the ground. [12]

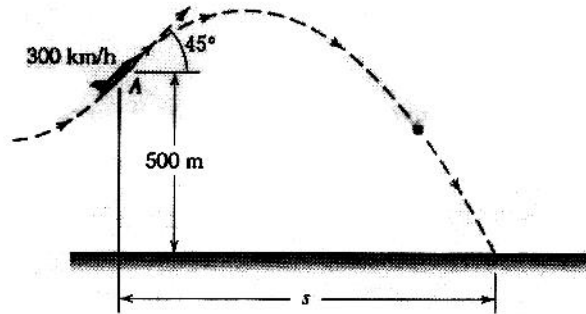


Figure (5b)

6. Answer the following questions-

- a. The rotation of the **0.9 m** arm OA about O (as shown in **Fig. 6a**) is defined by $\theta = 0.15t^2$ where θ is in radian and t in second. Collar B slides along the arm such that $r = 0.9 - 0.12t^2$ where r is in meter. After the arm has been rotated through 30° , determine radial and transverse ($r-\theta$) components of velocity and acceleration of the collar. Also find out the angle made by the velocity vector and the acceleration vector of the collar with the arm OA at this instant of time. [10]
- b. In **Fig. 6b**, the block C starts from rest and moves downward with a constant acceleration. Knowing that after **12 s** the velocity of block A is **456 mm/s**, determine the accelerations of A , B , and C . [10]

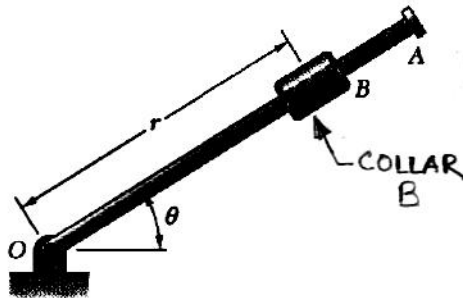


Figure (6a)

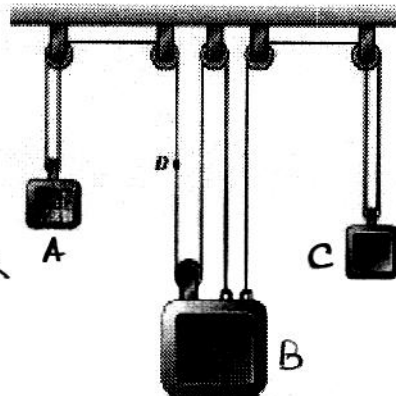
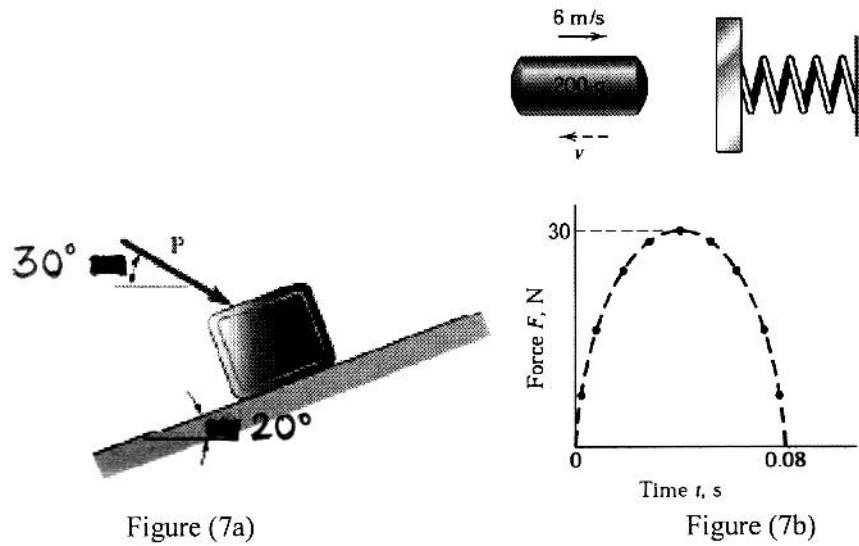


Figure (6b)

7. Answer the following questions-

- a. A **40-kg** package is at rest on an incline when a force P is applied to it (**Fig. 7a**). Determine the magnitude of P to initiate the motion in upward direction. Also determine the magnitude of P necessary if **4 s** is required for the package to travel **10 m** up the incline. The static and kinetic coefficients of friction between the package and the incline are **0.30** and **0.25**, respectively. Draw the necessary free-body diagram. [12]
- b. A **200-g (0.2-kg)** bullet initially travelling at **6 m/s** to the right strikes the still plate supported by a spring. The bullet remains in contact with the plate for **0.08 s**, during which a force of resistance (F) has been applied on the bullet which varies with time according to a function approximated by the upper half of an ellipse as shown in **Fig. 7b**. Find out the speed v at which the bullet will return to the left just after the contact has been cease. [8]



8. Write short notes on-
- Centroid of a 3D curvilinear segment.
 - Moment of a couple.
 - Expressions of velocity and acceleration in $r - \theta$ coordinate system.
 - Work-energy principle for particle dynamics.