

B.CHEMICAL ENGINEERING 3 RD YEAR 2 ND SEMESTER EXAMINATION, 2017

OPTIMIZATION METHODS IN CHEMICAL ENGINEERING

ANSWER ANY FOUR QUESTIONS

ASSUME MISSING DATA, IF ANY

FULL MARKS: 100

TIME: 3 HOURS

REFERENCE: EX/CHE/T/325/2017

1. Use the Lagrangian method to solve the following problem

$$\text{Minimize } Z = 4x_1 + 6x_2 - 2x_1^2 - 2x_1x_2 - 2x_2^2$$

$$\text{subject To } x_1 + x_2 = 2$$

$$\text{and } x_1, x_2 \geq 0$$

2. Use the Kuhn Tucker conditions to solve the following non-linear programming problem

$$\text{Maximize } Z = 2x_1 + x_1^2 + x_2$$

$$\text{subject To } 2x_1 + 3x_2 \leq 6$$

$$2x_1 + x_2 \leq 4$$

$$\text{and } x_1, x_2 \geq 0$$

3. Use Wolfe's Modified Simplex algorithm for solving the following quadratic programming problem

$$\text{Minimize } Z = 6 - 6x_1 + x_1^2 - 2x_1x_2 + 2x_2^2$$

$$\text{subject To } x_1 + x_2 \leq 2$$

$$\text{and } x_1, x_2 \geq 0$$

4. Minimize $f(x) = x(x - 1.5)$ in the interval (0.0, 1.0) by Fibonacci method. Use $n = 6$. Solve for two iterations only.

$$5. \text{ Minimize } f(x_1, x_2) = x_1 - x_2 + 2x_1^2 + 2x_1x_2 + x_2^2$$

Starting from $X_1^T = [0 \ 0]$ using Steepest Descent method. Solve for two iterations only.

6. Using Simplex algorithm solve the following linear programming problem

$$\text{Minimize } Z = x_1 + 4x_2 + 5x_3$$

subject To $3x_1 + \quad + 3x_3 \leq 22$

$$x_1 + 2x_2 + 3x_3 \leq 14$$

$$3x_1 + 2x_2 \leq 14$$

and $x_1, x_2, x_3 \geq 0$