## M.E. MECHANICAL ENGINEERING FIRST YEAR SECOND SEMESTER EXAM., 2019

## FINITE ELEMENT ANALYSIS IN ENGINEERING

Time: Three hours Full Marks: 100

Answer any five questions. All questions carry equal marks.

1: Consider a beam element having two degrees of freedom comprising deflection and rotation. The elements of the element stiffness matrix are given as (EI/ $^3$ )  $K_{ij}$  where  $K_{11} = 12$ ,  $K_{22} = 4$ ,  $K_{33} = 12$ ,  $K_{44} = 4$ ,  $K_{21} = K_{41} = 6$ ,  $K_{31} = -12$ ,  $K_{32} = K_{43} = -6$  and  $K_{42} = 2$ . The notations have their usual meanings. Using FEM determine the deflection at the mid-span of a fixed-fixed beam subjected to a uniformly distributed load of intensity p. The kinematically consistent element load vector is given as

$$\{Q\} = (pl/12)[6 \ 1 \ 6 \ -1]^T$$

- For a constant strain triangle (CST) finite element express the shape functions in terms of natural coordinates. Show that elements of the straindisplacement matrix of a CST finite element with isoparametric formulation are constants.
- (a) For a four-node isoparametric quadrilateral element derive the Jacobian matrix [J]. The element is having two degrees of freedom per node and the shape functions in terms of natural coordinates ξ, η are expressed as N<sub>i</sub> = 1/4 (1+ ξ,ξ<sub>i</sub>)(1+ η η<sub>i</sub>).

- (b) For a nine-node quadrilateral element determine the shape functions using the product rule.
- 4. Discuss the assumptions adopted in Kirchhoff Theory for bending of flat plates. Express the strain-displacement and moment curvature relations according to Kirchhoff Theory. Discuss the procedure for deriving the element stiffness matrix of a Mindlin plate element.
- 5. Determine the weight factor and the location of the sampling points for two-point Gauss quadrature. With suitable diagrams show the relevant parameters of an axially symmetric finite element of rectangular cross-section. Also derive the strain-displacement matrix [B] for this element.
- 6. (a) Express the displacements and nodal coordinates of an eight-node isoparametric degenerated solid shell element with suitable diagrams and reasons. What should be the orders of Jacobian matrix [J] and strain-displacement matrix [B] for this element?
  - (b) Discuss about the skyline storage scheme, mesh convergence, standard eigen value problem and generalized eigen value problem. Distinguish between lumped mass and consistent mass matrix formulations.