

Master of Arts Examination 2017
(2nd year 3rd semester)
Economics
Operations Research

Time: 2 Hours

Full Marks: 30

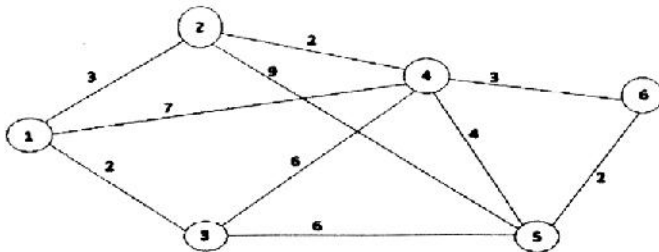
Answer any three questions: 3X10

- 1) Describe how the order size is determined in EOQ model with finite replenishment rate when the shortages are allowed.
- 2) For multiple item inventory, following information are provided

Item	Cost price(Rs)	demand
1	30	3000
2	20	2000
3	25	4000

The order cost is Rs 10 and carrying cost is 15%,

- a) What is the optimal ordering policy? 4
 - b) If the total order size has to be kept at a level 60 orders per year, what should be the total cost for optimal policy? 4
 - c) How much higher it is from the actual optimal total cost? 2
- 3) Find the shortest distance to node 3 from all other nodes from the following diagram. 2



- 4) Answer any 4 question: 4 x 2.5
 - a) Give the definition of Inventory. When an inventory problem called a static problem?
 - b) Find the nearest neighbours for the nodes 1, 2, 3, 5 and 6 from the diagram at question 3.
 - c) What are tree and spanning tree in a network?
 - d) Define path and directed path for a network.
 - e) Differentiate between ergodic and regular Markov chains.
 - f) Given the one-step transition probability matrix

[Turn over

$$P = \begin{array}{c|ccccc|c} & \text{A} & \text{B} & \text{C} & \text{D} & \text{E} & \\ \hline \text{A} & 0.3 & 0 & 0.2 & 0.1 & 0.4 & \text{A} \\ \text{B} & 0.1 & 0.2 & 0 & 0.6 & 0.1 & \text{B} \\ \text{C} & 0.3 & 0 & 0.5 & 0.1 & 0.1 & \text{C} \\ \text{D} & 0 & 0.1 & 0.3 & 0.2 & 0.4 & \text{D} \\ \text{E} & 0 & 0.2 & 0 & 0 & 0.8 & \text{E} \\ \hline \end{array}$$

Find out the probability that the process starting from state A attend the state E after two moves and state B after three moves.

5) If, for a Markov chain, the one-step transition probability matrix is given as:

$$P = \begin{array}{c|ccccc|c} & \text{A} & \text{B} & \text{C} & \text{D} & \text{E} & \\ \hline \text{A} & 0.4 & 0 & 0.2 & 0 & 0.4 & \text{A} \\ \text{B} & 0 & 1 & 0 & 0 & 0 & \text{B} \\ \text{C} & 0.3 & 0 & 0.2 & 0.1 & 0.4 & \text{C} \\ \text{D} & 0 & 0 & 0 & 1 & 0 & \text{D} \\ \text{E} & 0 & 0 & 0 & 0 & 1 & \text{E} \\ \hline \end{array}$$

- Find whether the chain is absorbing or not. 1
- Enumerate the transient states. 1
- Represent the chain with weighted digraph. 3
- Get the time to absorption if the chain absorbing and starts from state A or from state C. 2
- If the chain absorbing get the absorption probabilities from state A to state E and state C to state B. 3