BACHELOR OF ARTS EXAMINATION, 2017

## ( $3^{\text {RD }}$ Year, $5^{\text {th }}$ Semester) <br> ECONOMICS (HONOURS) <br> APPLIED ECONOMICS

Time: 2 hours

## Group: A

Full Marks:30
$3 \times 5=15$
a. How is Gini Coefficient affected if we add Rs. $\theta$ to everybody in the following income distribution comprising three individuals? Incomes (earned per day) of the three individuals (A, B \&C) are Rs. 100, 200 and 300 respectively.
b. Using simple random sampling at 8 B Bus-stand, Jadavpur, the relationship between disease (viz. acute respiratory problem) and exposure to air-pollution is displayed in the following contingency Table. Do these data suggest an association between disease and exposure (to pollution)?

| Exposure <br> (to pollution) | Disease |  |  |
| :--- | :---: | :---: | :--- |
|  | Yes | No |  |
|  | 37 | 13 | 50 |
| Yes | 17 | 53 | 70 |
| No | 54 | 66 | 120 |
| Total |  |  |  |

Production of rice (per acre) varies due to variations of seeds and use of different fertilizers. The following table shows the production of rice per acre (in metric tonnes):

| Varieties of fertilizers | Varieties of seeds |  |  |
| :--- | :--- | :--- | :--- |
|  | $\mathbf{A}$ | $\mathbf{B}$ | $\mathbf{C}$ |
| $\mathbf{W}$ | 6 | 5 | 5 |
| $\mathbf{X}$ | 7 | 5 | 4 |
| $\mathbf{Y}$ | 3 | 3 | 3 |
| $\mathbf{Z}$ | 8 | 7 | 4 |

Set up an Analysis of Variance table following Two Way Designs. How does production of rice vary due to variations of fertilizers or seeds or both? You need not to apply Fisher's or Scheffe's test of Critical Difference for intra-variability of Seeds/Fertilizers.

A random survey was conducted in an Engineering College in order to find out the determinants of drug addiction among the 3rd year students; survey findings reveal that 14
out of 30 students are found to be drug addicted. The following Logistic Regression result is found:

Number of observations $=30$, LR Chi Sq. (3) $=26.27(P=0.0000)$, Log Likelihood $=-7.05$
Pseudo $R^{2}=0.65$
Logit $=\ln \frac{P_{i}}{1-P_{i}}=8.852+4.95 X_{1}-0.810 X_{2}-0.271 X_{3}$
Given that, $\mathrm{P}_{\mathrm{i}}=\mathrm{E}\left(\mathrm{Y}=1 \mid \mathrm{X}_{\mathrm{i}}\right), \mathrm{Y}_{\mathrm{i}}=1$, if the student is drug addicted, 0 otherwise; $\mathrm{X}_{1}=1$, if the student studied in co-ed school at ( $10+2$ ) level, 0 otherwise; $X_{2}=$ time spent by mother (of student) in household chores per day; $X_{3}=$ time spent by the father (of student) in household per day. All the regression coefficients are statistically significant except variable $\mathrm{X}_{3}$. Mean of $X_{1}, X_{2}$ and $X_{3}$ are $0.466,14.2$ and 8 respectively. Given this information, answer the following:
a. Interprete the logit coefficients, (b) find the odd ratio of $X_{2}$ and (c) find the mean predicted probability of $\mathrm{P}(\mathrm{Y}=1 \mid \mathrm{X})$ from the above results and estimate the marginal effect of $X_{2}$.
[2+1+2]
4. a. Consider the following CES type production function:
$Y=\gamma\left[\sigma L^{-\rho}+(1-\sigma) K^{-\rho}\right]^{-1 / \rho}$ where, $Y=$ output, $\gamma=$ technological parameter, $\sigma$ stands for distribution parameter $(0<\sigma<1)$ and $\rho$ be the substitution parameter; $\gamma>0, \rho \neq 0$. Does this function represent an average? Give reasons for your answer.
b. Total cost function of a firm over a period of 15 years is estimated as:
$\hat{C}=2500+85.7 X-0.03 X^{2}+0.001 X^{3}$, where $\hat{C}$ is the total cost and $X$ represents the level of output; all the regression parameters are found to be statistically significant and $\mathrm{R}^{2}$ is very high.
Find the shape of Average Variable Cost Curve. At what output level AVC is rising?
5. Consider the following curve, where $P(t)$ stands for population size of fish in a lake:
$P(t)=\frac{L}{1+e^{-r(\beta-t)}}$ where, $L$ be the maximum value of $P(t), r, \beta>0$. What are the properties of this curve? Prove that the curve is skew-symmetric at $t=\beta$, where $P(t)=L / 2$. How do you estimate the unknown parameters like $L, r$ and $\beta$ ? Explain any plausible method.

## Group B

Answer any one of the following questions $15 \times 1=15$

1. Read the following ordinary least square regression output and answer the following questions:

| Source | SS | df | Number of <br> obs $=$ | $\mathbf{4 1 6 5}$ |
| :---: | :---: | :---: | :---: | :---: |
| Model | 370.955 | 10 | F $(10,4154)=$ <br> Prob $>$ F | 0.00000 |
| Residual | 515.95 | 4154 |  |  |
| Total | 886.905 | 4164 | Root MSE | 0.35243 |
|  |  |  | Chi2(1) $=$ | 18.21 |
|  |  |  | Prob>Chi2 $=$ | 0.0000 |
|  |  | Std. |  |  |
| LWAGE | Coef. | Err. | $\mathbf{t}$ | P>t |
| EXP | 0.04045 | 0.00217 | 18.61 | 0.0000 |
| EXP_SQ | -0.0007 | $4.8 E-05$ | -14.24 | 0.0000 |
| WKS | 0.00449 | 0.00109 | 4.12 | 0.0000 |
| OCC | -0.1405 | 0.01472 | -9.54 | 0.0000 |
| SOUTH | -0.0721 | 0.01249 | -5.77 | 0.0000 |
| SMSA | 0.13901 | 0.01207 | 11.51 | 0.0000 |
| MS | 0.06736 | 0.02063 | 3.26 | 0.0010 |
| FEM | -0.3892 | 0.02518 | -15.46 | 0.0000 |
| UNION | 0.09015 | 0.01289 | 6.99 | 0.0000 |
| ED | 0.05654 | 0.00261 | 21.64 | 0.0000 |
| CONSTANT | 5.245465 | 0.071705 | 73.15 | 0.0000 |

Where
EXP = work experience
EXP_SQ=EXP*EXP
WKS = weeks worked
OCC = occupation, 1 if blue collar,
IND $=1$ if manufacturing industry
SOUTH $\quad=1$ if resides in south
SMSA $=1$ if resides in a city (SMSA)
MS $=1$ if married
FEM $=1$ if female
UNION $\quad=1$ if wage set by union contract
ED = years of education
LWAGE $\quad=\log$ of wage $=$ dependent variable in regressions
a. Interpret the coefficients and compute the $95 \%$ confidence interval for the coefficients. [3+3]
b. Explain the underlying null hypothesis and alternative hypothesis for testing the significance of the coefficient associated with FEM variable.
c. Find out the marginal effect of an additional year of experience on wage in the model. [2]
d. How would you test the hypothesis that all coefficients in the model except the constant term are equal to zero?
e. Estimate $R^{2}$ and $\bar{R}^{2}$ from the above output table.
f. Looking at these results, would you conclude that there is evidence of heteroscedasticity in these data?
[1]
2. Read the results of the following regression model and answer the following questions:
$\log$ GSP $_{\text {it }}=\beta_{1} \beta_{2} \log$ PublicK $_{\mathrm{tt}}+\beta_{3} \log$ PrivateK $_{\mathrm{it}}+\beta_{4} \log$ Labor $_{i t}+\varepsilon_{\mathrm{it}}$
where GSP is gross state product. Ordinary least squares regression results appear below. KP is public capital; PC is private capital.

| Source | SS | df | Number of obs= | 816 |
| :---: | :---: | :---: | :---: | :---: |
|  |  |  | F[ 3, 812] | ***** |
| Residual | 6.469532 | 812 | R-Square= | . 9923871 |
|  |  |  | Adjusted R-squared $=$ | . 9923589 |
|  |  |  | Chi2(3) $=$ | =3980.37 |
|  |  |  | Prob $>$ Chi2 $=$ | 0.0000 |
|  | Coef. | Std. Err. | t | $\mathbf{P}>\mathbf{t}$ |
| LOGKP | 0.150783 | 0.0173571 | 8.687 | 0.0000 |
| LOGPC | 0.305538 | 0.0103786 | 29.439 | 0.0000 |
| LOGEMP | 0.598152 | 0.0139001 | 43.032 | 0.0000 |
| CONSTANT | 1.648864 | 0.058336 | 28.265 | 0.0000 |

Covariance Matrix
CONSTANT . 00340
LOGKP -. 00059 . 00030
LOGPC -. 00020 -. 00009078 . 00011

LOGEMP . 00064 -. $00020-.000008636$. 00019
a. Test the hypothesis that the marginal products of (coefficients on) private and public capital are the same.
b. Test the hypothesis of constant returns to scale.
c. Test the two hypotheses simultaneously.
d. How would you test the hypothesis that all coefficients in the model except the constant term are equal to zero? Compute the appropriate test statistic to answer this question.

