## MASTER OF ARTS EXAMINATION, 2022

(1std Year, 2nd Semester)

## **ECONOMICS**

## **ECONOMETRICS AII**

Time: Two hours Full Marks: 30

## Answer any three questions

1. (i) Consider The ARMA model

$$X_{t} = 1.0X_{t-1} - 0.5X_{t-2} + \varepsilon_{t} - 0.9\varepsilon_{t-1} + 0.2\varepsilon_{t-2}.$$

Express  $\mathcal{E}_t$  as a function of X, and lagged values of X, by expanding  $\mathcal{E}_t = (1 - 0.9L + 0.2L^2)^{-1} (1 - 1.0L + 0.5L^2) X_t$  in powers of L.

(ii) Which of the following processes are invertible?

a. 
$$X_{t-1} = 0.8X_{t-1} + 0.4X_{t-2} + \varepsilon_{t}$$

b. 
$$X_{t} = \varepsilon_{t} - 1.8\varepsilon_{t-1} + 0.4\varepsilon_{t-2}$$

(iii) Consider the model

$$y_t = \alpha + \beta x_t + u_t$$

$$u_{t} = \rho u_{t-1} + e_{t}, \ 0 \le \rho \le 1$$

 $e_t \sim IN(0, \sigma^2)$ . By regressing  $\Delta y_t$  on  $\Delta x_t$ , is it possible to get more efficient estimates of  $\beta$  than by regressing  $y_t$  on  $x_t$ .

3+2+2+3=10

- 2. Write short note on
  - a. Full information maximum likelihood method
  - b. Seemingly unrelated regression estimation method

5 x 2=10

3. Consider the model

$$y_1 = \alpha y_2 + \delta x + u_1$$

$$y_2 = \beta y_1 + \gamma x + u_2$$

Where x is exogenous, and the error terms  $u_1$  and  $u_2$  have mean zero and are serially uncorrelated.

[ Turn over

- (i) Write down the reduced form model and state the equations that are related to structural and reduced-form parameters.
- (ii) Show that if  $\gamma = 0$ , then  $\beta$  can be identified.
- (iii) Are the parameters  $\alpha$  and  $\delta$  identified in this case? Why or why not?
- (iv) How would you estimate the structural equations? Which method would you prefer: the system method or the single equation method? Why or why not?

2+2+2+4

4. State two main advantage of panel data over pooled data. Specify a linear static panel data model. Why is the model called static? Suppose that we want to estimate the effect of several variables on annual saving and that we have a panel data set on individuals collected on January 31, 1990, and January 31, 1992. If we include a year dummy for 1992 and use first differencing, can we also include age and gender in the original model? Explain. Consider a panel model describing annual savings and explain what estimation technique will you use to estimate the parameters of the model.

2+1+1+2+4