## Problem Sheet 1A (from Halliday-Resnik)

1. The dot in Fig. P1 represents the initial state of a gas, and the vertical line through the dot divides the $p-V$ diagram into regions 1 and 2. For the following processes, determine whether the work $W$ done by the gas is positive, negative, or zero: (a) the gas moves up along the vertical line, (b) it moves down along the vertical line, (c) it moves to anywhere in region 1 , and (d) it moves to anywhere in region 2.

2. An ideal diatomic gas, with molecular rotation but without any molecular oscillation, loses a certain amount of energy as heat $Q$. Is the resulting decrease in the internal energy of the gas greater if the loss occurs in a constant-volume process or in a constantpressure process?

5 An air bubble of volume $20 \mathrm{~cm}^{3}$ is at the bottom of a lake 40 m deep, where the temperature is $4.0^{\circ} \mathrm{C}$. The bubble rises to the surface, which is at a temperature of $20^{\circ} \mathrm{C}$. Take the temperature of the bubble's air to be the same as that of the surrounding water. Just as the bubble reaches the surface, what is its volume?
6. Figure P6 shows two paths that may be taken by a gas from an initial point $i$ to a final point $f$. Path 1 consists of an isothermal expansion (work is 50 J in magnitude), an adiabatic expansion (work is 40 J in magnitude), an isothermal compression (work is 30 J in magnitude), and then an adiabatic compression (work is 25 J in magnitude). What is the change in the internal
 energy of the gas if the gas goes from point $i$ to point $f$ along path 2 ?
7. A sample of an ideal gas is taken through the cyclic process $a b c a$ shown in P7. The scale of the vertical axis is set by $p_{b}=7.5 \mathrm{kPa}$ and $p_{a c}=2.5 \mathrm{kPa}$. At point $a, T=200 \mathrm{~K}$. (a) How many moles of gas are in the sample? What are (b) the temperature of the gas at point $b$, (c) the
 temperature of the gas at point $c$, and (d) the net energy added to the gas as heat during the cycle?
8. Suppose 0.825 mol of an ideal gas undergoes an isothermal expansion as energy is added to it as heat $Q$. If Fig. P8 shows the final volume $V_{f}$ versus $Q$, what is the gas temperature? The scale of vertical axis is set by $V_{f s}=0.30 \mathrm{~m} 3$, and the scale of the horizontal axis is set by $Q_{s}=1200 \mathrm{~J}$.
9. In the temperature range 310 K to 330 K , the pressure $p$ of a certain nonideal gas is related to volume $V$ and temperature $T$ by

$$
p=(24.9 \mathrm{~J} / \mathrm{K}) \frac{T}{V}-\left(0.00662 \mathrm{~J} / \mathrm{K}^{2}\right) \frac{T^{2}}{V} .
$$



How much work is done by the gas if its temperature is raised from 315 K to 325 K while the pressure is held constant?
10. The temperature of 3.00 mol of an ideal diatomic gas is increased by $40.0^{\circ} \mathrm{C}$ without the pressure of the gas changing. The molecules in the gas has linear translational and rotational degrees of freedom, but the molecules do not oscillate. (a) How much energy is transferred to the gas as heat? (b) What is the change in the internal energy of the gas? (c) How much work is done by the gas? (d) By how much does the rotational kinetic energy of the gas increase?
11. One mole of an ideal diatomic gas goes from $a$ to $c$ along the diagonal path in Fig. P11. The scale of the vertical axis is set by $p a b=5.0 \mathrm{kPa}$ and $p c=2.0 \mathrm{kPa}$, and the scale of the horizontal axis is set by $V b c=4.0 \mathrm{~m} 3$ and $V a=2.0 \mathrm{~m} 3$. During the transition, (a) what is the change in internal energy of the gas, and (b) how much energy is added to the gas as heat? (c) How much heat is required if the gas goes from $a$ to $c$ along the indirect path $a b c$ ?

12. When 20.9 J was added as heat to a particular ideal gas, the volume of the gas changed from 50.0 cm 3 to 100 cm 3 while the pressure remained at 1.00 atm . (a) By how much did the internal energy of the gas change? If the quantity of gas present was $2.00 \times 10^{-3} \mathrm{~mol}$, find (b) $C p$ and (c) $C_{V}$.
13. The volume of an ideal gas is adiabatically reduced from 200 L to 74.3 L . The initial pressure and temperature are 1.00 atm and 300 K .The final pressure is 4.00 atm . (a) Is the gas monatomic, diatomic, or polyatomic? (b) What is the final temperature? (c) How many moles are in the gas?
14. Figure P14 shows a cycle undergone by 1.00 mol of an ideal monatomic gas. The temperatures are $T_{1}=300 \mathrm{~K}, T_{2}=600 \mathrm{~K}$, and $T_{3}=455$ K. For $1 \rightarrow 2$, what are (a) heat $Q$, (b) the change in internal energy $\Delta E_{\text {int }}$, and (c) the work done $W$ ? For $2 \rightarrow 3$,
 what are (d) $Q$, (e) $\Delta E_{\text {int }}$, and (f) $W$ ? For $3 \rightarrow 1$, what are (g) $Q$, (h) $\Delta E_{\text {int }}$, and (i) $W$ ? For the full cycle, what are (j) $Q$, (k) $\Delta E_{\text {int }}$, and (l) $W$ ? The initial pressure at point 1 is $1.00 \mathrm{~atm}\left(=1.013 \times 10^{5} \mathrm{~Pa}\right)$. What are the $(\mathrm{m})$ volume and ( n ) pressure at point 2 and the ( o ) volume and ( p ) pressure at point 3 ?

