

M.E. (Water Resources and Hydraulic Engineering) EXAMINATION
(Evening), 2019
(2nd Year-2nd Semester)
Groundwater Dynamics
Paper-IX

Time: Three hours

Full Marks: 100

Answers any five questions

1. (a) Why Copper-Jacob straight line method is advantageous over the Thies method? State its limitation.

(b) A well penetrating a confined aquifer is pumped at a uniform rate of 3000 m³/day. Drawdowns during the pumping period are measured in an observation well 80 m away, observations of 't' and 's' are listed below in a tabulated form.

Time, t(min)	s(m)	Time, t (min)	s(m)
0	0	24	0.72
1	0.020	30	0.76
1.5	0.27	40	0.81
2.0	0.30	50	0.85
2.5	0.34	60	0.90
3.0	0.37	80	0.93
4.0	0.41	100	0.96
5.0	0.45	120	1.00
6	0.48	150	0.104
8	0.53	180	1.07
10	0.57	210	1.10
12	0.60	240	1.12
14	0.63		
18	0.67		

The well function $W(u)$ and u are also given in a tabular form

u	1	10^{-1}	10^{-2}	10^{-3}	10^{-4}	10^{-5}
$W(u)$	0.219	1.82	4.04	6.33	8.63	10.94

Calculate transmissivity and storativity of the confined aquifer using Theis Method.

(4+16)=20

2. (a) In a test of a confined aquifer, the pumping rate was 1000 m³/day. Drawdown and time data were collected at an observation well 350 m away (table given below). Determine the transmissivity and storativity of the aquifer using the Copper-Jacob Straight Line Method.

Table: Drawdown measured at an observation well 300 m away

Time(min)	s(m)	Time(min)	s(m)
0	0	24	0.72
1	0.020	30	0.76

1.5	0.27	40	0.81
2.0	0.30	50	0.85
2.5	0.34	60	0.90
3.0	0.37	80	0.93
4.0	0.41	100	0.96
5.0	0.45	120	1.00
6	0.48	150	0.104
8	0.53	180	1.07
10	0.57	210	1.10
12	0.60	240	1.12
14	0.63		
18	0.67		

(b) Prove that drawdown (s) can be expressed by "Copper-Jacob Method" with the series expression for $W(u)$ by equation

$$W(u) = -0.5772157 - \ln(u)$$

is given by

$$s = \frac{2.3Q}{4\pi T} \log \frac{2.25Tt}{r^2 S}$$

where Q is the discharge of pumping well, T and S are the Transmissivity and Storativity with time ' t ' and r is the radial distance between main well to observation well.

$$15+5=20$$

- 3) a) "It is a good practice to measure residual drawdowns" – justify the statement.
 b) A confined aquifer is pumped at 1200 m³/day. At time $t_0 = 220$ min drawdowns were recorded in nine observation wells (table below). Calculate the transmissivity and storativity of the aquifer.

Table : Values of drawdown versus distance measured at $t_0 = 220$ min.

$r(m)$	$s(m)$	$r(m)$	$s(m)$
3.0	10.6	75	4.1
15	7.3	90.0	3.9
30.0	5.9	120.0	3.13
45	5.1	150.0	2.7
60.0	4.5		

- c) A well pumping at a uniform rate of 2500 m³/day was shut down after 240 min, thereafter, measurements of s' and t' tabulated in table below were made in an observation well. Find the transmissivity of the aquifer.

Recovery Test Data (Pump shut down at $t = 240$ min)

t' (min)	s' (m)	t' (min)	s' (m)
1.0	0.89	20	0.55
2.0	0.81	30	0.38
3.0	0.76	40	0.34
5.0	0.68	60	0.28
7.0	0.64	80	0.24
10.0	0.56	100	0.21
15.0	0.49	140	0.17
		180	0.14

(2+8+10)

4. (a) Derive the governing equation for the two dimensional flow in an unconfined aquifer of a homogenous fluid in anisotropic homogenous porous media based on Dupuit approximation.

(b) A homogeneous anisotropic confined aquifer is 35 m thick and has principal hydraulic conductivities of $K_{xx} = 36$ m/d and $K_{yy} = 16$ m/d. Determine the principal transmissivities and state the differential equation describing the piezometric head distribution in the absence of recharge. Would the governing equation be any different if the aquifer were 60 m thick, $K_{xx} = 18$ m/d, and $K_{yy} = 8.0$ m/d?

(15+5)=20

5. (a) Deduce the governing equation for radial flow in a confined steady, homogenous and isotropic aquifer.

(b) Two observation wells were found at horizontal distance of 18 m and 38 m from the pumping well. The drawdowns were observed as 2.55 m and 1.30 m during pumping. The initial position of the water table was 2.1 m and aquifer thickness was 15.5 m. Calculate the coefficient of permeability if the pumping rate is 1800 L/min.

(14+6)=20

6. (a) What are the factors depends on coefficient of permeability in case of porous material? Deduce an expression the coefficient of permeability for fined grained soils.

(b) Show that equation which describes the transient drawdown in the piezometric head caused by a fully penetrating pumping well in a confined aquifer in unsteady-state solutions

$$s'(u) = \frac{Q}{4\pi T} W(u)$$

Where $\int_u^\infty \frac{e^{-x}}{x} dx = W(u)$ Well function and $S'(u) = \text{drawdown}$, $T = \text{Transmissivity}$, $Q = \text{discharge of well}$

(c) Constant head permeability test was carried out on a cylindrical sample of sand 155 cm in diameter and 16 cm in height. If 180 cm³ of water was collected in 1.80 minutes under a 35 cm head, calculate the coefficient of permeability and velocity of flow.

(6+8+6)=20

7. (a) A confined aquifer of thickness 30 m is pumped at a rate of 6480 m³/d from a well of radius 0.3 m. The superposition of the W(u) versus ln(u) curve onto the ln(s) versus ln(r²/t) curve is found with the help of time versus drawdown data in a monitoring well located 100 m from the pumping well, and the axis displacement indicates that $\alpha = 15.1$ and $\beta = (-) 0.557$, calculate the value of transmissivity (T) in m²/d.

- (i) 900 (ii) 1000 (iii) 1100 (iv) 1200

b) By considering the above problem 'a', what is the storage co-efficient of the aquifer?

- (i) 0.0001 (ii) 0.0010 (iii) 0.00001 (iv) 0.010

c) By considering the above problem 'a', what is the hydraulic conductivity (in m/d) of the aquifer?

- (i) 10 (ii) 20 (iii) 30 (iv) 40

d) The hydraulic conductivity distribution in a 30-m thick stratified aquifer is given in the following table

Depth (m)	K _{xx}	K _{yy}	Depth (m)	K _{xx}	K _{yy}	Depth (m)	K _{xx}	K _{yy}
0-5	25	30	5-10	30	33	10-15	40	37
15-20	32	28	20-25	22	19	25-30	13	11

Estimate the effective hydraulic conductivity (in m/d) when the table is 4 m below the ground surface

- (i) 27.3 and 25.8 (ii) 30.3 and 28.8 (iii) 33.3 and 31.8 (iv) 36.3 and 34.8

e) By considering the above problem 'd', would the effective hydraulic conductivity (in m/d) be the same at a location where the water table is 5 m below the ground surface?

- (i) 27.4 and 25.6 (ii) 30.4 and 28.6 (iii) 33.4 and 31.6 (iv) 36.4 and 34.8

f) What is the well function 'W(u)', if 'u' is a dimensionless term to be estimated as 1.01×10^{-10} ? Assume neglecting second and higher order terms.

- (i) 22.44 (ii) 32.44 (iii) 42.44 (iv) 52.44

g) For the well, determine the 'u' value at the well where radius of well and the radial distance are 304.8 mm and 1000 mm respectively after 1 year of pumping at a rate of 500 m³/d with a transmissivity of the aquifer of 879 m²/d. The storage co-efficient of the aquifer is 0.00035.

- (i) 1.53×10^{-11} (ii) 2.53×10^{-11} (iii) 3.53×10^{-11} (iv) 4.53×10^{-11}

h) If W(u) value is found to be 32.84, determine the drawdown at the well in case of unsteady-state confined aquifer. The well is being pumped at a rate of 500 m³/d with a transmissivity of the aquifer of 879 m²/d.

- i) 1.5 m ii) 2.5 m iii) 3.5 m iv) 0.5 m

i) During a falling head permeability test, the initial head at $t_1=30$ min is 80 cm. At $t_2=60$ min, the head is 75 cm. The diameter of the standpipe and the specimen are 1.5 cm and 20 cm, respectively. The length of the specimen is 30 cm. Determine the hydraulic conductivity of the specimen.

- (j) 6.04×10^{-8} m/s (ii) 7.04×10^{-5} m/s (iii) 6.04×10^{-5} m/s (iv) 7.04×10^{-8} m/s

J) What is the entrance velocity, the if the well discharge, clogging coefficient, screen diameter, screen length and the percentage of open area in the screen are $50 \text{ m}^3/\text{h}$, 0.5, 100 mm, 20 m and 60% respectively?

- (k) 0.0074 m/s (ii) 0.074 m/s (iii) 0.0094 m/s (iv) 0.094 m/s
(2x10)=20