7. (a) Consider a mono-atomic one-dimensional lattice (Figure 2), where *M* and *K* are the mass of the atom and inter-atomic spring constant, respectively.

Figure 2 : Mono-atomic one-dimensional lattice

- (i) Write down the equation of motion for the vibration of the *n*-th atom.
- (ii) Obtain the expression of frequency of vibrational modes.
- (b) Obtain the expression of Bragg's law for X-ray diffraction in crystals.
- (c) If the first order Bragg's peak for X-rays of wavelength 2.50 Å is observed at 30°, determine the inter-planar spacing of the reflecting planes. [(2+4)+2+2=10]
- 8. (a) (i) Define magnetization (M). (ii) Write down the equation relating magnetization, magnetic induction (B) and external magnetic field (H). (iii) Find the expression of magnetic moment, μ_m , due to the circular (orbital) motion of an electron about its nucleus.
 - (b) Develop the Langevin (classical) theory of diamagnetism and derive the expression of diamagnetic susceptibility. [(1+1+2)+6=10]

BACHELOR OF SCIENCE EXAMINATION, 2019

(2nd Year, 4th Semester)

PHYSICS

Paper : GE - 4

Time : Two hours

Full Marks : 50

The figures in the margin indicate full marks.

Answer any *five* questions.

- 1. (a) Explain Wien's displacement law. Deduce Wein's displacement law from Planck's radiation law.
 - (b) What are the difficulties of classical physics to explain the black body radiation ?
 - (c) What is the maximum wavelength of electromagnetic radiation which can eject electrons from a metal having a work function of 3 eV? [(2+4)+2+2=10]
- 2. (a) Explain why the classical electromagnetic theory fails to explain the photoelectric effect.
 - (b) The photoelectric threshold for a certain metal is 300 nm. Determine the maximum energy of the electrons ejected by a radiation of 200 nm. Given $h = 6.625 \times 10^{-34}$ Js.
 - (c) Discuss the theoretical background of Millikan's experiment to verify Einstein's photo electric equation. [2+3+5=10]

- 3. (a) What are the characteristics of de Broglie matter wave ? Deduce the expression for the wavelength of de Broglie matter wave.
 - (b) Does the concept of Bohr orbit violate the Heisenberg's uncertainty principle ?
 - (c) The position and momentum of a 1 KeV electron are simultaneously determined. If its position is located to within 1 Å, what is the percentage of uncertainty in its momentum?
 - (d) What do you understand by group velocity and phase velocity for the de Broglie wave?

[(2+4)+1+2+1=10]

- 4. (a) What is the origin of nuclear magnetic moment?
 - (b) What do you understand by the binding energy of the nucleus. Explain the significance of the plot of binding energy per nucleon versus mass number.
 - (b) 1 gm of radium is reduced by 2.1 mg in 5 years by α -decay. Calculate the half-life of radium.
 - (d) What is the difference between secular and transient radioactive equilibrium? [2+(1+2)+3+2=10]
- 5. (a) A particle is restricted to move over the *x*-axis and its quantum mechanical state is described by the wave function, $\Psi = Ax$, (A is a constant) when 0 < x < 1 and $\Psi = 0$, elsewhere.

- (i) Find the probability that the particle can be found between x = 0.20 and x = 0.40.
- (ii) Find the expectation value, $\langle x \rangle$, of the particle's position.
- (b) By using the time-dependent Schrodinger equation and its complex conjugate obtain the equation of continuity of probability density, $\rho = \psi^* \psi$. [(2+3)+5=10]
- 6. Consider the step poential as described in Figure 1, where energy (E) of the incoming particle of mass *m* is lower than the height of the potential (V_0) , i, e., $E < V_0$.
 - (a) Write down the Schrodinger equations in regions I and II, separately.
 - (b) Derive the expressions of wave functions in the respective regions, by solving the Schrödinger equations, separately.
 - (c) Find the expressions of reflection and transmission amplitudes with the help of those wave functions.



Figure 1 : A particle of energy E approaches a step potential of height V_0 , where $E < V_0$. (Turn Over)