

BACHELOR OF ENGINEERING (ELECTRICAL ENGINEERING) EXAMINATION,2019  
(SECOND YEAR FIRST SEMESTER)  
FIELD THEORY

Time:3 hours

Full Marks:100

(50 marks for each part)

Use separate Answer-script for each part

## PART-I

Answer any three questions. Two marks for neatness. All symbols have their usual significance

1. a) What is the fundamental definition of curl of a vector field?  
Also derive the expression for curl of a vector field  $\mathbf{F}$ , written as  $\nabla \times \mathbf{F}$  where,  $\nabla$  is the vector differential operator in Cartesian coordinates. What is the physical significance of the curl of a vector field?  
b) Establish the Stoke's Theorem.
 

10+6=16
2. a) Show that  $\nabla \times \mathbf{H} = \mathbf{J}$ .  
b) Using Biot- Savart Law derive  $B$  ( $\text{wb/m}^2$ ) at the centre of a square current loop of 4m side having current 100A in clockwise direction and derive the formulae used if any.
 

6+10 =16
3. a) Establish  $\nabla \times \mathbf{E} = - \partial \mathbf{B} / \partial t$  and show the pictorial view of this relation.  
b) Derive an expression for Self-Inductance per unit length for a Coaxial Cable of solid inner conductor assuming the cable inner conductor radius ' $R_1$ ' and hollow outer conductor radius ' $R_2$ '.
 

8+8=16
4. a) Derive electromagnetic (E.M. ) wave equation for Electric Field (E). Using E.M. wave equation in free space, obtain an analytical solution of the wave equation of Electric Field (E) considering it as a plane wave.  
b) What is "Poynting Vector"?
 

12+4=16
5. Write short notes on any two:
 

8+8=16

  - a)  $\nabla \cdot \mathbf{J} = 0$  and  $\nabla \cdot \mathbf{B} = 0$ .
  - b)  $\nabla \times \mathbf{H} = \mathbf{J} + \partial \mathbf{D} / \partial t$  and the displacement current?
  - c) Electromagnetic (E.M. ) wave propagations for  $\mathbf{E}$  &  $\mathbf{H}$  field in free space.

[ Turn over

**BACHELOR OF ENGINEERING  
IN ELECTRICAL ENGINEERING (EVENING) EXAMINATION, 2019  
(2nd Year, 1st Semester)**

**SUBJECT: FIELD THEORY**

Time: Three Hours

Full Marks: 100  
(50 Marks for each part)

**Use a separate Answer-Script for each part**

Two marks for neat and well-organized answers

Question No.	Part-II	Marks
Answer any three questions		
1.	(a) Derive the differential form of Gauss's Law. Hence, show how it leads to Divergence Theorem.	6+2
	(b) The potential field in a medium having relative permittivity of 3.8 is given by $\phi = 3x^3y^2 + 2y^3z^2 - 4x^2z^3$ volts. Find the electric flux density in vector form at the point (1,4,2)m.	8
2.	(a) Derive the expression for the electric field intensity at a particular point located at a height "h" on the axis of a ring charge of radius "r" having uniform charge density.	8
	(b) A point charge $Q_1 = +0.8 \mu\text{C}$ is located at (2,1,4)m and another point charge $Q_2 = -0.6 \mu\text{C}$ is located at (0,3,1)m. Calculate the electric field intensity at (1,4,1)m in vector form. Medium is air.	8
3.	(a) For a single core cable, find the conductor radius 'r' for minimum electric field intensity on the inner conductor surface for a fixed outer sheath radius 'R'. Derive the formulae used.	8
	(b) Prove that the electric field intensity just off the conductor surface is twice the electric field intensity on the conductor surface.	8
4.	(a) Derive the FDM equations for the unknown node potentials in 2-D system with equal nodal distances in homogeneous medium.	8
	(b) State and prove Uniqueness Theorem.	8
5.	(a) Explain how the field due to co-axial cylindrical system can be analyzed with the help of conformal transformation.	8
	(b) Derive an expression for the volume density of energy stored in an electric field.	8