

M. CHEMICAL ENGINEERING FIRST YEAR SECOND SEMESTER SUPPLEMENTARY
EXAMINATION 2025

SUBJECT: MODELLING AND SIMULATION OF CHEMICAL PROCESSES

Time: Three hours

Full Marks 100

State all the assumptions. Assume any missing data.

No. of Questions	Answer any 2 questions from question 1-3 and all the rest.	Marks
1.	<p>Consider a plate type 5th stage (counter current) absorption column. The liquid feed (entering at the top plate) flow rate $L=100$ kgmole inert oil/hr, gas feed (entering at the bottom plate) flow rate $V =120$ kgmole air/hr, liquid feed composition $x_f=0.0$ kgmole Benzene/kgmole inert oil, gas feed composition $y_6=0.25$ kgmol Benzene/kgmole air. Assume that liquid molar hold up for each stage is $M =6$ kgmol. Assume a linear equilibrium relationship $y_i=ax_i$; $a=0.5$.</p> <p>Write the steady state model equations for any intermediate stage i, for top stage and bottom stage. Derive the steady state matrix equations for plate composition (x_i). Name the numerical technique for solution of steady state plate-composition-</p>	(15)
2.	<p>Consider a multicomponent distillation column having 3 equilibrium stages, a partial condenser, a partial reboiler. The saturated liquid feed consisting of 3 components is introduced at the middle plate.</p> <p>(i) Write the MESH equations. (ii) You need to solve the MESH equations using Bubble Point method. Draw the algorithm (flowchart).</p>	(15)
3.	<p>Consider single-stage multi-component isothermal flash distillation. Draw the process and define the variables. The feed temperature, composition, equilibrium temperature and pressure are known. Write the generalized model equations.</p> <p>(ii) For composition independent equilibrium constant K values, simplify the model equations for the simulation of percent vaporization (ψ), liquid and gas phase composition. Draw the information flow diagram</p>	
4.	<p>Consider a process that uses bacteria to produce antibiotic. The reactor is contaminated with protozoan that consumes bacteria. Assume that predator – prey equations are used to model the system (x_1 : bacteria (prey), x_2 : protozoa (predator). The time unit is in days.</p> $\frac{dx_1}{dt} = \alpha x_1 - \gamma x_1 x_2 ; \frac{dx_2}{dt} = \epsilon \gamma x_1 x_2 - \beta x_2$ <p>(i) What are the trivial and nontrivial steady state concentration x_1s, x_2s?</p> <p>(ii) Use the nontrivial steady state values of x_1 and x_2 to scale the variables as $y_1=x_1/x_1s$ and $y_2=x_2/x_2s$ and derive the governing equations in terms of scaled variables y_1 and y_2.</p>	(2+2) (6)

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5.	<p>(iii) Linearize the scaled equations and write in state space form. Find the eigen values of the Jacobian around the nontrivial steady state (i.e. $y_1s=1, y_2s=1$) in terms of α and β. Evaluate the eigen values for $\alpha = \beta=1$. Discuss about the stability of the nontrivial steady state. What type of phase plane plot (y_1 vs y_2) do you expect?</p> <p>Consider a non-isothermal CSTR with jacket cooling where reactant A is converted to product by a first order reaction ($A \longrightarrow B$). Assume constant volume system and constant density system. Write the dynamic model equations (overall material balance, component balance and energy balance). Linearize the model equations around the steady state and express the dynamic equation in state-space form (in terms of deviation variables). Check the stability of the steady state $C_{As}=5.518, T_s=339.1$, for the following set of parameters and input variable data.</p> <p>Data: $F/V, \text{ hr}^{-1}=1, K_0 \text{ hr}^{-1} = 9703*3600; (-\Delta H) \text{ Kcal/kgmol} = 5960; E, \text{ kcal/kgmol} = 11843; \rho C_p \text{ kcal/m}^3 \text{ }^\circ\text{C} = 500; T_f \text{ }^\circ\text{C} = 25; C_{Af} \text{ kgmol/m}^3 = 10; UA/V \text{ kcal/m}^3 \text{ }^\circ\text{C hr} = 150; T_j \text{ }^\circ\text{C} = 25.$</p> <p>Derive a single steady state energy balance equation $G(T_s, \mu) = 0$ (by $Q_{gen} - Q_r = 0$) where T_s is the state variable and μ is the vector of physical parameters that can be varied. Discuss about multiple steady state behaviour and cusp catastrophe.</p> <p>A tubular chemical reactor (plug flow reactor with axial dispersion) of length L and cross section 1 cm^2 is employed to carry out a first order chemical reaction in which material A is converted to product B. The specific rate constant is $k \text{ s}^{-1}$. Feed rate is $u \text{ m}^3/\text{s}$ and feed concentration is $C_0 \text{ mol m}^{-3}$ and axial diffusivity is assumed to be constant $D \text{ m}^2/\text{s}$. Assume that there is no volume change during the reaction and steady state conditions are established. Derive the differential model equation for concentration of solute as a function (z) axial position. Nondimensionalize the equations and boundary conditions and obtain the dimensionless numbers. For numerical solution discretize the governing equation by Finite difference method and insert the boundary conditions to derive the matrix equation. What kind of matrix would you get? Mention the numerical algorithm to solve the same.</p>	<p>(6+4)</p> <p>(15)</p> <p>(15)</p> <p>(10+10)</p>
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