

**BACHELOR OF ENGINEERING (ELECTRICAL ENGINEERING)
FIFTH YEAR SECOND SEMESTER - 2024**

ADVANCED CONTROL THEORY

Time : 3 hours

Full Marks : 100
(50 marks for each part)

Use separate answer-scripts for each parts.

Part-I

Answer any three questions. Two marks are reserved for neatness.

Answer all parts of a question in the sequential order.

- 1.a) Explain the concept of “equilibrium” in the context of analysis of nonlinear systems.
- b) Derive the “error dynamic model” of any nonlinear system and explain its advantage in control system analysis and design.
- c) Explain with suitable sketches, the “Hard” and “Soft” nonlinearities observed in dynamic systems.

[3+(4+1)+8=16]

2. a) Explain the concept of stability of a nonlinear system when its equilibrium state lies in the n-dimensional state space. In this context, explain the concept of asymptotic stability, marginal stability, instability and domain of attraction.
- b) When will you call a system to be “exponentially stable”?
- c) Explain the first method of Lyapunov for the assessment of stability of nonlinear systems.

[(4+4)+2+6=16]

3. a) Compare the Jacobian Linearization and Feedback Linearization methods. Hence suggest which method would be useful in what situation.
- b) Derive the control law for input-state feedback linearization for the following system:

$$\dot{x} = f(x) + g(x)u$$

[(6+2)+8=16]

[Turn over

4. a) Describe the basic steps of Sliding Mode Controller design for the following second order nonlinear system:

$$\ddot{x} = f(\dot{x}, x) + u$$

where x is a scalar and $f(\cdot, \cdot)$ be an uncertain function, where the estimate of $f(\cdot, \cdot)$ is known and bounded as following:

$$|f(\dot{x}, x) - \hat{f}(\dot{x}, x)| \leq F(\dot{x}, x), \forall \dot{x}, x$$

b) Why “Chattering” is observed in Sliding Mode Controllers? What are the measures to reduce it?

[12+(2+2)=16]

5) Write short note **on any two** from the following:

[8+8=16]

- a) Various properties of phase plane portraits of any nonlinear system.
- b) Phase plane portraits of second order LTI system with different damping ratios.
- c) Krasovskii's method of determination of Lyapunov candidate function.
- d) Various significant features of nonlinear systems.

B. E. (ELECTRICAL ENGINEERING) 5TH YEAR 2ND SEMESTER EXAMINATION, 2024**Subject: ADVANCED CONTROL THEORY****Time: Three Hours****Full Marks: 100****Part II** (50 marks)

Question No.	<u>Answer <i>Any Five</i> questions (5×10)</u>	Marks
Q1 (a)	(i) What is meant by Plant Uncertainty? How such uncertainties are classified?	2+2
	(ii) Discuss how the study of Robust Control facilitates one to take care of such uncertainties?	2
(b)	Draw the block diagram of a generalized feedback control scheme involving plant with any one of such uncertainties.	4
Q2 (a)	(i) Define Sensitivity of a system with respect to variations in its parameter values.	2
	(ii) Show how feedback can be used to reduce the sensitivity in respect of changes in the plant parameters.	4
(b)	For a negative unity feedback system with forward path transfer function	
	$G(s) = \frac{1}{s + \alpha}$	4
	Derive the expression for the sensitivity of the closed-loop system with respect to variations in the values of α .	
Q3 (a)	Define Gain Margin (GM) of a system.	2
(b)	(i) With the help of a block diagram show how an uncertain gain K with a multiplicative uncertainty can be represented.	4
	(ii) Assuming that the gain K varies between K_{min} and K_{max} derive the nominal gain and the perturbation range for an uncertainty factor that may have any real value of magnitude not exceeding unity.	4
Q4 (a)	(i) Define 2-norm and ∞ -norm of a vector.	2+2
	(ii) Show that ∞ -norm is always less than the 2-norm of a vector.	2
(b)	Find 2-norm and ∞ -norm for a continuous time function defined as	
	$f(t) = \begin{cases} t & -5 < t < 3 \\ 0 & otherwise \end{cases}$	4

Q5 (a) State Small Gain Theorem for robust stability. 2

(b) Consider a feedback control system with a feedback controller C and a plant with unstructured additive uncertainty given as

$$\tilde{G} = G + \Delta_A$$

where,

\tilde{G} represents true plant dynamics,

G is a model of plant dynamics,

and Δ_A represents unstructured additive uncertainty.

Assume that Δ_A is stable and its upper bound is known.

(i) Draw the block diagram of the system and derive the block diagram showing a generalized plant with unstructured additive uncertainty. 4

(ii) Obtain the condition that a feedback controller C must satisfy to ensure robust stability. 4

Q6 (a) With the help of block diagrams show the different ways an uncertainty can affect a nominal plant. 4

(b) Consider a control system consisting of the generalized plant $P(s)$ and the controller $K(s)$ as shown in Figure Q6(b). Obtain the transfer function that relates the controlled variable, $z(s)$, with the exogenous disturbances, $w(s)$. 6

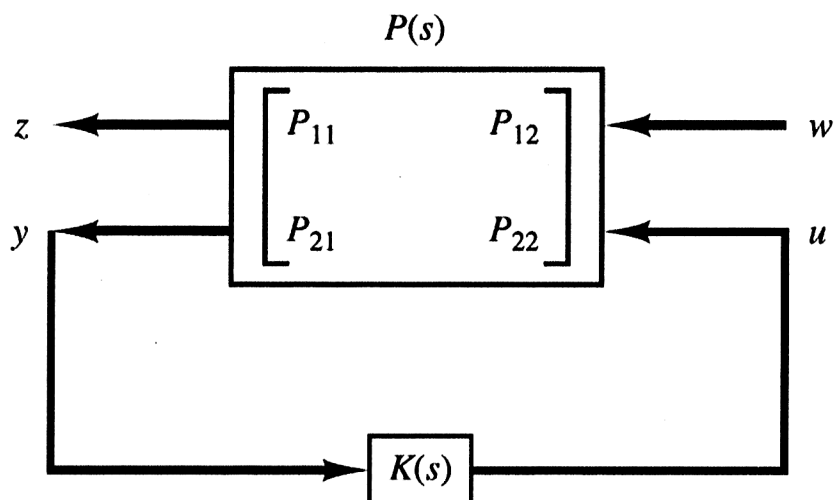


Figure Q6(b)

- Q7 (a) Define Interval Polynomial Family. 2
 (b) State Kharitonov's Theorem related to robust stability. 2
 (c) Consider a system with the characteristic equation given as

$$s^3 + a_2s^2 + a_1s + a_0 = 0$$

The uncertainties associated with the co-efficients are given as

$$8 \leq a_0 \leq 60 \quad 6$$

$$12 \leq a_1 \leq 100$$

$$7 \leq a_2 \leq 25$$

Derive the Kharitonov polynomials.

- Q8 (a) Define Robust Stability and Robust Performance problems. 2
 (b) Consider a feedback control system with unstructured multiplicative uncertainty as shown in Figure Q8(b) with

$$\tilde{G} = G(1 + \Delta_M)$$

where,

\tilde{G} : true plant dynamics,

G : model of plant dynamics and

Δ_M : unstructured multiplicative uncertainty.

Assume that Δ_M is stable and its upper bound is known.

- (i) Develop the block diagram showing the generalized plant with unstructured multiplicative uncertainty. 4
 (ii) Derive the conditions that the feedback controller K must satisfy to ensure robust performance such that the output $y(t)$ follows the input $r(t)$ as closely as possible. 4

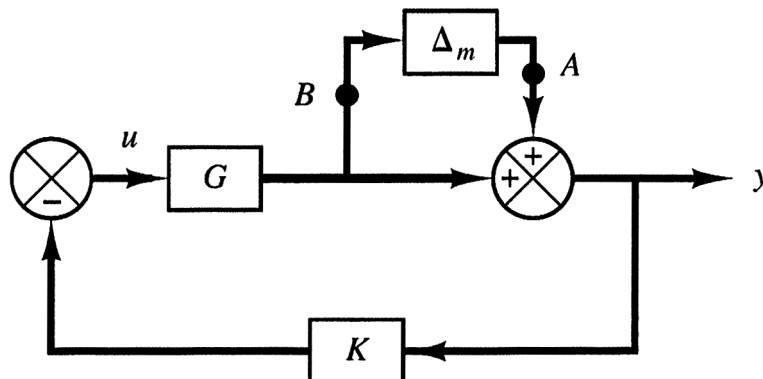


Figure Q8(b)