

MASTER OF ARTS EXAMINATION, 2025**DEPARTMENT OF ECONOMICS****1st Year, 2nd Semester****Subject Code : ECO/A/C 8.3****ECONOMETRICS AII****Time : Two Hours****Full Marks : 30****Group – A****(Compulsory)**

4×1=4

1. (a) Define structural form model.
- (b) What is the use of Hausman test in panel data regression ?
- (c) What is the implication of seemingly unrelaterd regression with identical regressors ?
- (d) What is the primary advantage of the Full Information Maximum Likelihood (FIML) method in statistical analysis ?

Group – B**(Answer any two questions)**

2×5=10

2. (a) Is the following MA(2) process invertible ?

$$X_t = \epsilon_t - 0.9\epsilon_{t-1} + 0.2\epsilon_{t-2}$$
- (b) Compute the auto correlation function (acf) for the following AR (2) process

$$X_t = 0.9X_{t-1} - 0.2X_{t-2} + \epsilon_t$$

2.5+2.5

3. Derive two stage least square (2 SLS) estimate in a simultaneous equation system consisting of G number of endogenous and K number of exogenous variables. Show that 2 SLS estimates are consistent. 3+2
4. Consider a simple Keynesian model with no government

$$C_t = \alpha + \beta Y_t + u_t \quad t = 1, 2, \dots, T$$

$$Y_t = C_t + I_t$$

Where C_t denotes consumption, Y_t denotes disposable income, and I_t denotes autonomous investment. This is a system of two simultaneous equations, also known as structural equations with the second equation being an identity.

Show that β_{OLS} overstates β if $0 \leq \beta \leq 1$

Group – C

(Answer any two questions)

2×8=16

5. Consider the following demand and supply equations :

Demand : $Q = a - bP + u_1$

Supply : $Q = c + dP + eW + fL + u_2$

where W denotes weather conditions affecting supply, and L denotes the supply of immigrant workers available at harvest time.

- (a) Write this system in the matrix form. 1
- (b) What does the order-condition for identification say about these two equations ? 1+1+2
- (c) Suppose researcher decides to estimate the above mentioned model using two stage least square (2SLS) method. Is the 2SLS an appropriate method, why ? Write the steps to be followed to estimate the above model. Can you estimate the following parameters : a, b, c, d, e, f ? [Justify your statement]. 1+3+1

6. Consider the simple panel data regression model

$$y_{it} = \beta x_{it} + u_{it}$$

$$i = 1, 2, \dots, N ; t = 1, 2, \dots, T$$

Where, $u_{it} = \mu_i + v_{it}$ where $\mu_i \sim \text{IID}(0, \sigma^2 \mu)$ and $v_{it} \sim \text{IID}(0, \sigma^2 v)$.

Discuss appropriate method of estimating the above model with proper justification. 8

7. For the MA (1) model

$$y_t = \epsilon_t + \theta \epsilon_{t-1}$$

$$t = 1, 2, \dots, T; \text{ with } \epsilon_t \sim \text{IIN}(0, \sigma_\epsilon^2)$$

- (a) Show that $E(y_t) = 0$ and $\text{var}(y_t) = \sigma_\epsilon^2(1 + \theta^2)$ so that the mean and variance are independent of t .
- (b) Show that $\text{cov}(y_t, y_{t-1}) = \theta \sigma_\epsilon^2$ and $\text{cov}(y_t, y_{t-s}) = 0$ for $s > 1$ which is only dependent on s , the distance between the two time periods. Conclude from parts (a) and (b) that this MA (1) model is weakly stationary.
- (c) Discuss the method of estimating the above model. 2+3+3=8